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ETH

Eidgenössische Technische Hochschule Zürich Swiss Federal Institute of Technology Zurich

Acoustics I: sound field calculations

Kurt Heutschi 2022-12-12

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- calculation of a situation specific location- and time dependent sound field (often p)
- conditions for a valid solution:
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 fulfillment of the boundary conditions:
 - Sources
- analytical solutions for special geometries only
- numerical solutions in the general case:
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Kirchhoff - Helmholtz integral

Green's theorem: Helmholtz equation \sim Kirchhoff - Helmholtz integral:

$$\dot{p}(x,y,z,\omega) = \frac{1}{4\pi} \int_{S} \left(j\omega \rho_0 \check{v}_S(\omega) \frac{e^{-j\omega r/c}}{r} + \check{p}_S(\omega) \frac{\partial}{\partial n} \frac{e^{-j\omega r/c}}{r} \right) \mathrm{d}S$$

- S: closed surface
- \check{v}_S : sound particle velocity on and normal to S
- \check{p}_S : sound pressure on S
- r: distance of the surface point to the receiver point (x, y, z)
 - \blacktriangleright Kirchhoff-Helmholtz integral \rightarrow wave field synthesis

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Kirchhoff - Helmholtz integral

- Kirchhoff-Helmholtz integral KHI is valid:
 - \blacktriangleright in the interior of S
 - \blacktriangleright in the exterior of S
 - on the surface S with a correction factor of 2

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Boundary Elements Method

typical radiation problem:



- surface velocity is given as boundary condition
- search for sound pressure field inside or outside of S
- solution with the Boundary Elements Method:
 - discretisation of the radiator surface in n elements
 - with KHI: $\check{p}_{S,i} = \sum_{j=1}^{n} f(\check{p}_{S,j},\check{v}_{S,j})$
 - ▶ solve the system of equations with *n* unknowns $\rightarrow \check{p}_{S,i}$
 - calculate sound pressure at any point in space with the KHI

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Rayleigh Integral

radiation of an oscillating piston → Kirchhoff-Helmholtz Integral
 special case: oscillating piston mounted in a large and rigid wall
 wall introduces boundary condition: v_n = 0



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Rayleigh Integral

- replace the effect of the wall by a mirror source
- \blacktriangleright oscillating piston \rightarrow pulsating piston



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Rayleigh Integral

evaluation of the Kirchhoff Helmholtz Integral:

$$\check{p}(x, y, z, \omega) = \frac{1}{4\pi} \int_{S} \left(j\omega \rho_0 \check{v}_S(\omega) \frac{e^{-j\omega r/c}}{r} + \check{p}_S(\omega) \frac{\partial}{\partial n} \frac{e^{-j\omega r/c}}{r} \right) \mathrm{d}S$$



contribution of sound pressure = 0!

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Rayleigh Integral

Kirchhoff Helmholtz Integral simplifies to the Rayleigh Integral:

$$\check{p}(x, y, z, \omega) = \frac{j\omega\rho_0}{2\pi} \int_{S} \check{v}_n(x, y, \omega) \frac{e^{-jkr}}{r} \mathrm{d}S$$

S: visible piston surface (front) v_n: piston velocity

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Kirchhoff's approximations: diffraction problems

- screen with aperture:
 - plane wave incident on aperture in a hard screen
 - sound pressure field behind the screen?



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Kirchhoff's approximations: diffraction problems

- solution: application of the Rayleigh Integral
 - needed: sound particle velocity in the apertureKirchhoff's approximation:
 - assume sound particle velocity as if no screen is present
 - \blacktriangleright \rightarrow ignore edge
 - error decreases with decreasing ratio wavelength / diameter

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Kirchhoff's approximations: diffraction problems

example: sound field of a plane wave behind an aperture of 25 cm diameter



sound field behind aperture with Kirchhoff's aproximation

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Kirchhoff's approximations: diffraction problems

Rayleigh Integral:

$$\check{p}(x, y, z, \omega) = \frac{j\omega\rho_0}{2\pi} \int_{S} \check{v}_n(x, y, \omega) \frac{e^{-jkr}}{r} \mathrm{d}S$$

- approximation with Fresnel zones for receivers not too close:
 - ignore small changes of r
 - differentiate phase in classes + (0 degrees) and (180 degrees) only
 - corresponding regions in the aperture: Fresnel zones

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Kirchhoff's approximations: diffraction problems

Fresnel zones in case of circular aperture:



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Kirchhoff's approximations: diffraction problems

$$p \sim \frac{A_1}{r_1} - \frac{A_2}{r_2} + \frac{A_3}{r_3} - \frac{A_4}{r_4} \dots$$

A_i: area of the *i*-th Fresnel zone r_i: average distance to the *i*-th Fresnel zone

for large apertures:

 $p\sim rac{A_1}{2r_1}$

if aperture = 1. Fresnel zone \rightarrow amplification of +6 dB re. free field

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Fresnel zones for reflection problems

- reflection at inhomogeneous or finite surfaces:
 - \blacktriangleright half of the 1. Fresnel zone defines the relevant region F on a reflector
 - concept allows for the estimation of situations with:
 - ▶ small reflectors $F < \frac{A_1}{2} \rightarrow p_{\text{refl}} \approx \frac{2F}{A_1} p_{\text{refl}\infty}$
 - inhomogeneous reflectors

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finite elements

- common method to numerically solve differential equations by discretization of the field volume
- well suited for:
 - bounded field regions such as vehicle interiors
 - coupled structure/fluid systems, e.g. simulation of airborne sound insulation in the laboratory
 - simulation of inhomogeneous properties of the medium (c, density)
- not well suited for:
 - radiation in unbounded space

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- discretization of the field volume in finite elements
- establish one equation per element and node
- assembly of the system of equations

finite elements

solve the system of equation for each frequency of interest



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FDTD: finite differences in the time domain

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Finite Differences in the Time Domain (FDTD)

standard method to find solutions of differential equations numerically

- usage of the fundamental acoustical partial differential equations in the time domain:
 - grad(p) = −ρ^{∂v}/∂t
 −^{∂p}/∂t = κP₀div(v)
- Newton
- Poisson, mass conservation

- strategy:
 - discretisation of simulation domain in space and time
 replacement of derivatives by differences (space and time)

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Finite Differences in the Time Domain (FDTD)

- standard method to find solutions of differential equations numerically
- usage of the fundamental acoustical partial differential equations in the time domain:

•
$$grad(p) = -\rho \frac{\partial \vec{v}}{\partial t}$$

• $-\frac{\partial p}{\partial t} = \kappa P_0 \operatorname{div}(\vec{v})$

Newton

Poisson, mass conservation

discretisation of simulation domain in space and time
 replacement of derivatives by differences (space and time)

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Finite Differences in the Time Domain (FDTD)

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- usage of the fundamental acoustical partial differential equations in the time domain:

•
$$grad(p) = -\rho \frac{\partial \vec{v}}{\partial t}$$

• $-\frac{\partial p}{\partial t} = \kappa P_0 \operatorname{div}(\vec{v})$

Newton

Poisson, mass conservation

- strategy:
 - discretisation of simulation domain in space and time
 replacement of derivatives by differences (space and time)
 - $\blacktriangleright \ \rightarrow$ updating equations in time

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finite differences in the time domain (FDTD) 2D-formulation:



$$\begin{array}{lll} \mathbf{v}_{\mathrm{x}}^{\mathrm{new}} & = & \mathbf{v}_{\mathrm{x}}^{\mathrm{old}} - \alpha \left(\mathbf{p}_{\mathrm{right}} - \mathbf{p}_{\mathrm{left}} \right) \\ \mathbf{p}^{\mathrm{new}} & = & \mathbf{p}^{\mathrm{old}} - \beta \left(\mathbf{v}_{\mathrm{xright}} - \mathbf{v}_{\mathrm{xleft}} \right) - \beta \left(\mathbf{v}_{\mathrm{ytop}} - \mathbf{v}_{\mathrm{ybottom}} \right) \end{array}$$

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finite differences in the time domain (FDTD)

- typical simulation / calculation:
 - impulse-like pressure distribution as starting condition
 - time-stepwise updating of the field variables at the grid points

advantages:

- no system of equation that has to be solved
- impulse response as a result contains information about all frequencies

disadvantage:

implementation of frequency domain boundary conditions is not straight forward

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finite differences in the time domain (FDTD)

computational effort:

- $\blacktriangleright\,$ 2D-simulation of a region of 200 m $\times\,$ 40 m
- $f_{max} = 2 \text{ kHz} \rightarrow \text{discretization in space: } 0.02 \text{ m}$
- mesh size $10'000 \times 2'000 = 20 \cdot 10^6$ grid points
- calculation time \rightarrow a few minutes

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mapping of 3-dimensional geometries onto 2 independent coordinates:

- translation invariant situation
- rotation invariant situation

2-/3-D simulations

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2-/3-D simulations

translation invariant situation

- cartesian coordinate system
- situation geometry does not change in y-direction
- all derivatives of the sound field equations with respect to y-direction are set to 0
- \blacktriangleright simulated source = coherent line source with extension in y-direction
- coherent incoherent line source??

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2-/3-D simulations

rotation invariant situation

- cylindrical coordinate system
- $\blacktriangleright\,$ situation geometry does not change with angle $\phi\,$
- \blacktriangleright all derivatives of the sound field equations with respect to $\phi\text{-direction}$ are set to 0
- simulated source = point source in the origin
- \blacktriangleright caution: reflections lead to focusing effects at the source position \rightarrow only strictly propagating waves allowed

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finite differences in the time domain (FDTD)

example: road traffic situation



road traffic noise situation

reflection at noise barrier

noise barrier



reflection at noise barrier

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example: Hardbrücke, effect of absorbing layer at the bottom of bridge



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reflecting bridge:



Hardbrücke - reflecting

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absorbing bridge:



Hardbrücke - absorbing

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finite differences in the time domain (FDTD) example: railway line cutting



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Kirchhoff-Helmholtz integral is valid for arbitrary surfaces

$$\check{p}(x, y, z, \omega) = \frac{1}{4\pi} \int_{S} \left(j\omega \rho_0 \check{v}_S(\omega) \frac{e^{-j\omega r/c}}{r} + \check{p}_S(\omega) \frac{\partial}{\partial n} \frac{e^{-j\omega r/c}}{r} \right) \mathrm{d}S$$

▶ for some specially designed surfaces, simplifications are possible

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for a plane S that closes in infinity



sound pressure in the right half space is given as:

$$\check{p}(x, y, z, \omega) = j \int_{S} \check{p}_{S}(\omega) \cos \phi \left(1 - \frac{j}{kr}\right) \frac{e^{-jkr}}{\lambda r} \mathrm{d}S$$

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- equation from above describes p̃ in 3D-space by a p̃ distribution on a 2D-plane
- \blacktriangleright \rightarrow principle of holography

acoustical holography

- how to capture a hologram in practice:
 - simultaneous determination of sound pressure distribution (amplitude and phase) at discrete grid points on a suitable plane
 - usage of microphone arrays
 - sequential sampling by using a fixed reference (phase)
 - \blacktriangleright \rightarrow complete information about the 3D field

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