

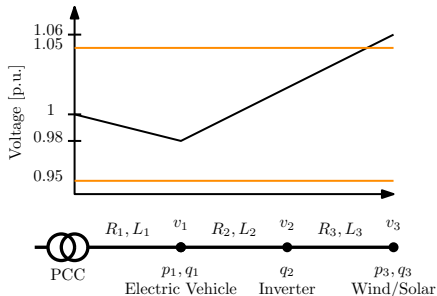


# Experimental Validation of Feedback Optimization in Power Distribution Grids

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# Congestion Leading to Overvoltage



## Volt/VAR Problem

$$\text{find } q_h \min_q \frac{1}{2} q^T M q$$

$$\text{subject to } v_{\min} \leq v_h(q, w) \leq v_{\max}$$

$$q_{\min, h} \leq q_h \leq q_{\max, h}$$

Example:

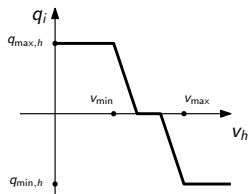
- Long distribution grid line
- Wind/Solar inject  $p_3$  leads to overvoltage
- Power consumption of EV  $p_1$  is higher than Wind/Solar production  $p_3$

# Local Feedback Control

## Local Strategies

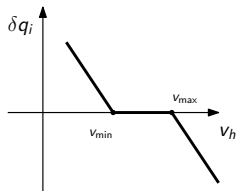
$$q_h(t+1) = g_h(q_h(t), v_h(t))$$

where  $g_h(q, v)$  only uses local information



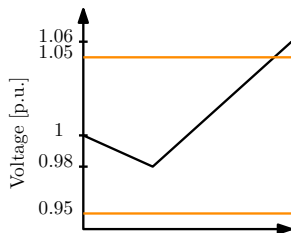
$$q_h(t+1) = f_h(v_h(t))$$

Droop control  
IEEE 1547



$$q_h(t+1) = q_h(t) + \delta q_h(v_h(t))$$

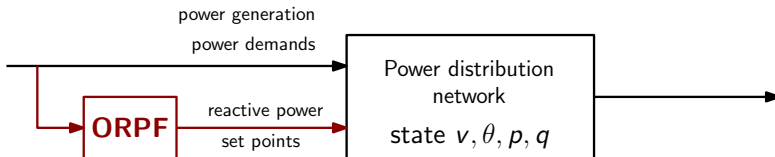
Integral control



## Local control strategies cannot solve this problem

Mathematically proven in "On the need for communication for voltage regulation of power distribution grids"

# A Feedforward Approach



## Optimal Reactive Power Flow (ORPF)

- Similar to power transmission grid ORPF
- Motivated by encouraging results on **ORPF convexification** Lavaei (2012), Farivar (2013), ...
- Requires **load knowledge - full communication**
- Heavily **model based**

# The Optimization Problem

$$\begin{aligned} \min_q \quad & \frac{1}{2} q^T M q \\ \text{subject to} \quad & v_{\min} \leq v_h(q, w) \leq v_{\max} \\ & q_{\min, h} \leq q_h \leq q_{\max, h} \end{aligned}$$

Without model for  $v_h(q, w)$  and knowledge of  $w$

**How to design a feedback controller that steers grid to the solution?**

**Lagrangian**  $\mathcal{L}(q, \lambda) = \frac{1}{2} q^T M q + \lambda_{\max}^T (v(q, w) - v_{\max}) + \lambda_{\min}^T (v_{\min} - v(q, w))$

## Optimization Algorithm

- **Dual update**  $\lambda(t+1) = [\lambda(t) + \alpha \frac{\partial \mathcal{L}}{\partial \lambda}]_{\geq 0}$
- **Primal update**  $q(t+1) = \arg \min_{q \in Q} \mathcal{L}(q, \lambda(t+1))$

# Feedback Optimization Control

**Lagrangian**  $\mathcal{L}(q, \lambda) = \frac{1}{2}q^T M q + \lambda_{\max}^T (v(q, w) - v_{\max}) + \lambda_{\min}^T (v_{\min} - v(q, w))$

**Dual update**

$$\lambda(t+1) = \left[ \lambda(t) + \alpha \frac{\partial \mathcal{L}}{\partial \lambda} \right]_{\geq 0}$$

$$\lambda_{\max}(t+1) = [\lambda_{\max}(t) + \alpha(v(q, w) - v_{\max})]_{\geq 0}$$

$$\lambda_{\min}(t+1) = [\lambda_{\min}(t) + \alpha(v_{\min} - v(q, w))]_{\geq 0}$$

( $\lambda$ -Update)

**Locally integrate the voltage violation**

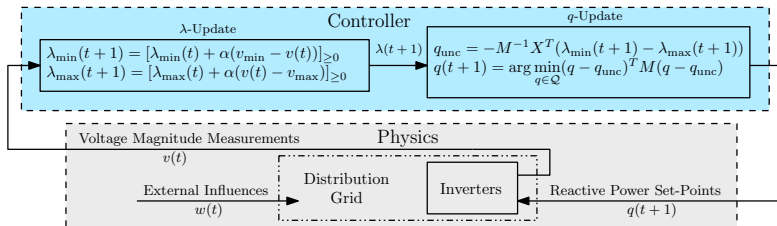
**Primal update**  $q(t+1) = \arg \min_{q \in Q} \mathcal{L}(q, \lambda(t+1))$

$$\frac{\partial \mathcal{L}}{\partial q} = 0 \Rightarrow Mq + \underbrace{\frac{\partial v}{\partial q}}_X (\lambda_{\max} - \lambda_{\min}) = 0 \Rightarrow q_{\text{unc}} = -M^{-1}X(\lambda_{\max} - \lambda_{\min})$$

$$q(t+1) = \arg \min_{q \in Q} \|q - q_{\text{unc}}\|_M$$

( $q$ -Update)

# Block Diagram



- Inverters take local voltage magnitude measurements
- Central control unit calculates set-points
- Set-points are send to the inverters

# Needed Model Information

## Linear Model Approximation

- The derivative  $\frac{\partial v(q,w)}{\partial q}$  can be approximated by a constant  $X$
- $X$  models the sensitivity of  $v$  with respect to  $q$
- Can be calculated using topology and cable data
- Similar to Power Transfer Distribution Factors

## Model-free Approximation

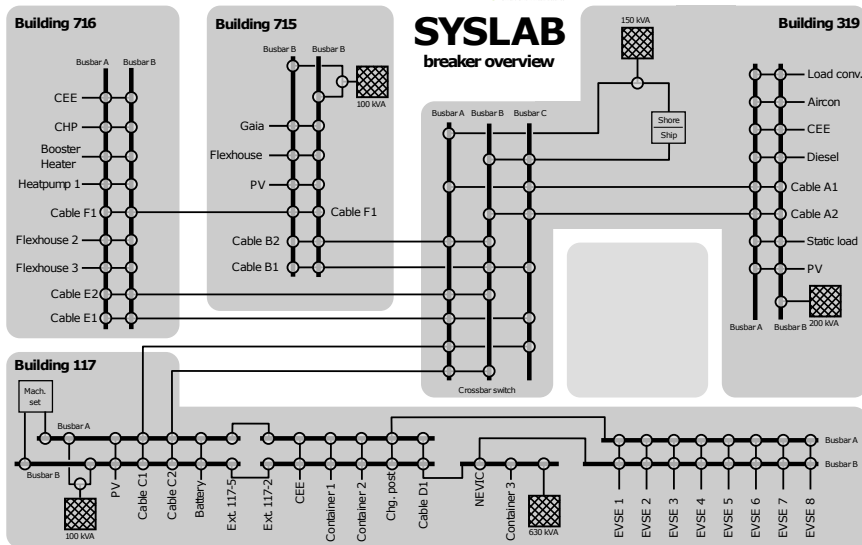
All entries of  $X$  are positive

$$\Rightarrow X = \begin{bmatrix} 1 & \dots & 1 \\ \vdots & \ddots & \vdots \\ 1 & \dots & 1 \end{bmatrix}$$

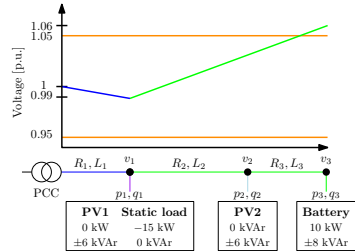
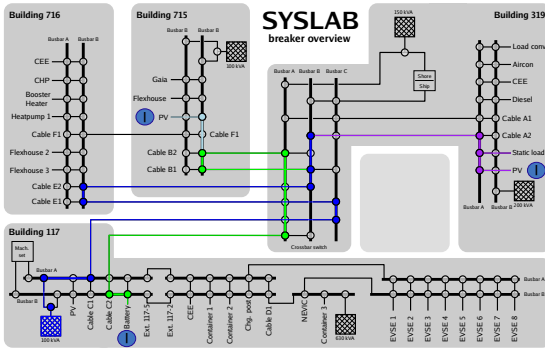


# Hardware Setup

## SYSLAB breaker overview



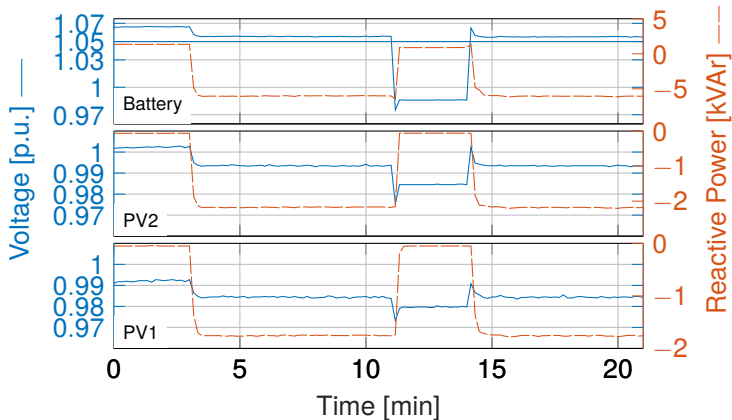
# Hardware Setup



## Active Power and Reactive Power Capabilities

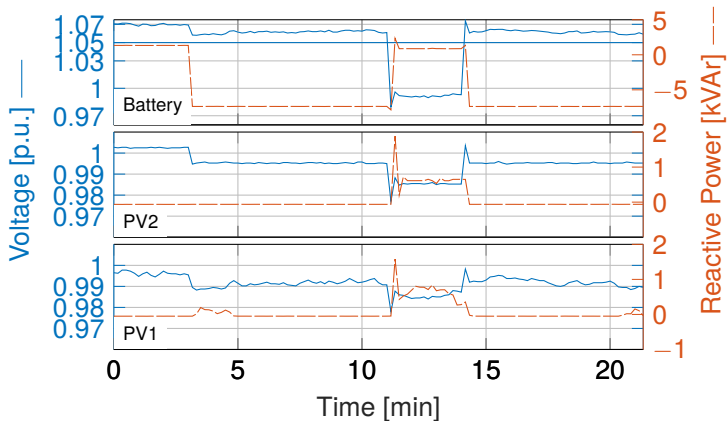
Battery:	$P=10$ kW	$Q=\pm 8$ kVAr
Static Load:	$P=15$ kW	$Q=0$ kVAr
PV Inverter:	$P=0$ kW	$Q=\pm 6$ kVAr

# Experimental Results - ORPF



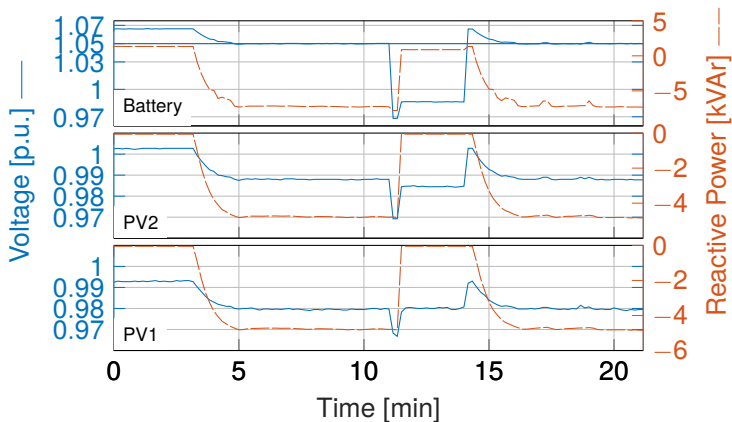
**Steady-state error with voltage violation**

# Experimental Results - Droop Control



**Reactive power of PVs not used  $\Rightarrow$  persistent overvoltage**

# Exp. Results - Feedback Optimization



**Convergence to the allowed voltage band**  
**This is the model-free version**

# Conclusions

## Take-Away Messages

- All local control strategies can make over/undervoltages worse
- Feedback Optimization can solve the problem
- Feedback Optimization has great potential for power grid applications
- Feedback Optimization is very robust

# People Involved



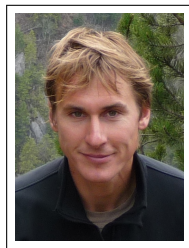
Lukas Ortmann



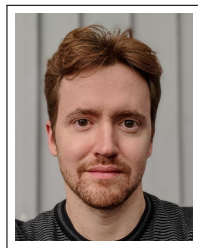
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