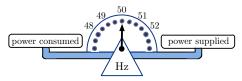


-ENTSO-E Press Release



### Modern challenges for control engineers

- Declining inertia and load-frequency responsiveness
  - Sensitive system
  - Large and frequent deviations
- e Heterogeneous small-scale power sources

Many small but fast sourcesFast freq. regulation markets

Opportunities for control engineers

- Inverter-based resources and fast communication
- Hierarchical control of many small devices

4/16

 $\Delta P^{\text{ref}} \xrightarrow{\Delta P_{u}} \Delta \omega$ System  $\Delta \omega$ System  $\Delta \omega$ System  $\Delta \omega$ System  $\Delta \omega$ Control inputs: Power set-points to devices  $\Delta P_{i}^{\text{ref}}$ Meas. / Controlled output: Frequency error  $\Delta \omega_{i}$ Unknown disturbances: Uncontrolled load/generation  $\Delta P_{u,i}$   $\Delta \dot{\theta}_{i} = \Delta \omega_{i},$   $M_{i} \Delta \dot{\omega}_{i} = -\sum_{j=1}^{n} T_{ij} (\Delta \theta_{i} - \Delta \theta_{j}) - D_{i} \Delta \omega_{i} + \Delta P_{m,i} + \Delta P_{u,i}$   $T_{i} \Delta \dot{P}_{m,i} = -\Delta P_{m,i} - R_{d-i}^{-1} \Delta \omega_{i} + \Delta P_{i}^{\text{ref}}.$ 

(Note: Real governor model may be highly nonlinear!)

Simple dynamic models for frequency control (single area)

5/16

#### Fundamental insights from output regulation theory Johnson, Davison, Francis, Wonham ...

System models are BIBO stable with steady-state given by

$$\Delta \omega = \underbrace{\beta^{-1} \mathbb{1} \mathbb{1}^{\mathsf{T}}}_{:=G_0 \text{ (DC Gain)}} (\Delta P_{\mathrm{u}} + \Delta P^{\mathrm{ref}}), \qquad \underbrace{\beta = \sum_i (D_i + R_{\mathrm{d},i}^{-1})}_{i}$$

Total proportional gain

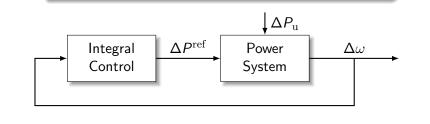
- **1** Insight #1:  $\Delta \omega \in \operatorname{span}(\mathbb{1}_n) \iff$  "frequency is global"
- **2** Insight #2: Only sum of powers matters  $\implies$  Resource allocation
- **Insight #3:**  $rank(G_0) = 1$ , which means ...

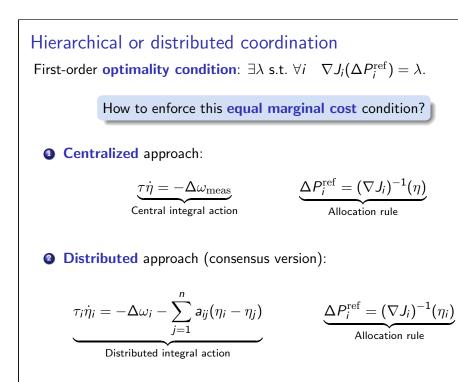
Only <u>one</u> frequency integrator permitted in <u>any</u> internally stable secondary control system!

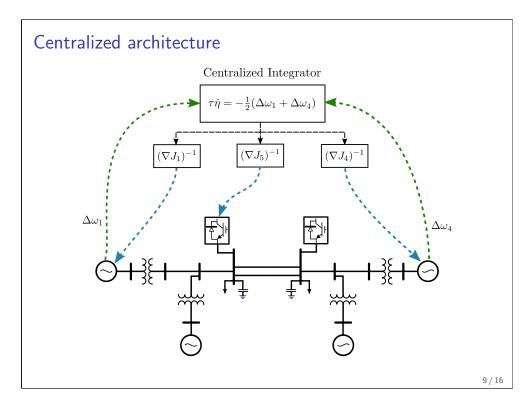
# Optimal allocation of secondary resources

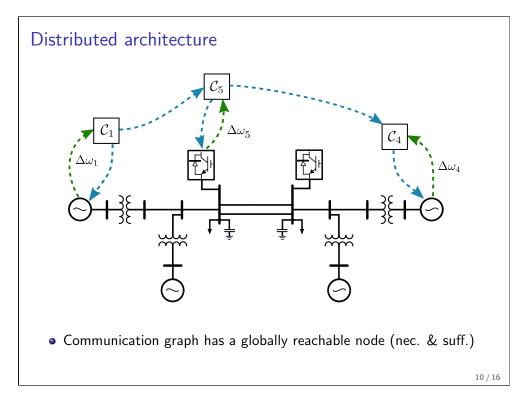
Optimally allocate inputs subject to power balance and limits

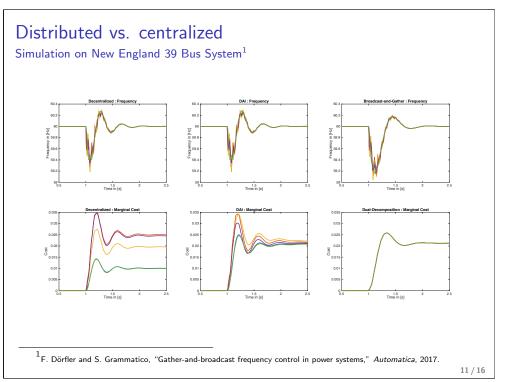
minimize 
$$\sum_{i=1}^{n} J_i(\Delta P_i^{ref})$$
  
subject to  $\sum_{i=1}^{n} \Delta P_i^{ref} + \Delta P_{u,i} = 0$   
 $\Delta P_i^{ref} \in \{\text{power limits}\}.$   
Equivalent:  
(i) Power balance  
(ii) Regulation  $\Delta \omega = 0$   
Solve w/  $\Delta \omega$  feedback + Lagrange coordination











#### Hierarchical or distributed coordination contd.

- **O Distributed** approach (primal-dual version) uses
  - virtual phase angles  $\hat{\theta}$
  - virtual flow on line  $\ell = (i, j)$  as  $\hat{p}_{\ell} = T_{\ell}(\hat{\theta}_i \hat{\theta}_j)$

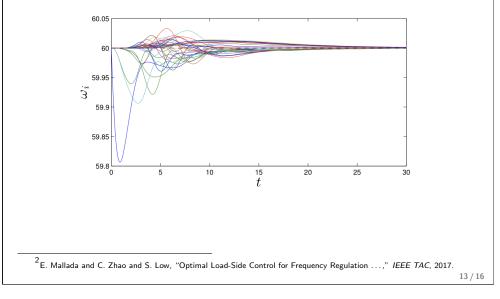
minimize  $\sum_{i=1}^{n} J_i (\Delta P_i^{\text{ref}}) + \frac{1}{2} D_i (\Delta \omega_i)^2$ <br/>subject to  $\Delta P_{u,i} + \Delta P_i^{\text{ref}} - D_i \Delta \omega_i = \sum_j A_{i\ell} \hat{p}_{\ell}$ <br/> $\Delta P_{u,i} + \Delta P_i^{\text{ref}} = \sum_j T_{ij} (\hat{\theta}_i - \hat{\theta}_j)$ 

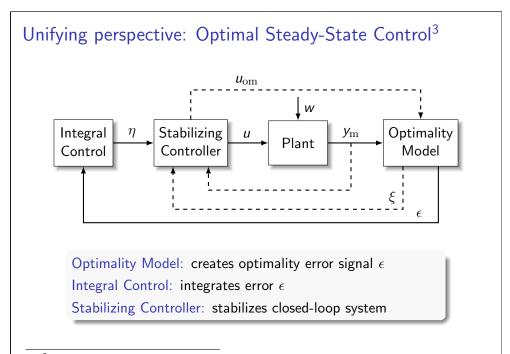
Now apply primal-descent and dual-ascent to Lagrangian  $\ensuremath{\mathcal{L}}$ 

Primal dynamics: Embeds natural system dynamics Dual dynamics: Distributed control

12/16







### Practical challenges

We have discussed structural and architectural aspects, but  $\ldots$ 

- **1** Dynamic models are **highly** uncertain and time-varying
  - Device models often either unknown or not maintained
  - High-order governor models, deadbands, saturation all important
  - $\bullet\,$  Machines dispatched in and out of system every  $\approx 15$  mins
  - Load characteristics change dramatically day-to-day
  - Even DC gain  $(\beta^{-1})$  of system can vary by a factor of 2–3!

Possible approach: **data-driven** + **gain-scheduled** methods

- ② Communication infrastructure challenges
  - If it ain't broke, don't upgrade it
  - High-bandwidth control over comm. channels perceived as risky

<sup>&</sup>lt;sup>3</sup>L. Lawrence, JWSP, E. Mallada "Linear-convex optimal steady-state control," *TAC*, Submitted.

## Questions



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