Control of Low-Inertia Power Systems: Naive & Foundational Approaches

INCITE Seminar @ Universitat Politècnica de Catalunya

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FONDS NATIONAL SUISSE
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SUIZZERO



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3/56





S. Curi



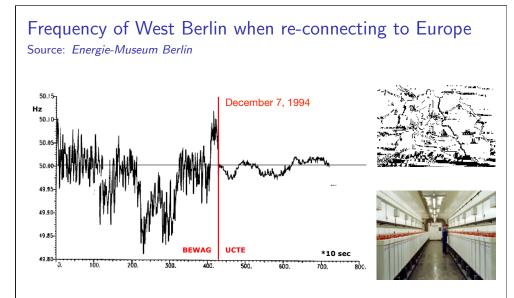
M. Colombino





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What do we see here?



before re-connection: islanded operation based on batteries & single boiler **afterwards** connected to European grid based on synchronous generation

Essentially, the pre/post West Berlin curves date back to...

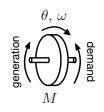


Fact: all of AC power systems built around synchronous machines!

At the heart of it is the generator swing equation:

$$M \frac{d}{dt} \omega(t) = P_{\text{generation}}(t) - P_{\text{demand}}(t)$$

change of kinetic energy = instantaneous power balance



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Operation centered around bulk synchronous generation Filips Frimary Control Primary Control Secondary Control Oscillation/Control 19.99 19.90

Renewable/distributed/non-rotational generation on the rise

synchronous generator



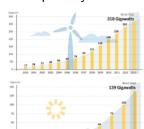
new workhorse



scaling



new primary sources



location & distributed implementation



focus today on **non-rotational** generation

The foundation of today's power system







Source: W. Sattinger, Swissgrid

Synchronous machines with rotational inertia

$$M\frac{d}{dt}\omega \approx P_{\text{generation}} - P_{\text{demand}}$$

Today's grid operation heavily relies on

- 1 robust stabilization of frequency and voltage by generator controls
- 2 self-synchronization of machines through the grid
- 3 kinetic energy $\frac{1}{2}M\omega^2$ as safeguard against disturbances

We are replacing this solid foundation with . . .

Tomorrow's clean and sustainable power system







Non-synchronous generation connected via power electronics

As of today, power electronic converters

- Iack robust control for voltage and frequency
- 4 do not inherently synchronize through the grid
- provide almost no energy storage

What could possibly go wrong?

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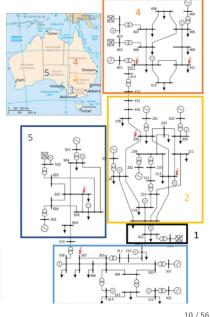
The concerns are not hypothetical: South Australia event



UPDATE REPORT –
BLACK SYSTEM EVENT
IN SOUTH AUSTRALIA ON
28 SEPTEMBER 2016

AN UPDATE TO THE PRELIMINARY OPERATING INCIDENT REPORT FOR THE NATIONAL ELECTRICITY MARKET. DATA ANALYSIS AS AT 5.00 PM TUESDAY 11 OCTOBER 2016

my conclusion from official report: blue low-inertia area 5 was not resilient; conventional system would have survived



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Black System Event in South Australia (Sep 2016)

The Sydney Morning Herald

NATIONAL

State in the dark: South Australia's major power outage

South Australia blackout: entire state left without power after storms

Key events¹

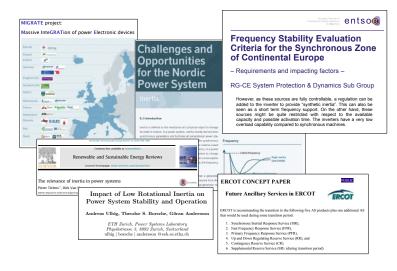
- intermittent voltage disturbances due to line faults
- 2 loss of synchronism between SA and remainder of the grid
- SA islanded: frequency collapse in a quarter of a second

"Nine of the 13 wind farms online did not ride through the six voltage disturbances experienced during the event."

¹AEMO: Update Report - Black System Event in South Australia on 28 September 2016

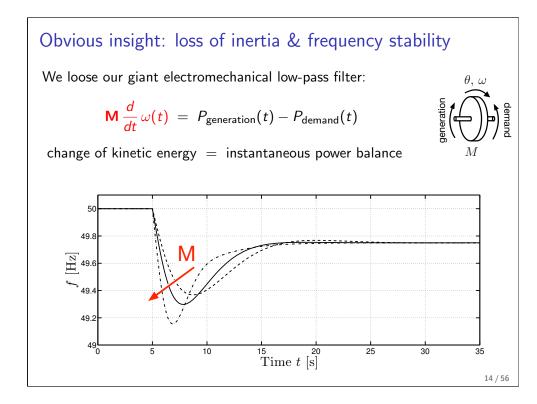
Low inertia issues have been broadly recognized

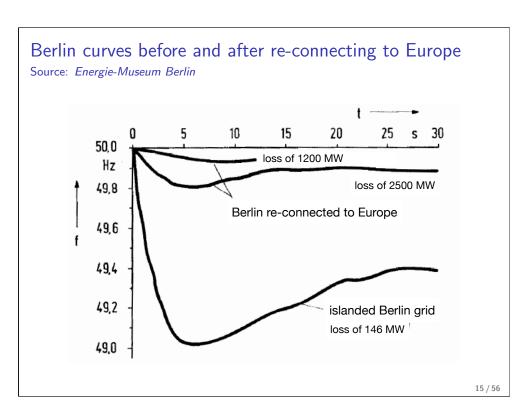
by TSOs, device manufacturers, academia, funding agencies, etc.



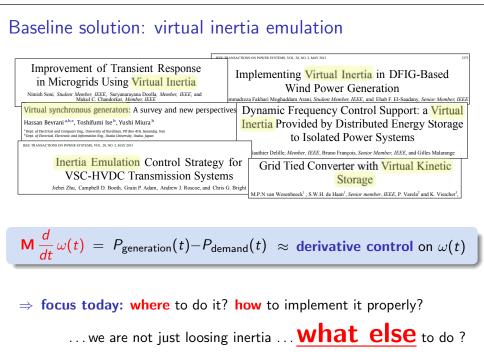
MIGRATE consortium: green-field approach to control of zero-inertia grids

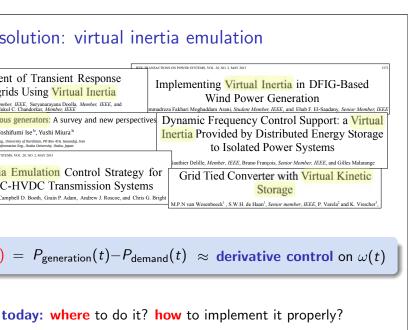
frequency violations in Nordic grid (source: ENTSO-E) same in Switzerland (source: Swissgrid) 0.00 -0.2-0.15-0.1-0.05 0 0.05 0.1 0.15 Frequency deviation [Hz] a day in Ireland (source: F. Emiliano) a year in France (source: RTE) 13/56





obvious insights lead to obvious (naive) answers





Outline

Introduction

System Level: Optimal Placement of Virtual Inertia network, disturbances, & performance metrics matter

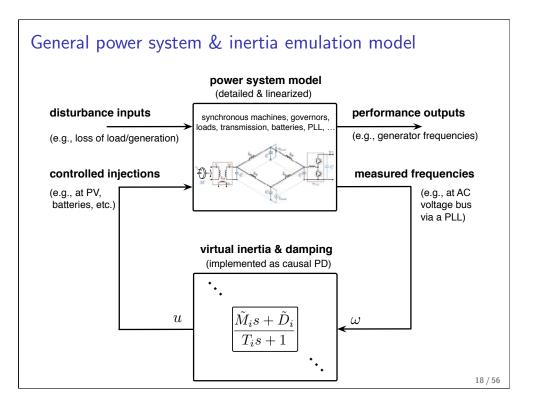
Device Level: Proper Virtual Inertia Emulation Strategy maybe we should not think about frequency and inertia

A Foundational Control Approach restart from scratch for low-inertia systems

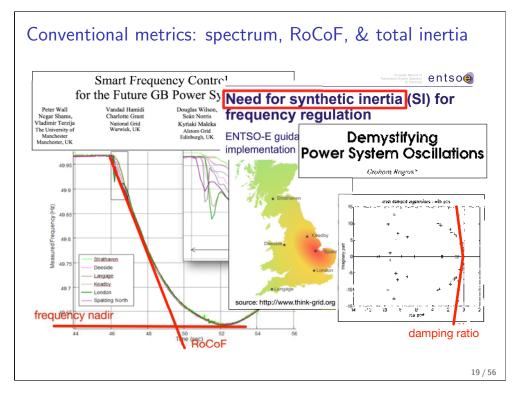
Conclusions



optimal placement of virtual inertia



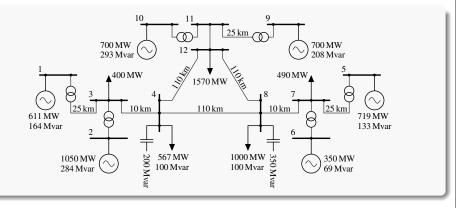
which metric(s) should our controller optimize?



are these suitable metrics?

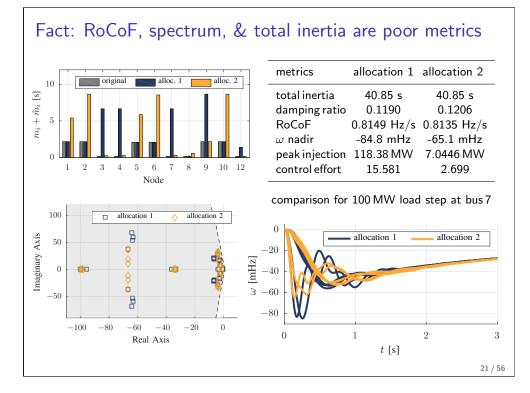
let's look at some simulations

Running example: modified Kundur three-area case study

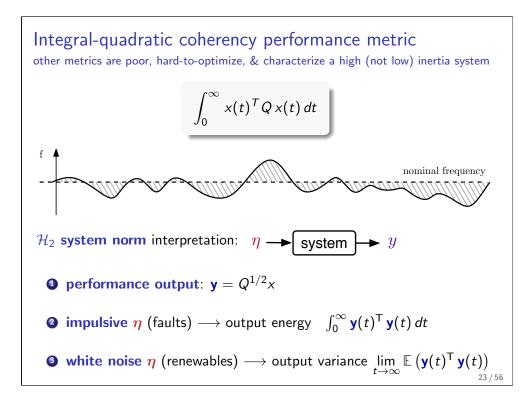


- added third area to standard case
- PLLs at all buses for inertia emulation (overall device response time ${\sim}100 \, \mathrm{ms})$
- transformer reactance 0.15 p.u, line impedance (0.0001+0.001i) p.u./km
- original inertia 40s: removed of rotational 28s which can be re-allocated as virtual inertia
- added governors & droop control at all generators

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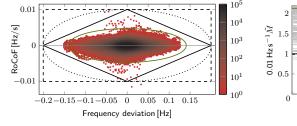


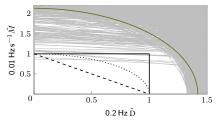
Re-visiting performance metrics for low-inertia systems restoration time nominal frequency secondary control energy unbalance frequency nadir ROCOF (max rate of change of frequency) **System norm** quantifying signal amplifications disturbances: impulse performance outputs: system (fault), step (loss of unit), integral, peak, ROCOF, white noise (renewables) restoration time, ... 22 / 56



Constraints on control inputs

- **1** energy constraint: $\int_0^\infty u^T R \, u \, dt$ directly captured in \mathcal{H}_2 framework
- **2** power constraint: $u_i = \tilde{M}_i \dot{\omega}_i + \tilde{D}_i \omega_i$ must satisfy $||u_i(t)||_{\ell_{\infty}} \leq \overline{u_i}$





European frequency data (source: RTE)

corresponding bounds on gains

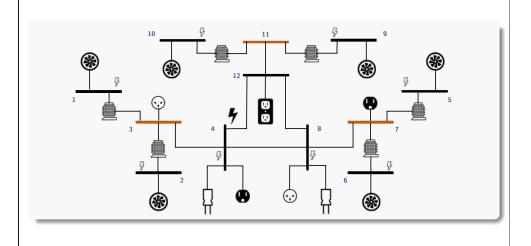
- $\Rightarrow \|(\omega_i(t),\dot{\omega}_i(t))\|_1, \|(\tilde{D}_i,\tilde{M}_i)\|_{\infty} \text{ bounded } \Rightarrow \|u_i(t)\|_{\ell_{\infty}} \text{ bounded}$
- **3 budget constraint** for finitely many devices: $\sum_{i} \overline{u_i} = const.$

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(sub)optimize performance and see what we learn

Modified Kundur case study: 3 areas & 12 buses

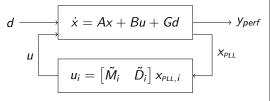
added governors (droop) at generators & PLLs to obtain frequency for inertia emulation



Test case

• inertia emulation control via PLL & batteries:

$$u_i = \begin{bmatrix} \tilde{M}_i & \tilde{D}_i \end{bmatrix} x_{\scriptscriptstyle PLL,i}$$



- dynamics: swing equation, droop via governor & turbine, and PLL
- \bullet state: $\textit{x} = \left[\text{ generator states , frequencies , governor control , PLL } \right]$
- cost penalizes frequencies, droop control, & inertia emulation effort:

$$\underbrace{\begin{bmatrix} \omega \\ u_{gov} \\ u \end{bmatrix}}_{Varif} = \underbrace{\begin{bmatrix} 0 & I & 0 & 0 \\ 0 & 0 & K_{gov} & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}}_{=O1/2} x + \underbrace{\begin{bmatrix} 0 \\ 0 \\ I \end{bmatrix}}_{=P1/2} u$$

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Algorithmic approach to desperate & non-convex problem

- structured state-feedback with constraints on gains
- $\dot{x} = Ax + Bu + Gd \longrightarrow y_{perf}$ $u = [\tilde{M}_i \quad \tilde{D}_i] x_{PLL,i}$
- **computation** \mathcal{H}_2 norm, gradient, & projections:
- observability and controllability Gramians via Lyapunov equations

$$(A - BK)^{T}P + P(A - BK) + Q + K^{T}RK = 0$$

 $(A - BK)L + L(A - BK)^{T} + GG^{T} = 0$

- **2** \mathcal{H}_2 norm $J = \text{Trace}(G^{\top}PG)$ and gradient $\nabla_K J = 2(RK B^{\top}P)L$
- **3** projection on structural & ∞ -norm constraint: $\Pi_{\tilde{M},\tilde{D}}[\nabla_K J]$
- \Rightarrow \tilde{M} and \tilde{D} can be optimized by first-order methods, IPM, SQP, etc.

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can we make this control design strategy useful?

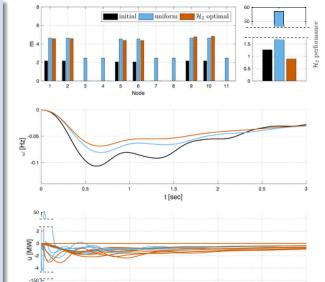
Results & insights for the three-area case study

Optimal allocation:

- location of inertia & damping matters
- outperforms heuristic uniform allocation
- need penalty on droop control effort
- power constraint results in $\tilde{D} \approx 2\tilde{M}$

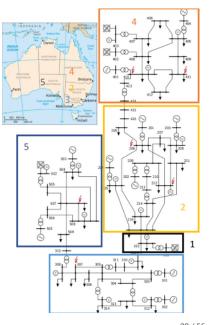
Fault at bus #4:

- strong reduction of frequency deviation
- much less control effort than heuristic

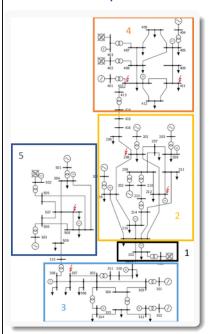








Control & optimization design scale up to large systems

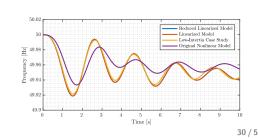


low-inertia Eastern-Australian grid:

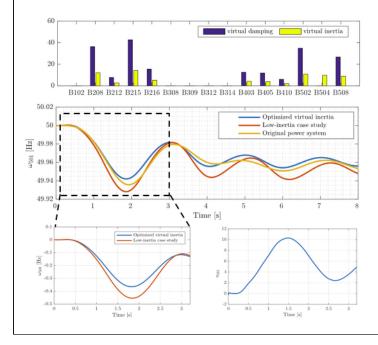
- removed rotational generation at buses 101, 402, 403 and 502
- added controllable power sources with PLLs at 15 buses

tractable model for design:

- linearization of nonlinear model
- balanced reduction to 140 states



\mathcal{H}_2 -optimal virtual inertia allocation with ℓ_{∞} constraints



allocation at core area 2 and critical areas 4 & 5

improves performance of low-inertia & original case

post-fault frequencies & control input well-behaved

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placement & metrics matter!

can we get analytic insights?

Inertia placement in swing equations

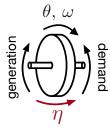
• simplified network swing equation model:

$$m_i \ddot{\theta}_i + d_i \dot{\theta}_i = p_{gen,i} - p_{dem,i}$$

generator swing equations

$$p_{dem,i} \approx \sum_{j} b_{ij} (\theta_i - \theta_j)$$

linearized DC power flow



- likelihood of disturbance at #i: $\eta_i \ge 0$ (available from TSO data)
- \mathcal{H}_2 performance **metric**: $\int_0^\infty \sum_{i,j} a_{ij} (\theta_i \theta_j)^2 + \sum_i s_i \dot{\theta}_i^2 dt$
- **decision variable** is inertia: $m_i \in [m_i, \overline{m_i}]$ (additional nonlinearity: enters as m_i^{-1} in constraints & objective) $_{
 m 32/56}$

Closed-form results for cost of primary control

recall: primary control $d_i \dot{\theta}_i$ effort was crucial

$$\int_0^\infty \dot{\theta}(t)^\mathsf{T} D \,\dot{\theta}(t) \,dt$$

(computations show that insights *roughly* generalize to other costs)

allocation: the primary control effort \mathcal{H}_2 optimization reads equivalently as

subject to
$$\sum_{i} m_{i} \leq m_{\text{bdg}}$$

$$\underline{m_i} \leq m_i \leq \overline{m_i}$$

key take-away is disturbance matching:

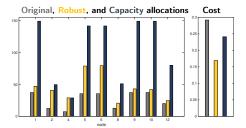
- optimal allocation $m_i^{\star} \propto \sqrt{\eta_i}$ or $m_i^{\star} = \min\{m_{\text{bdg}}, \overline{m_i}\}$
- ⇒ disturbance profile known from historic data, but rare events are crucial
- suggests robust $min_m max_n$ allocation to prepare for worst case
- \Rightarrow valley-filling solution: $\eta_i^{\star}/m_i^{\star} = const.$ (up to constraints)

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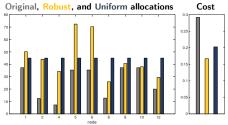
Robust min-max allocation for three-area case study

Scenario: fault (impulse) can occur at any single node

- $\qquad \text{disturbance set} \\ \eta \in \{ \mathbf{e}_1 \cup \dots \cup \mathbf{e}_{12} \}$
- ⇒ min/max over convex hull
- ► inertia capacity constraints
- robust inertia allocation outperforms heuristic max-capacity allocation
- results become intuitive: valley-filling property
- same for uniform allocation



allocation subject to capacity constraints



allocation subject to the budget constraint

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Outline

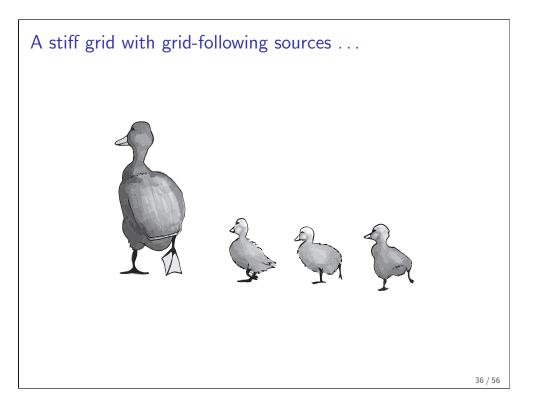
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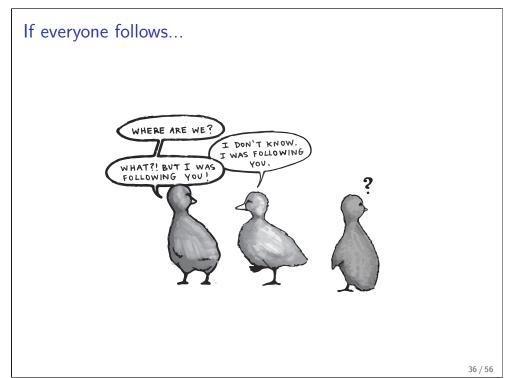
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A Foundational Control Approach restart from scratch for low-inertia systems

Conclusions





we are not just loosing inertia

interestingly, many so-called "virtual inertia" controllers are grid-following

design of robust grid-forming mechanisms

Modeling: signal space in three-phase AC power systems

three-phase AC

$$\begin{bmatrix} x_a(t) \\ x_b(t) \\ x_c(t) \end{bmatrix} = \begin{bmatrix} x_a(t+T) \\ x_b(t+T) \\ x_c(t+T) \end{bmatrix}$$

periodic with 0 average

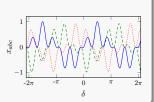
$$\frac{1}{T} \int_0^T x_i(t) dt = 0$$

balanced (nearly true)

$$=A(t)\begin{bmatrix}\sin(\delta(t))\\\sin(\delta(t)-\frac{2\pi}{3})\\\sin(\delta(t)+\frac{2\pi}{3})\end{bmatrix}=A\begin{bmatrix}\sin(\delta_0+\omega_0t)\\\sin(\delta_0+\omega_0t-\frac{2\pi}{3})\\\sin(\delta_0+\omega_0t+\frac{2\pi}{3})\end{bmatrix}$$

so that

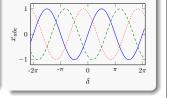
$$x_a(t)+x_b(t)+x_c(t)=0$$
 \Rightarrow const. in rot. frame



synchronous (desired)

$$=A\begin{bmatrix}\sin(\delta_0+\omega_0t)\\\sin(\delta_0+\omega_0t-\frac{2\pi}{3})\\\sin(\delta_0+\omega_0t+\frac{2\pi}{3})\end{bmatrix}$$

const. freq & amp

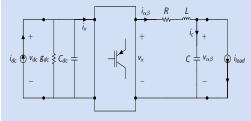


assumption: signals are balanced \Rightarrow 2d-coordinates $x(t) = [x_{\alpha}(t) \ x_{\beta}(t)]$

(equivalent representation: complex-valued polar/phasor coordinates)

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Averaged power converter model



DC cap & AC filter equations:

$$C_{dc}\dot{v}_{dc} = -G_{dc}v_{dc} + i_{dc} - \frac{1}{2}m^{\top}i_{\alpha\beta}$$

$$Li_{\alpha\beta}^{\cdot} = -Ri_{\alpha\beta} + \frac{1}{2}mv_{dc} - v_{\alpha\beta}$$

$$C\dot{v}_{\alpha\beta} = -i_{load} + i_{\alpha\beta}$$

modulation: $v_x = \frac{1}{2} m v_{dc}$, $i_x = \frac{1}{2} m^{\top} i_{\alpha\beta}$

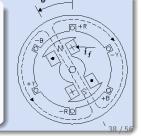
control/dist. inputs: (i_{dc}, i_{load})

synchronous generator: mechanical + stator flux + AC cap

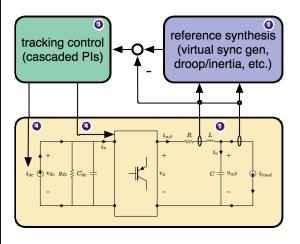
$$\theta = \omega$$

$$M\dot{\omega} = -D\omega + \tau_m + i_{\alpha\beta}^{\top} L_m i_f \begin{bmatrix} -\sin(\theta) \\ \cos(\theta) \end{bmatrix}$$

$$L_{s}\dot{i_{lphaeta}} = -Ri_{lphaeta} - v_{lphaeta} - \omega L_{m}i_{f} \begin{bmatrix} -\sin(heta) \\ \cos(heta) \end{bmatrix}$$
 $C\dot{v_{lphaeta}} = -i_{load} + i_{lphaeta}$



Standard power electronics control would continue by



- acquiring & processing of AC measurements
- 2 synthesis of references (voltage/current/power)
- **1** track error signals at converter terminals
- actuation via modulation (inner loop) and/or via DC source (outer loop)

I guess you can see the problems building up ...

Challenges in power converter implementations



Real Time Simulation of a Power System with VSG Hardware in the Loop

- delays in measurement acquisition, signal processing, & actuation
- 2 accuracy in AC measurements (averaging over multiple cycles)
- constraints on currents, voltages, power, etc.
- certificates on stability, robustness, & performance

Frequency Stability Evaluation Criteria for the Synchronous Zone of Continental Europe

- Requirements and impacting factors -

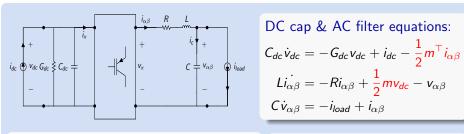
RG-CE System Protection & Dynamics Sub Group

added to the inverter to provide "synthetic inertia". This can also be seen as a short term frequency support. On the other hand, these sources might be quite restricted with respect to the available capacity and possible activation time. The inverters have a very low

let's do something smarter . . .

entso

See the similarities & the differences?



DC cap & AC filter equations:

$$C_{dc}\dot{v}_{dc} = -G_{dc}v_{dc} + i_{dc} - \frac{1}{2}m^{\top}i_{\alpha\beta}$$
 $Li_{\alpha\beta}^{\cdot} = -Ri_{\alpha\beta} + \frac{1}{2}mv_{dc} - v_{\alpha\beta}$
 $C\dot{v}_{\alpha\beta} = -i_{load} + i_{\alpha\beta}$

modulation:
$$v_{\rm x}=\frac{1}{2} m v_{dc}\,,\,i_{\rm x}=\frac{1}{2} m^{\top} i_{\alpha\beta}$$

passive:
$$(i_{dc}, i_{load}) \rightarrow (v_{dc}, v_{\alpha\beta})$$

synchronous generator:

mechanical + stator flux + AC cap

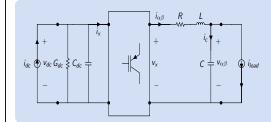
$$\theta = \omega
M\dot{\omega} = -D\omega + \tau_m + i_{\alpha\beta}^{\top} L_m i_f \begin{bmatrix} -\sin(\theta) \\ \cos(\theta) \end{bmatrix}$$

$$L_{s}i_{\alpha\beta} = -Ri_{\alpha\beta} - v_{\alpha\beta} - \omega L_{m}i_{f} \begin{bmatrix} -\sin(\theta) \\ \cos(\theta) \end{bmatrix}$$

$$C\dot{v}_{\alpha\beta} = -i_{load} + i_{\alpha\beta}$$



Model matching (\neq emulation) as inner control loop



DC cap & AC filter equations:

$$C_{dc}\dot{v}_{dc} = -G_{dc}v_{dc} + i_{dc} - \frac{1}{2}m^{\top}i_{\alpha\beta}$$

$$\dot{L}i_{\alpha\beta} = -Ri_{\alpha\beta} + \frac{1}{2}mv_{dc} - v_{\alpha\beta}$$

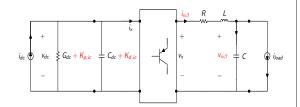
$$\dot{C}\dot{v}_{\alpha\beta} = -i_{load} + i_{\alpha\beta}$$

matching control:
$$\dot{\theta} = K_m \cdot v_{dc}$$
, $m = \hat{m} \cdot \begin{bmatrix} -\sin(\theta) \\ \cos(\theta) \end{bmatrix}$ with K_m , $\hat{m} > 0$

- \Rightarrow equivalent inertia $M=\frac{C_{dc}}{\kappa^2}$, imbalance signal $\omega=K_m\cdot v_{dc}$, etc.
- ⇒ pros: uses physical storage, uses DC measurements, & remains passive

Further properties of machine matching control

- base for outer loops
- $\Rightarrow i_{dc} = PD(v_{dc})$ gives virtual inertia & damping

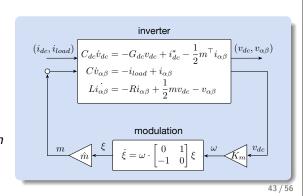


2 reformulation of

$$m = \hat{m} \cdot \begin{bmatrix} -\sin(\theta) \\ \cos(\theta) \end{bmatrix}$$

as adaptive **oscillator**:

$$\dot{m} = K_m \, v_{dc} \cdot \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} m$$



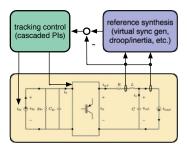
Summary: bottlenecks to inertia emulation

power system model on grid level:

$$M \frac{d}{dt} \omega = P_{\text{generation}} - P_{\text{demand}}$$



inertia emulation on device level:



- I/O mismatch: none of the converter inputs or outputs are present in the swing-equation, e.g., frequency is not a state in the converter
- inertia emulation à la PD problematic both in theory & practice
- \Rightarrow maybe matching control $\dot{m} = K_m v_{dc} \cdot \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} m$ was quite clever?

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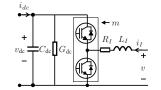
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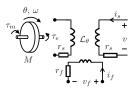
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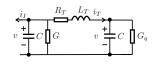
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Conclusions

Low-inertia power system model from first principles







- ▶ balanced three-phase system
 - (α, β) coordinates
- synchronous machines
 - first principle, 5th order
- ▶ DC/AC inverters
 - averaged-switched
- ▶ nonlinear loads $G(\|v\|)$

- voltage bus charge dynamics
- dynamic transmission lines: Π-model

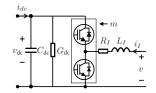
Port-Hamiltonian model

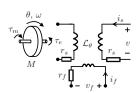
$$\dot{x} = \left(J(x, u) - R(x)\right) \nabla H(x) + g(x)u$$

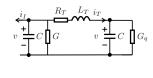
nonlinear & large, but insightful

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Desired steady-state locus & control specifications

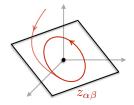






steady-state specifications for nonlinear system:

- synchronous frequency
- constant amplitude
- three-phase balanced



AC quantities v, i_s, i_l, i_T :

$$\dot{z}_{\alpha\beta} = \omega_0 \cdot \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} z_{\alpha\beta}$$

rotor angles: $\dot{\theta} = \omega_0$

DC quantities v_{dc}, v_f, ω : $\dot{z} = 0$

desired dynamics: $\dot{x} = f_{\text{des}}(x, \omega_0)$

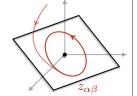
controls i_{dc}, m, τ_m, i_f to be found

, , ..., .

Proving the obvious (?)

• **steady-state locus**: physics & desired closed-loop vector field coincide (point-wise in time) on set

$$\mathcal{S} := \{(x, u, \omega_0) : f_{\mathsf{phys}}(x, u) = f_{\mathsf{des}}(x, \omega_0)\}$$



- **control-invariance**: steady-state operation $(x, u, \omega_0) \in \mathcal{S}$ for all time **if and only if**
 - **1 synchronous frequency** ω_0 is constant
 - 2 network satisfies power flow equations with impedances $R + \omega_0 JL$
 - **3** at each **generator**: constant torque τ_m & excitation i_f
 - **4** at each **inverter**: constant DC current i_{dc} & inverter duty cycle with constant amplitude & synchronous frequency: $\dot{m} = \omega_0 \cdot \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} m$
 - ⇒ internal models & feedforward input-to-steady-state map

Reduction to a tractable model for synthesis

• internal oscillator model for inverter duty cycle with inputs ω_m , \hat{m}

$$\dot{\theta}_I = \omega_m, \quad m = \hat{m} \begin{bmatrix} -\sin(\theta) \\ \cos(\theta) \end{bmatrix}$$

- model reduction steps
 - **1** rotating coordinate frame with synchronous frequency ω_0
 - \Rightarrow time scales of AC quantities scaled by $1/\omega_0$
 - **2** DC/AC time-scale separation via singular perturbation ($\epsilon \to 0$)

slow DC variables: $x_r = (\theta, \omega, i_f, \theta_I, v_{dc}),$ $\dot{x}_r = f_z(x_r, z_{\alpha,\beta}, u)$ fast AC variables: $z_{\alpha,\beta} = (i_s, i_I, v, i_T),$ $\epsilon \dot{z}_{\alpha,\beta} = f_{\alpha,\beta}(x_r, z_{\alpha,\beta}, u)$

 \odot reformulation via **relative angles** δ with respect to synchronous motion

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Insights from reduced model: $v_{dc} \propto$ power imbalance

• nonlinear reduced order model in rotating frame:

$$\begin{split} \dot{\theta} &= \omega \\ M\dot{\omega} &= -D\omega + \tau_m - \tau_e(x_r, u) \\ L_f \dot{i}_f &= -R_f i_f + v_f - v_{EMF}(x_r, u) \\ \dot{\theta}_I &= \omega_m \\ C_{dc} \dot{v}_{dc} &= -G_{dc} v_{dc} + i_{dc} - i_{sw}(x_r, u) \end{split}$$

- interconnection via τ_e , i_{sw} , v_{EMF}
- ullet analogies: suggest matching control: $\omega_m \sim v_{dc}$

generator	inverter	interpretation
$\frac{1}{2}M\omega^2$	$\frac{1}{2}C_{dc}v_{dc}^2$	energy stored in device
$^{-} au_{m}$	i_{dc}	energy supply
$ au_{e}$	i _{sw}	energy flow to grid
ω	V _{dc}	power imbalance

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Completing the control design

Thus far:

desired steady-state locus requires internal oscillator model

$$\dot{\theta}_I = \omega_m, \quad m = \hat{m} \begin{bmatrix} -\sin(\theta) \\ \cos(\theta) \end{bmatrix}$$

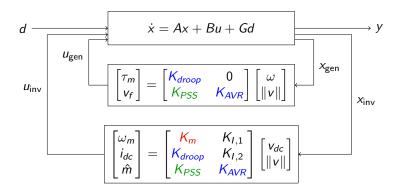
2 converter/generator analogies suggest model matching control

$$\omega_m = K_m \cdot (v_{dc} - v_{dc}^*)$$

Remaining steps:

9 performance requires design of structured & optimal MIMO control

Decentralized MIMO control architecture



- states $x = (\delta, \omega, i_f, v_{dc}, ||v||)$ & output $y = (\omega, v_{dc}, ||v||)$
- ullet included measurement devices for **AC voltage magnitude** $\|v\|$
- H2-optimal tuning of decentralized MIMO converter controller

Illustrative conceptual example test case: generator & inverter impedance load inverter control inactive inverter control active • 10% load increase at t=0ε [Hz] [Hz]-0.01Generator no inverter control: -0.02-0.02• ω_m and i_{dc} constant 10.5 • power imbalance: ω_G , v_{dc} $^{v_{DC}} [\mathrm{kV}]$ • governor stabilizes ω_G controlled inverter: t [sec]t [sec]• reduced peak in ω_G 1.2 [kA]

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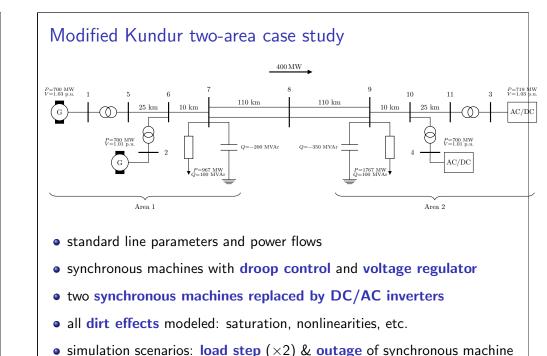
t [sec]

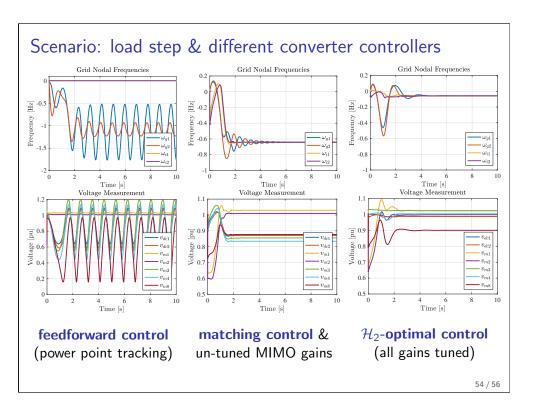
10 15 **52 / 56**

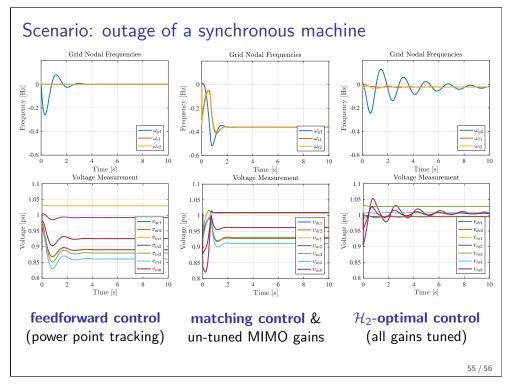
t [sec]

• v_{dc} stabilized via i_{dc}

• ω_m and ω_G synchronize







conclusions

Conclusions on virtual inertia emulation

Where to do it?

- \bullet \mathcal{H}_2 -optimal (non-convex) allocation
- 2 numerical approach via gradient computation
- 3 closed-form results for cost of primary control

How to do it?

- down-sides of naive inertia emulation
- 2 machine matching reveals power imbalance in DC voltage

What else to do?

- 1 first-principle low-inertia system model
- nonlinear steady-state control specifications
- g reduction to tractable model for synthesis
- f 4 first promising controller synthesis: internal model + matching + ${\cal H}_2$ performance loops



