



Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

Acoustics II: loudspeakers

Reto Pieren
2024

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electrostatic

radiation

directivity
radiated power
velocity distribution of a
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membrane driver principles:

- ▶ electrodynamic
- ▶ electrostatic

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excitation: force F acting on a wire of length ℓ carrying current i and located in a magnetic field B :

$$F = B \times \ell \cdot i$$

the other way round, a voltage U is induced for a wire moving with velocity u :

$$U = B \times \ell \cdot u$$

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electrostatic transducer

electrostatic transducer

excitation: electrostatic force F acting on a plate condenser of area S and distance x and for a voltage U :

$$F = \frac{\epsilon_0 S U^2}{2x^2}$$

with: ϵ_0 : electric field constant = $8.85 \times 10^{-12} \text{ AsV}^{-1} \text{ m}^{-1}$

- ▶ non-linear relation between force and voltage asks for biasing!
 - ▶ \approx linear behavior for small variations

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sound radiation by a moving membrane

sound radiation by a moving membrane

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diffraction of plane wave at a circular opening (assuming Kirchhoff approximation):

movie: [diffraction at circular opening](#)

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Calculation of sound pressure \check{p} for a circular piston

- ▶ of area S
- ▶ with velocity \check{v}_n
- ▶ in an ∞ wall

with help of the Rayleigh-Integral:

$$\check{p} = \frac{j\omega\rho}{2\pi} \int_S \check{v}_n \frac{1}{r} e^{-jkr} dS$$

Far field directivity for circular piston

for distances not too small: $1/r \approx r_0 = \text{const.}$

$$\check{p}(\theta) \approx \frac{\check{v}_n}{r_0} jka^2 \rho c \frac{J_1(ka \sin \theta)}{ka \sin \theta}$$

where

\check{v}_n : velocity of the piston

r_0 : reference distance

k : wave number = $2\pi/\lambda$

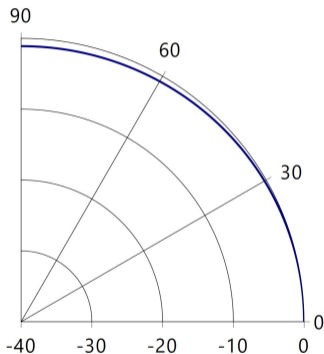
a : radius of piston

J_1 : Bessel function

θ : angle to the receiver position

Directivity

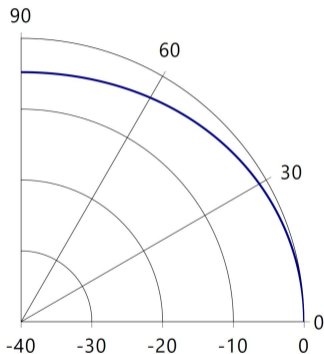
Directivity of the circular piston radiator in the ∞ -wall:



$ka = 1$, e.g. $a = 0.15$ m, $f = 360$ Hz

Directivity

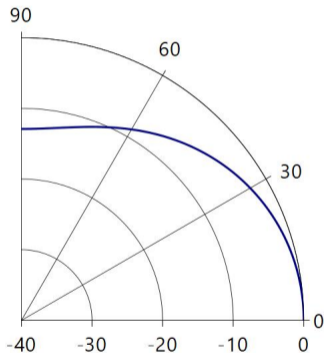
Directivity of the circular piston radiator in the ∞ -wall:



$ka = 2$, e.g. $a = 0.15$ m, $f = 720$ Hz

Directivity

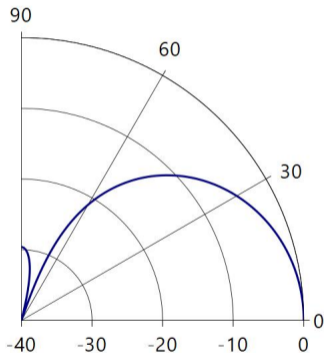
Directivity of the circular piston radiator in the ∞ -wall:



$ka = 3$, e.g. $a = 0.15$ m, $f = 1080$ Hz

Directivity

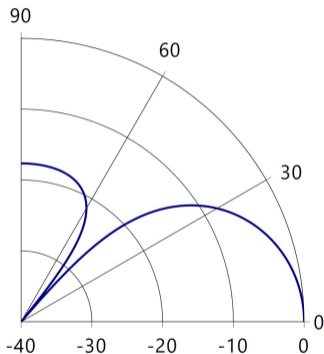
Directivity of the circular piston radiator in the ∞ -wall:



$ka = 4$, e.g. $a = 0.15$ m, $f = 1440$ Hz

Directivity

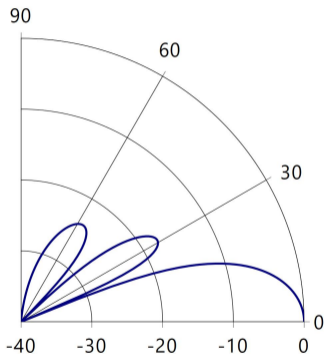
Directivity of the circular piston radiator in the ∞ -wall:



$ka = 5$, e.g. $a = 0.15$ m, $f = 1800$ Hz

Directivity

Directivity of the circular piston radiator in the ∞ -wall:



$ka = 10$, e.g. $a = 0.15$ m, $f = 3600$ Hz

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factors that influence radiated power of a membrane?

radiated power

radiation of a membrane depends on:

- ▶ membrane velocity (usually piston-like movement is assumed)
- ▶ membrane area
- ▶ surrounding of the membrane
- ▶ medium
- ▶ frequency

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radiated power

radiation impedance Z_{Ro} :

$$Z_{Ro} = \frac{p}{v}$$

where

p : average sound pressure on the surface of the membrane

v : velocity of the membrane (normal component)

- ▶ describes loading of the membrane
- ▶ calculation with wave theoretical methods
- ▶ alternative definition (volume flow): $Z_R = \frac{p}{Q}$
- ▶ radiation impedance is complex quantity → active and reactive component

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radiated power W by moving membrane is

$$W = Q^2 \operatorname{Re}[Z_R]$$

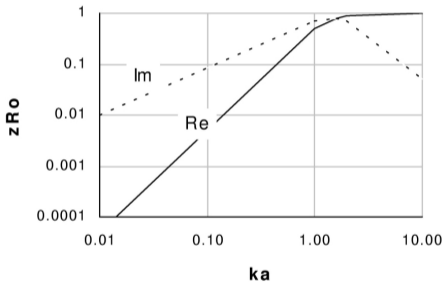
with

Q : volume flow (product of velocity and membrane area)

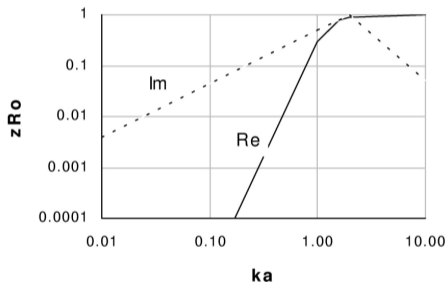
$\operatorname{Re}[Z_R]$: real (active) part of radiation impedance

radiated power

examples of radiation impedances (rel. to ρc):



piston in ∞ -wall



free piston

radiated power

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simulation of radiation impedances in equivalent electrical networks
(frequency range with f^2 dependency):

- ▶ often series arrangement of *frequency dependent* resistance (real part) and inductance (imaginary part)
- ▶ approximation of the load in networks: parallel arrangement
 - ▶ resistance $R = \rho c$ (dominates above $ka = 1$)
 - ▶ inductance $L = \rho a / \sqrt{2}$ (dominates below $ka = 1$)

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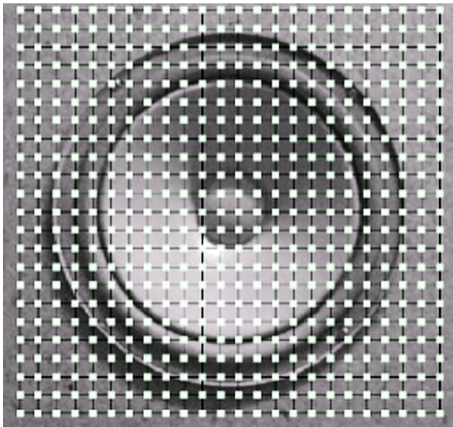
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velocity distribution of a membrane

velocity distribution of a membrane

- ▶ investigation of the membrane movement of a 20 cm woofer
- ▶ measurement method: Laser vibrometer (Doppler)



velocity distribution of a membrane

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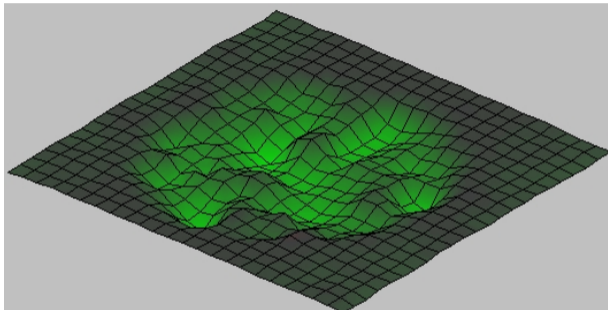
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frequency: 218 Hz

movie: frequency: 218 Hz

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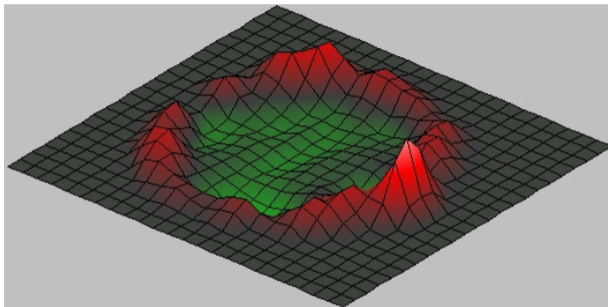
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frequency: 656 Hz

movie: frequency: 656 Hz

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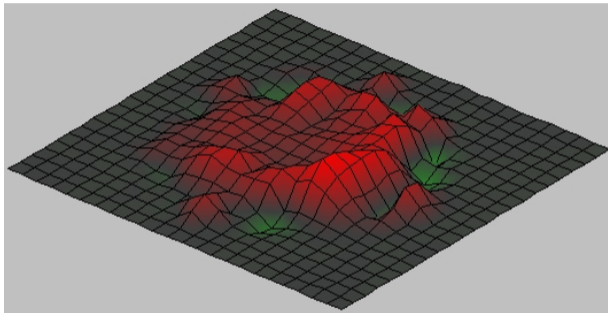
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frequency: 2000 Hz

movie: frequency: 2000 Hz

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electrodynamic loudspeaker: basic structure

basic structure

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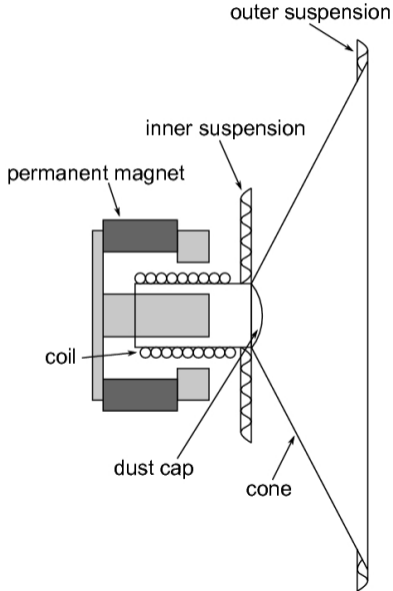
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Electrodynamic loudspeaker: equivalent network

equivalent network

elements to consider:

M_{AR}, R_{AR} acoustical mass and resistance of the air on the rear side of the membrane corresponding to real and imaginary part of the radiation impedance

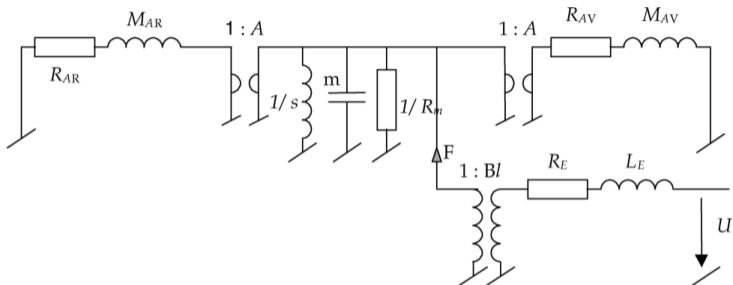
m, s mass of the membrane and the coil, stiffness of the membrane

R_m mechanical friction (suspension of the membrane)

M_{AV}, R_{AV} acoustical mass and resistance of the air on the front side of the membrane corresponding to real and imaginary part of the radiation impedance

R_E, L_E electrical resistance and inductance of the coil

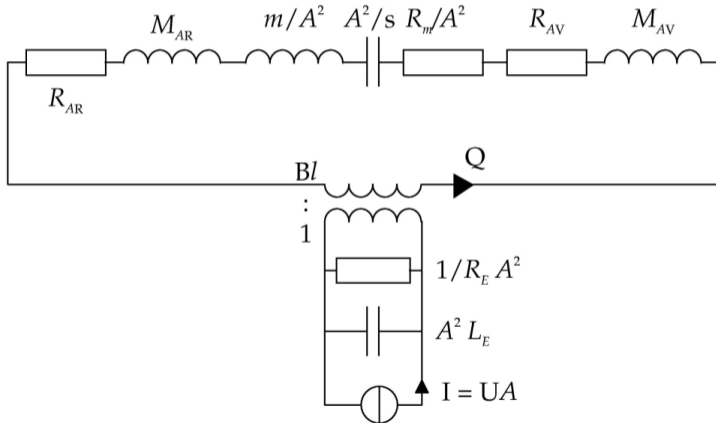
equivalent network



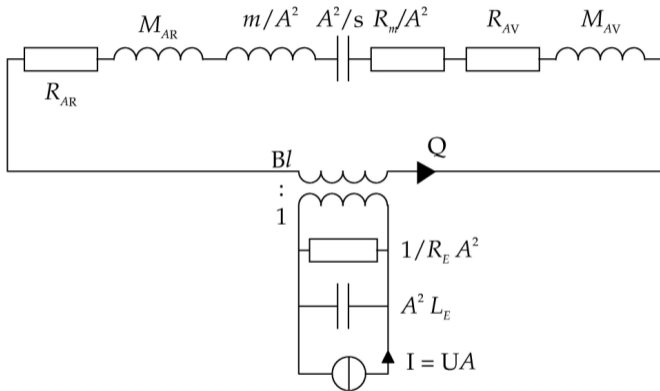
- ▶ $B \times \ell$: force factor
- ▶ electrical interface:
 - ▶ source current \rightarrow force F
 - ▶ membrane velocity \rightarrow induced voltage

equivalent network

elimination of the gyrators by dual conversion with $r = 1/A$, omission of the 1:1 transformers

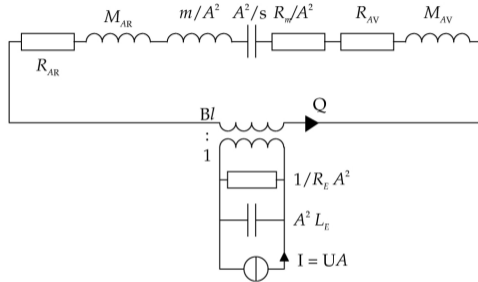


equivalent network



amplitude response of volume flow Q ?

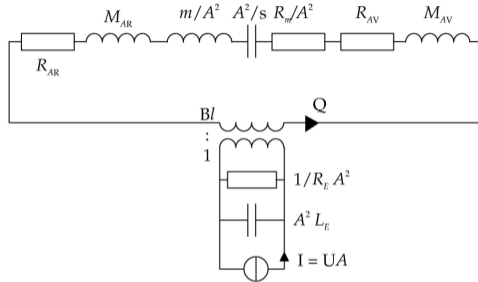
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amplitude response of volume flow Q :

- ▶ low frequencies: capacitor dominates $\rightarrow Q \sim \omega$
- ▶ resonance frequency: Q is limited by resistances
- ▶ high frequencies: inductances dominate $\rightarrow Q \sim 1/\omega$

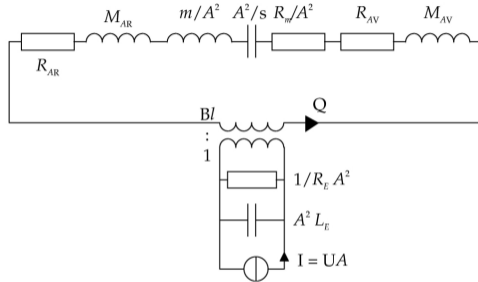
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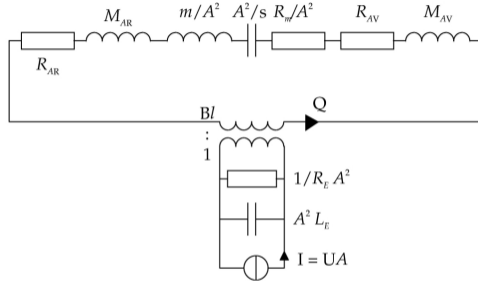
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- ▶ low frequencies: capacitor dominates $\rightarrow Q \sim \omega$
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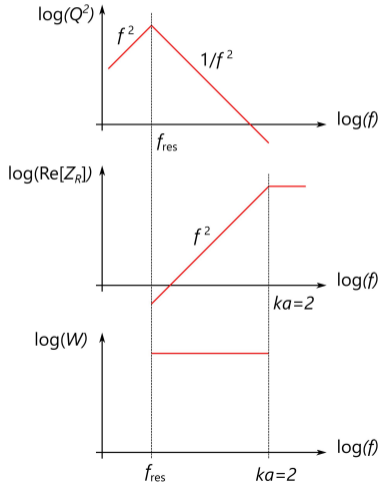


amplitude response of volume flow Q :

- ▶ low frequencies: capacitor dominates $\rightarrow Q \sim \omega$
- ▶ resonance frequency: Q is limited by resistances
- ▶ high frequencies: inductances dominate $\rightarrow Q \sim 1/\omega$

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- radiated sound power $W = Q^2 \cdot \text{Re}[Z_R]$



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- ▶ **W independent of frequency** for $Q \sim 1/\omega$ and $Re[Z_R] \sim \omega^2$
- ▶ \rightarrow operation above resonance
- ▶ \rightarrow piston mounted in ∞ -wall
- ▶ \rightarrow upper limiting frequency: $ka < 1$

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Electrodynamic loudspeaker: Nonlinearities

Nonlinearities

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- ▶ for large amplitudes, the element values will vary according to the membrane position
- ▶ → nonlinear behavior
- ▶ critical:
 - ▶ stiffness of the outer and inner suspension
 - ▶ inductance of the moving coil L_E
 - ▶ force factor $B \times \ell$

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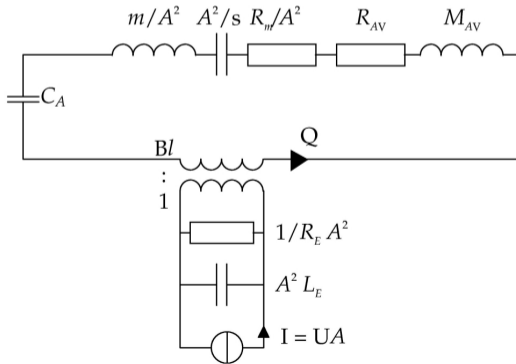
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electrodynamic loudspeaker: mounting in a cabinet

mounting in a cabinet

- ▶ chassis in ∞ -wall realized by mounting in a cabinet
- ▶ changes:
 - ▶ no radiation impedance on rear side
 - ▶ increased stiffness due to enclosed air in the cabinet \rightarrow acoustical compliance C_A



mounting in a cabinet

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consequences:

- ▶ total capacitance of series resonance circuit is lowered
- ▶ increased resonance frequency
- ▶ the smaller the volume, the higher the resonance frequency
- ▶ → design rule: cabinet volume not too small and:
 - ▶ filling with porous material → isothermal behaviour → effective volume increased by 15%

mounting in a cabinet

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- ▶ potential problems introduced by the cabinet (compared to the ∞ -wall):
 - ▶ mechanical vibrations of the cabinet enclosure → booming
 - ▶ diffraction at the edges
 - ▶ standing waves (resonances) in the cabinet

mounting in a cabinet

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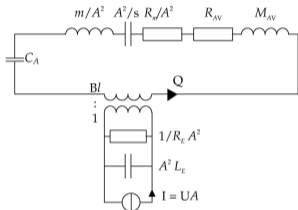
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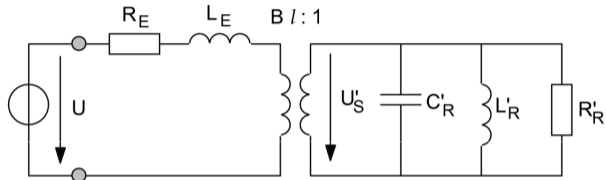
equivalent network so far:



further steps:

- ▶ combination of elements of the same type
- ▶ dual conversion of the complete network with $r = 1/A$
- ▶ ignore real part of the radiation impedance (o.k. for low frequencies)

mounting in a cabinet



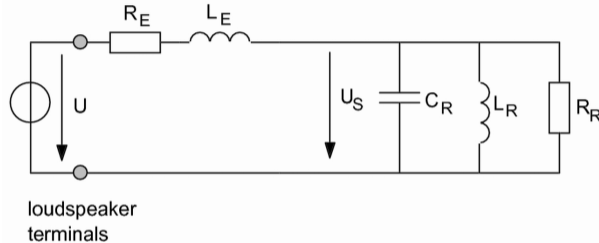
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terminals

quantity of interest: volume flow Q , appears as voltage U'_S :

$$U'_S = \frac{Q}{A}$$

mounting in a cabinet

elimination of transformer by impedance scaling with $(B \times \ell)^2$



quantity of interest: volume flow Q is transformed into voltage U_S :

$$U_S = (B \times \ell) U'_S = (B \times \ell) \frac{Q}{A}$$

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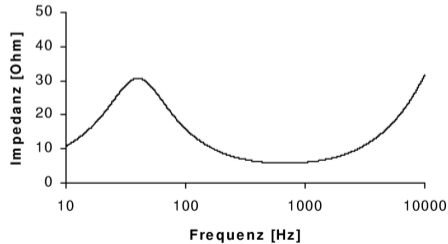
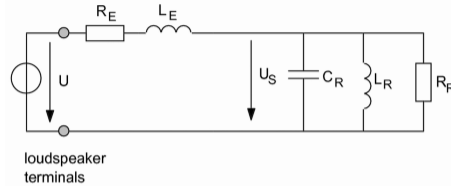
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electrodynamic loudspeaker: electrical impedance

electrical impedance



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electrodynamic loudspeaker: sound pressure frequency response

sound pressure frequency response

- ▶ restriction to low frequencies
 - ▶ → omnidirectional radiation

$$p(d) = \sqrt{\frac{W \rho_0 c}{4\pi d^2}} = \frac{Q \sqrt{\operatorname{Re}[Z_R] \rho_0 c}}{\sqrt{4\pi d}}$$

where

$p(d)$: sound pressure in distance d

W : radiated sound power

Q : volume flow of the membrane (velocity times area)

$\operatorname{Re}[Z_R]$: Real part of the radiation impedance

Sound pressure frequency response

radiation impedance (approximation for low frequencies, mounted in a cabinet):

$$\operatorname{Re}[Z_R] \approx \frac{\rho_0 c}{2} (ka)^2 \frac{1}{a^2 \pi} = \frac{\rho_0 \omega^2}{2\pi c}$$

with

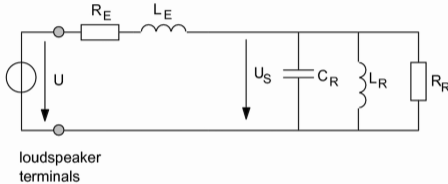
k : wave number

a : radius of the membrane

ω : angular frequency

Sound pressure frequency response

determination of Q from $U_S = (B \times \ell) \frac{Q}{A}$



neglecting L_E :

$$\frac{U_S}{U} \approx \frac{j\omega L_R R_R}{-\omega^2 L_R R_R C_R R_E + j\omega(L_R R_R + L_R R_E) + R_R R_E}$$

Sound pressure frequency response

$$\frac{p(d)}{U} \approx \frac{\rho_0 a^2}{d \sqrt{8Bl}} \frac{1}{j} \frac{1}{R_E C_R} \frac{-\omega^2 L_R C_R}{-\omega^2 L_R C_R + j\omega \frac{L_R R_R + L_R R_E}{R_R R_E} + 1}$$

frequency dependency \rightarrow high-pass function 2. order:

$$G(j\omega) = \frac{-\omega^2 T_c^2}{-\omega^2 T_c^2 + j\omega \frac{T_c}{Q_{TC}} + 1}$$

with

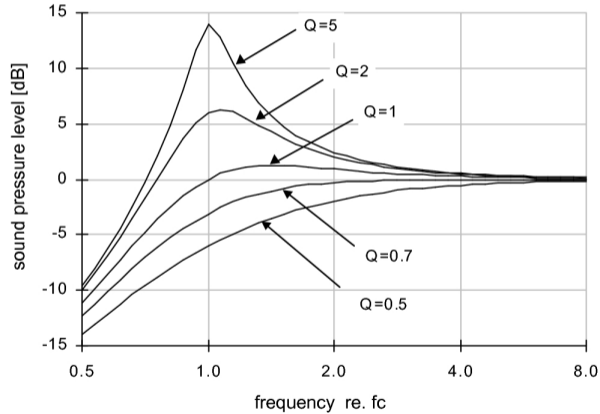
$$T_c = \frac{1}{\omega_c}$$

ω_c : lower limiting frequency of the high-pass filter

Q_{TC} : quality factor of the high-pass filter

Sound pressure frequency response

$p(d)/U$ for different values of quality factor Q_{TC} :



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electrodynamic loudspeaker: Thiele-Small parameters

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Thiele-Small parameters for the characterization of a free chassis:
resonance frequency f_s in Hz : lower end of frequency range of usage
compliance equivalent volume V_{AS} in l : stiffness of the membrane and suspension, expressed as equivalent air volume of equal stiffness

Thiele-Small-Parameters

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mechanical Q factor Q_{MS} : mechanical damping of the resonance (by R_R)

electrical Q factor Q_{ES} : electrical damping of the resonance (by R_E and possible output resistance of voltage source)

total Q factor Q_{TS} : $Q_{TS} = \frac{Q_{MS}Q_{ES}}{Q_{MS}+Q_{ES}}$

membrane area A in m^2

DC-resistance R_E in Ohm

force factor $B \times \ell$ in $T \times m$

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- ▶ can be determined from two electrical impedance measurements
 - ▶ case a): free chassis
 - ▶ case b): chassis mounted in a cabinet of small volume or alternatively loaded with additional mass put on the membrane

Thiele-Small-Parameters: mounted in a cabinet

free chassis specified by f_s , Q_{TS} , V_{AS}

behavior of chassis mounted in a cabinet of volume V_B :

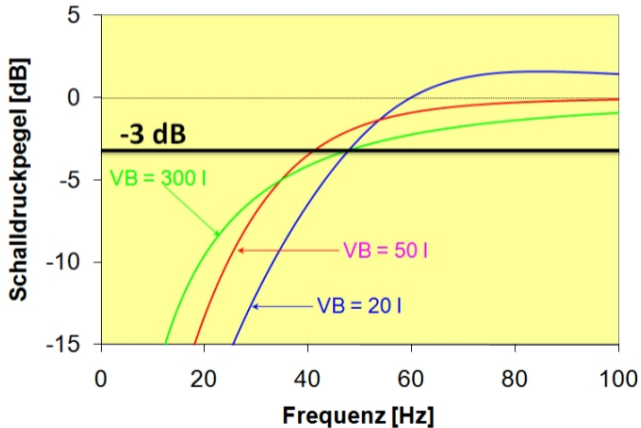
$$f_c = f_s \sqrt{\frac{V_{AS}}{V_B} + 1}$$

$$Q_{TC} = Q_{TS} \sqrt{\frac{V_{AS}}{V_B} + 1}$$

Thiele-Small-Parameters: chassis mounted in a cabinet

amplitude responses for different cabinet volumes:

Chassis: $f_s = 19$ Hz; $Q_{TS} = 0.32$; $V_{AS} = 200$ l



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Electrodynamic loudspeaker: velocity and displacement of the membrane

velocity and displacement of the membrane

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loudspeaker systems

- ▶ in the range of operation: membrane velocity $v \sim \frac{1}{f}$
- ▶ → membrane displacement: $x \sim \frac{1}{f^2}$
- ▶ → maximal excursion at lower end of frequency range of operation

velocity and displacement of the membrane

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velocity and displacement of the membrane

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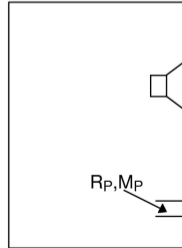
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electrodynamic loudspeaker: bass reflex cabinet

bass reflex cabinet

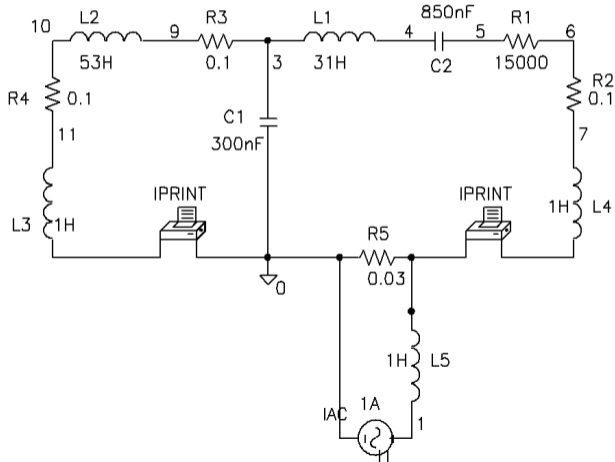
- ▶ extension of frequency range of operation to lower frequencies
- ▶ strategy: implementation of an additional resonance:
 - ▶ acoustical compliance: air volume in cabinet: C_A
 - ▶ acoustical mass: cylinder of air in tube: M_p
- ▶ near and at resonance: strongest oscillations of air column
- ▶ → relevant sound radiation



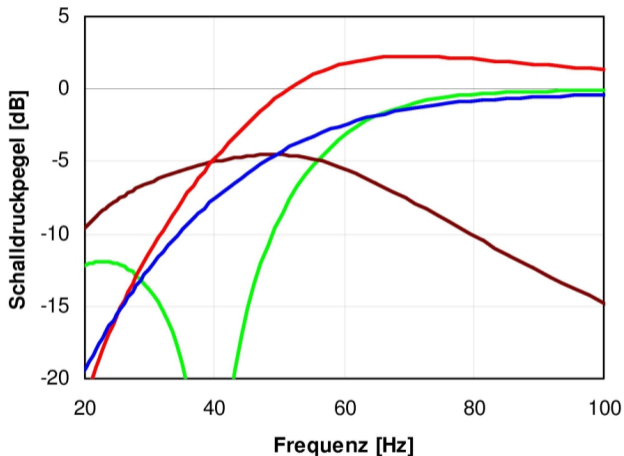
Bass reflex cabinet

Spice simulation:

chassis: $f_s = 31 \text{ Hz}$; $Q_{TS} = 0.3$; $V_{AS} = 118 \text{ l}$

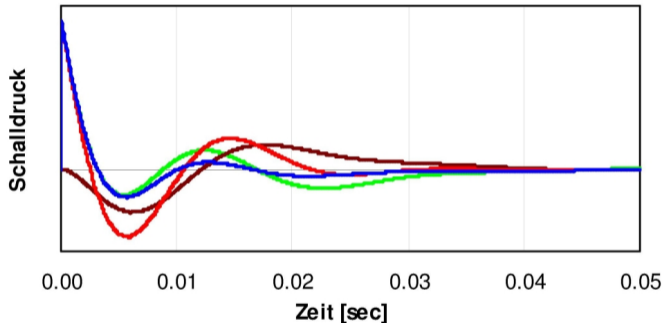


Bass reflex cabinet



— Membrane — Öffnung — Total Bassreflex — Total geschlossen

Bass reflex cabinet



Membrane

Tot Bassreflex

Öffnung

Tot geschlossen

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Bass reflex cabinet

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possible problems:

- ▶ unsatisfying transient behavior
- ▶ possible air flow noise at end of tube
 - ▶ to overcome by *passive membrane* systems
 - ▶ realization of mass by mechanical means

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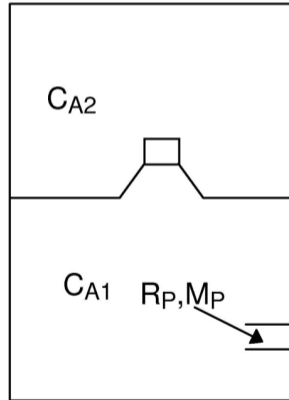
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Electrodynamic loudspeaker: Bandpass cabinet

Bandpass cabinet

- ▶ sub-woofer with acoustical low-pass filtering
- ▶ bandpass cabinet with chassis mounted in the interior of the cabinet



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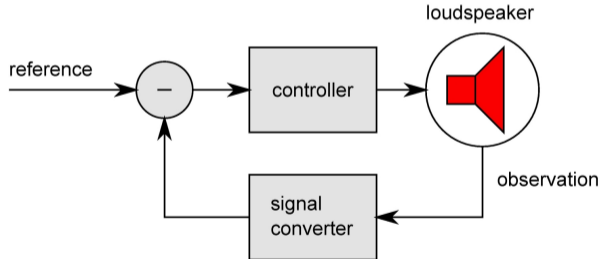
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electrodynamic loudspeaker: feed-back

feed-back

- ▶ aim of feed-back systems:
 - ▶ control of oscillation at resonance
 - ▶ reduction of non-linearities (large membrane excursions)



Feed-back

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- ▶ observation of membrane movement:
 - ▶ measurement of membrane velocity by additional moving coil
 - ▶ measurement of membrane position by capacitive sensor
 - ▶ measurement of membrane position by optical means

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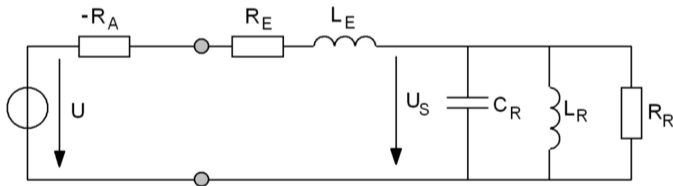
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Electrodynamic loudspeaker: Control of membrane velocity

Control of membrane velocity

- ▶ cancellation of driving coil DC resistance
 - ▶ powering by amplifier with negative output resistance
- ▶ → direct control of membrane velocity $U_S \approx U$



Control of membrane velocity

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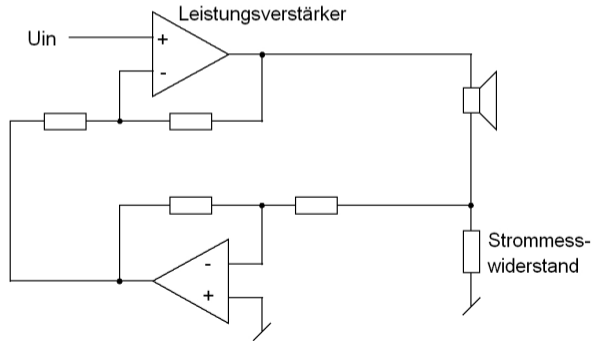
loudspeaker systems

- ▶ excellent transient behavior
- ▶ electrical $1/f$ -correction necessary to adjust for $Q \sim 1/f$
- ▶ control effect gets lost for high frequencies as L_E becomes important
- ▶ caution: $R_E - R_A > 0 \rightarrow$ stability condition!
- ▶ $|R_E| \approx |R_A|$ is difficult to achieve (compensation of temperature variation of R_E)

Control of membrane velocity

realization example: Studer A723

- ▶ negative output resistance:
 - ▶ increase of output current \rightarrow increase of output voltage



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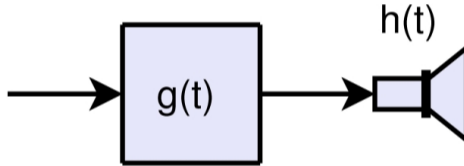
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Electrodynamic loudspeaker: Digital Equalizing

Digital Equalizing

Audio-
signal



▶ will this work?

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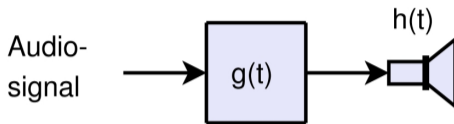
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Digital Equalizing



- ▶ impulse response of loudspeaker: $h(t)$
- ▶ inverse filter $g(t)$ where $g(t) * h(t) = \delta(t)$
- ▶ pre-filtering of audio signal with $g(t)$
- ▶ but:
 - ▶ physical limitations ($1/0 \rightarrow \infty$)
 - ▶ $h(t)$ depends on radiation angle
 - ▶ $h(t)$ depends on membrane excursion (nonlinearities)

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horn loudspeaker

- ▶ improved impedance matching (membrane movement \rightarrow air)
- ▶ significantly higher efficiency
- ▶ more pronounced directivity



horn loudspeaker

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common horn shape: exponential function:

$$S(x) = S_T \cdot e^{mx}$$

where

$S(x)$: cross sectional area at x

S_T : cross sectional area at throat ($x = 0$)

m : geometrical constant

horn loudspeaker

wave equation for the exponential horn:

$$\frac{\partial^2 p}{\partial t^2} - c^2 m \frac{\partial p}{\partial x} - c^2 \frac{\partial^2 p}{\partial x^2} = 0$$

guess for $\underline{p}(t)$:

$$\underline{p}(t) = \hat{p} e^{ax} e^{j\omega t}$$

with coefficient a :

$$a = - \left(\frac{m}{2} + j \frac{\sqrt{4(\omega/c)^2 - m^2}}{2} \right)$$

horn loudspeaker

determination of sound particle velocity:

→ relation between p and v :

$$\frac{\partial p}{\partial x} = -\rho \frac{\partial v_x}{\partial t}$$

in complex writing:

$$\underline{v} = -\frac{1}{j\omega\rho} \frac{\partial \underline{p}}{\partial x}$$

with \underline{p} inserted:

$$\underline{v} = \frac{1}{j\omega\rho} \left(\frac{m}{2} + j \frac{\sqrt{4(\omega/c)^2 - m^2}}{2} \right) \underline{p}$$

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radiation impedance:

$$\underline{Z}_{Ro} = \frac{p}{\underline{v}} = \frac{2j\omega\rho}{m + j\sqrt{4(\omega/c)^2 - m^2}}$$

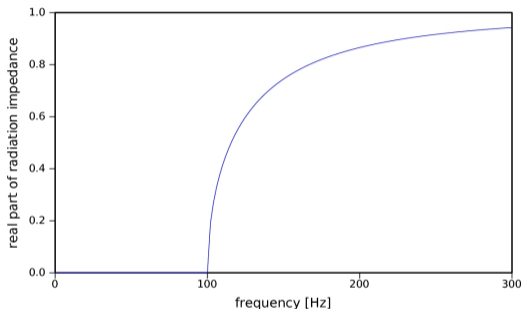
discussion of \underline{Z}_{Ro} :

$$2(\omega/c) < m \quad \operatorname{Re}[\underline{Z}_{Ro}] = 0$$

$$2(\omega/c) \geq m \quad \operatorname{Re}[\underline{Z}_{Ro}] = \rho c \sqrt{1 - \frac{m^2}{4(\omega/c)^2}}$$

horn loudspeaker

exemplary radiation impedance for $m = 3.7$:



- ▶ frequency range of operation: constant impedance
- ▶ → volume flow $Q \approx \text{constant}$ (→ at resonance with strong damping)
- ▶ caution: non-linear distortions due to high flow amplitudes in the throat

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▶ consequences of finite horn length?

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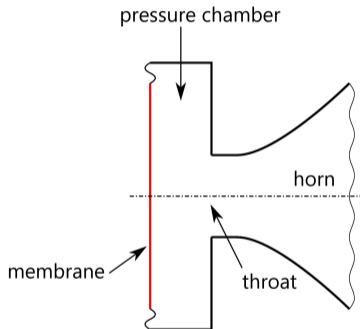
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- ▶ practical design rules (reflections at the end can be ignored) if:
 - ▶ length of the horn $> 3\lambda$ and
 - ▶ circumference at the end $> \lambda$

horn loudspeaker

compression driver (principle):

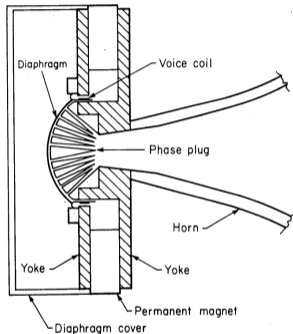


▶ acoustical transformer:

▶ low velocity of large membrane → high velocity in narrow throat

horn loudspeaker

compression driver (practical design):



- ▶ phase plugs:
 - ▶ suppression of cavity resonances
 - ▶ to obtain in-phase superposition of velocities in throat cross section

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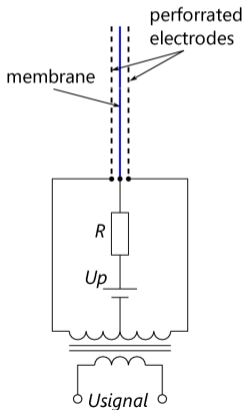
magnetostatic
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electrostatic loudspeaker

electrostatic loudspeaker

- ▶ push-pull principle → sandwich structure:
 - ▶ two perforated stationary electrodes (acoustically transparent)
 - ▶ lightweight stretched membrane in between (0.2 g/dm^2)



electrostatic loudspeaker

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- ▶ bias voltage U_p needed (linearisation of $F \sim U^2$)
- ▶ excellent transient behavior (lightweight and homogeneously driven membrane)
- ▶ only small excursions possible \rightarrow large membrane areas needed
- ▶ weak at bass frequencies
- ▶ increasing directivity at high frequencies (large membrane area)
- ▶ room surfaces behind the speaker cause reflections

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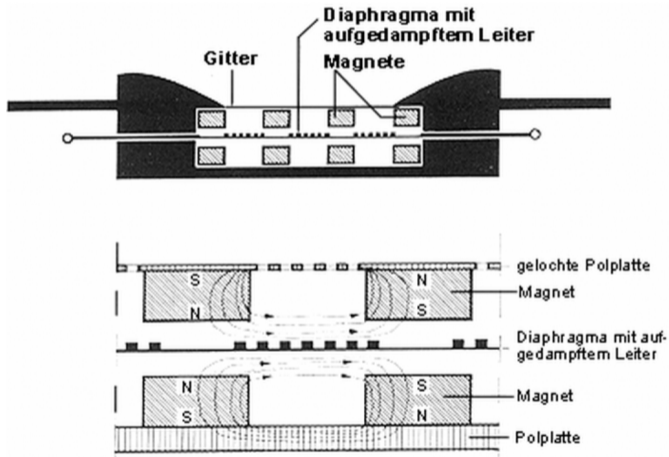
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loudspeaker systems

- ▶ radiation of the full audio frequency range (20 Hz ... 20 kHz) with one chassis is problematic as
 - ▶ radiation at low frequencies requires large membrane excursion or large membrane areas → in conflict with upper limiting frequency ($kr = 2$)
 - ▶ Doppler distortions (frequency modulations of high frequency signal components by low frequencies)

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- ▶ solution:
 - ▶ subdivision of frequency range into several bands by frequency dividing network and radiation by different specialized chassis
 - ▶ typical number of bands: 2 or 3

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potential difficulties:

- ▶ destructive interferences in the transition region due to:
 - ▶ differences in phase response of the chassis
 - ▶ differences in propagation distance: chassis → listener

solutions:

- ▶ adjustment of phase response
- ▶ adjustment for equal propagation distance by geometrical means
- ▶ optimal: concentric dual chassis

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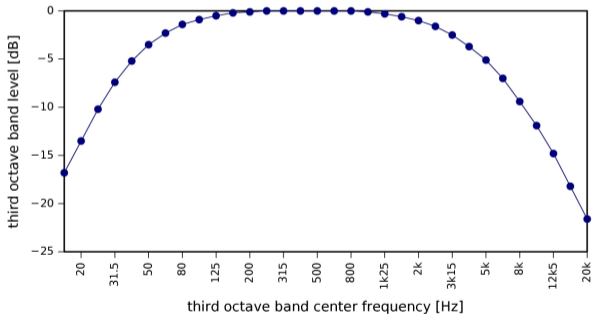
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power handling:

- ▶ limited by:
 - ▶ max. membrane excursion → specified by peak power
 - ▶ power dissipation (heating) → specified by average power

loudspeaker systems

continuous power testing with standard third-octave spectrum according to IEC 268:



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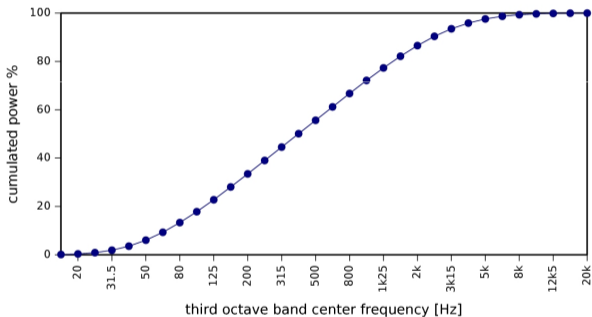
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cumulated power for the spectrum according to IEC 268:



caution: maximum power handling of a chassis is usually specified as power of the whole system!

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loudspeaker systems

- ▶ frequency response of the electrical impedance at the terminals
- ▶ frequency response of sound pressure on axis
- ▶ impulse response of sound pressure on axis
- ▶ cumulative decay spectrum of sound pressure on axis
- ▶ directivity of sound pressure for various discrete frequencies

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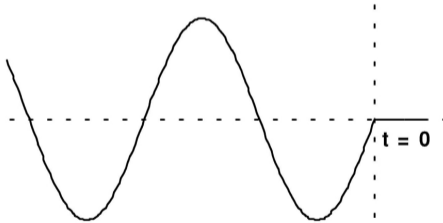
magnetostatic loudspeaker

loudspeaker systems

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- ▶ cumulative decay spectrum of sound pressure on axis
- ▶ directivity of sound pressure for various discrete frequencies

cumulative decay spectrum of sound pressure

- ▶ description of the transient behavior as a function of frequency
- ▶ experiment: excitation with tone burst signal



cumulative decay spectrum

- ▶ post-oscillation of the membrane produces sound pressure signal $s_\omega(t)$

$$s_\omega(t) = H_\omega(t) \sin(\omega t)$$

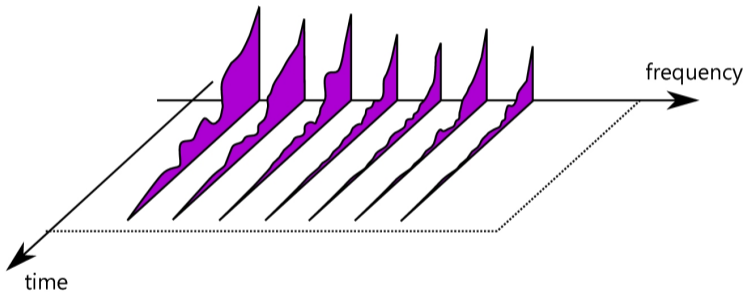
with

$H_\omega(t)$: modulation of amplitude

ω : angular frequency of the excitation signal

→ waterfall diagram of $H_\omega(t)$

cumulative decay spectrum



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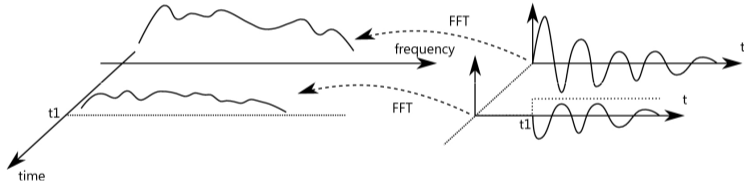
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cumulative decay spectrum

efficient generation by calculating FFT of time-windowed impulse response:



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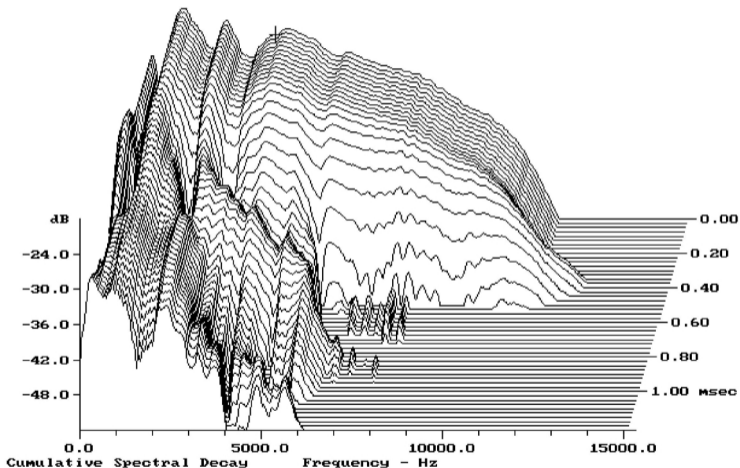
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example of a measurement of a mid-range speaker:



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NXT - distributed mode - loudspeaker

Distributed mode - loudspeaker

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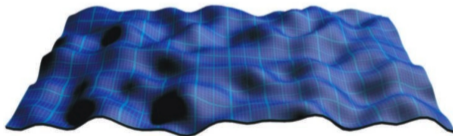
loudspeaker systems

history:

- ▶ 1991 first patent by Ken Heron of Britain's Defence Evaluation and Research Agency (DERA)
- ▶ British company NXT got a licence on the principle of operation
 - ▶ further investigation of the concept and development of the corresponding technology

Distributed mode - loudspeaker: principle

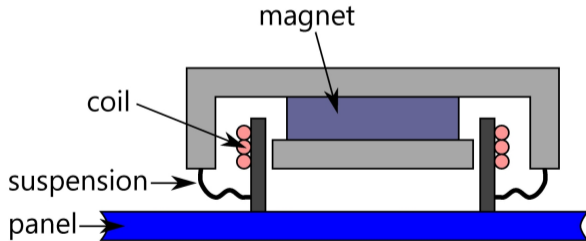
- ▶ NXT speakers consist of large panels
- ▶ drivers excite a great many of partial oscillations (bending waves) → panel oscillates with 'arbitrary' local velocity distribution
- ▶ oscillation pattern leads to incoherent (energetic) superposition at a receiver → omnidirectional radiation characteristics (figure-of-eight in case of mounting in free space)



Distributed mode - loudspeaker

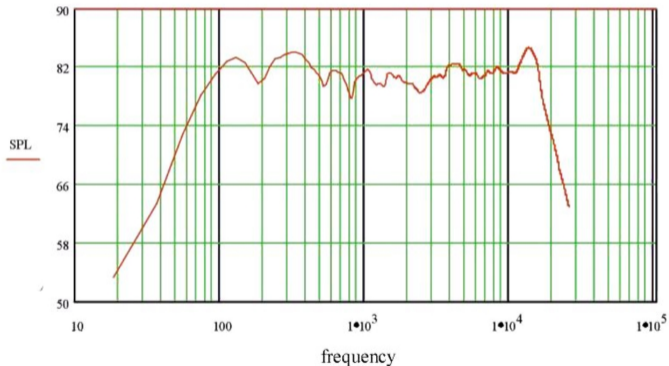
construction:

- ▶ large panels e.g. 60x60 cm
- ▶ excitation by one or several drivers



Distributed mode - loudspeaker

typical amplitude response:



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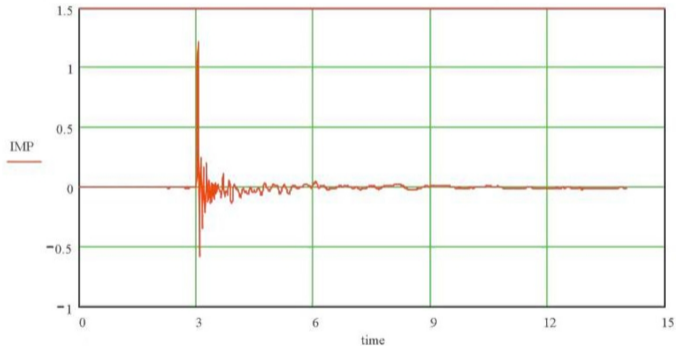
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Distributed mode - loudspeaker

typical impulse response [ms units]:



Distributed mode - loudspeaker

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applications:

- ▶ invisible P.A. systems (e.g. speaker arrays mounted in a ceiling)
- ▶ in case of special requirements (fire retardant, cleanable)
- ▶ optical-acoustical double-usage (e.g. surface for optical projection acts as speaker as well)

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Air motion transformer

Air motion transformer

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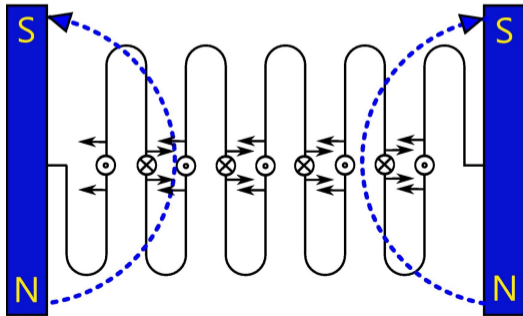
loudspeaker systems

history:

- ▶ Oskar Heil, USA

Air motion transformer: principle

- ▶ folded plastic foil between permanent magnets (large air gap \rightarrow strong magnets required)
- ▶ conductors along the folds (up and down)
- ▶ force across the membrane surface \rightarrow folds are opened and closed



air motion transformer

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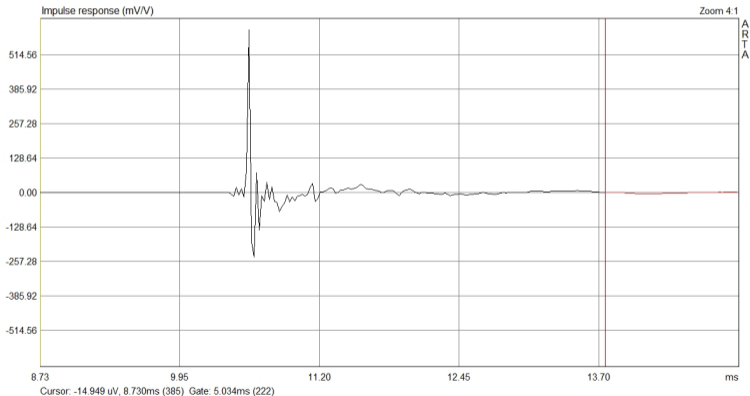
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advantages:

- ▶ small membrane movement → efficient volume variation → high volume flow
- ▶ typical transformation ratio: 1:5
- ▶ excellent transient behavior

air motion transformer

impulse response eton:



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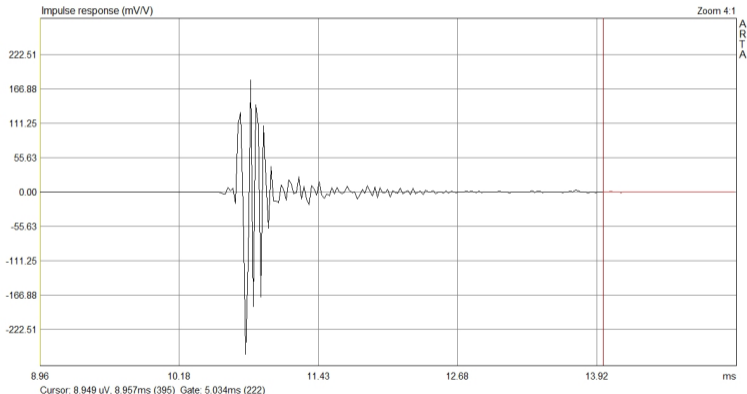
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