



# Control in Low-Inertia Power Systems: from the device level to the system level

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# Replacing the power system foundation



## *fuel & synchronous machines*

- not sustainable
- + central & dispatchable generation & ancillary service provision
- + large rotational inertia as buffer
- + self-synchronize through the grid
- + resilient voltage / frequency control
- slow actuation & control

## *renewables & power electronics*

- + sustainable
- distributed & variable generation & ancillary service provision
- almost no energy storage
- no inherent self-synchronization
- fragile voltage / frequency control
- + fast / flexible / modular control

# Issues are broadly recognized

- **low-inertia issues were not really on the radar** (outside few places, e.g., Ireland) until eight years ago

→ led to almost comical situations ...

Biblis A generator stabilizes the grid as a synchronous condenser



SIEMENS

USING DECOMMISSIONED NUCLEAR POWER PLANT AS SYSTEM SERVICE PROVIDERS

REPORT 2017:348

Energiforsk



**challenges:** low-inertia stability, grid-forming control, & fast frequency support

→ industry & academia joining forces & willing to explore **green-field approach**

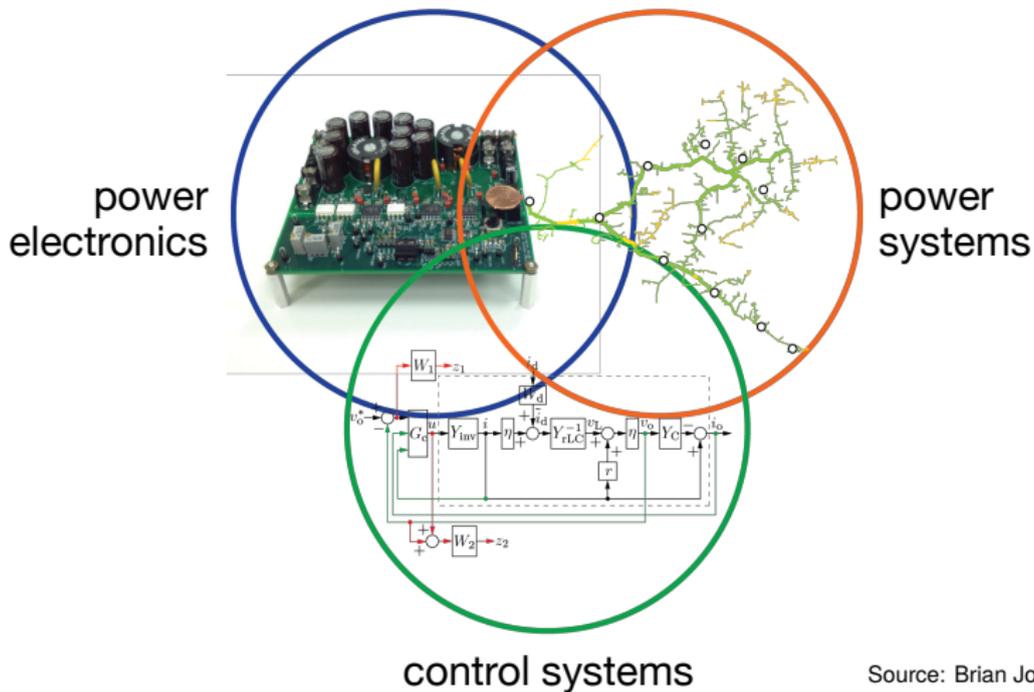
- since 2015: EU **MIGRATE** project & successors (OSMOSE, POSITYF, ...)



- across the pond:

unifi  
consortium

# Exciting research bridging communities



theory ↔ practice

device ↔ system

proof ↔ experiment

# Outline

Introduction

Device-Level: Grid-Forming Converter Control

System-Level: Ancillary Services in Low-Inertia Grids

Conclusions

# Outline

## Introduction

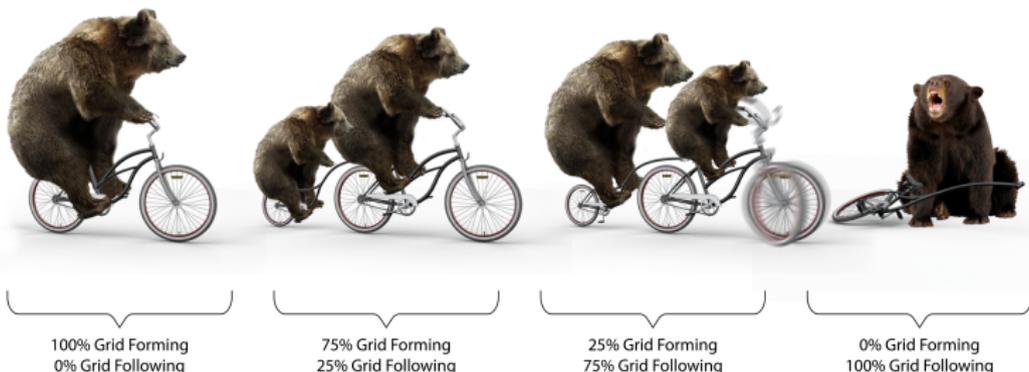
### Device-Level: Grid-Forming Converter Control

- Salient Characteristics & Specifications
- State-of-the-Art Grid-Forming Controls
- Synopsis & Lessons Learnt

### System-Level: Ancillary Services in Low-Inertia Grids

## Conclusions

# Grid-forming control

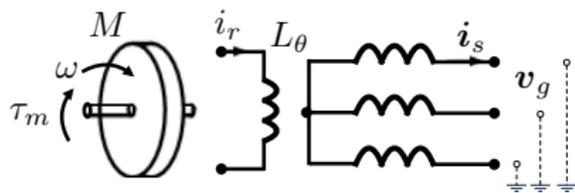


Source: NREL

- fact: power systems need XXX% of **grid-forming sources**
- **no universally accepted definition** of grid-forming behavior

	<i>grid-following</i>	<i>grid-forming</i>
<i>converter-type</i>	current-controlled & frequency-following	voltage-controlled & frequency-forming
<i>signal causality</i>	$(\omega, \ v\ ) \rightarrow (P, Q)$	$(P, Q) \rightarrow (\omega, \ v\ )$
<i>dynamic reachability</i>	needs a stiff grid	blackstart & islanded operation
<i>disturbance sensitivity</i>	filters only low frequencies	smoothens high frequencies

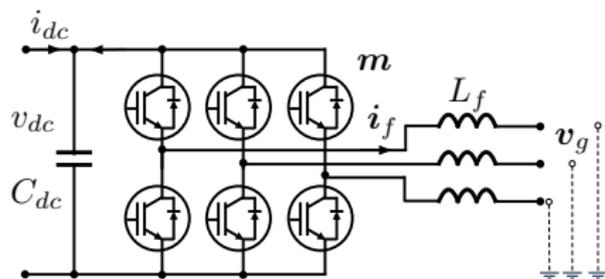
# Comparison: storage & conversion mechanisms



$$\frac{d\theta}{dt} = \omega$$

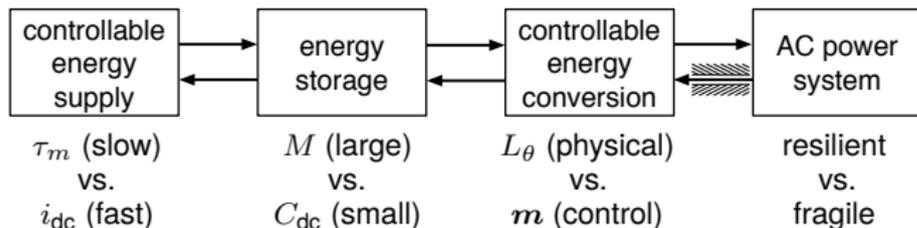
$$M \frac{d\omega}{dt} = -D\omega + \tau_m + L_m i_r \begin{bmatrix} -\sin\theta \\ \cos\theta \end{bmatrix}^\top \mathbf{i}_s$$

$$L_s \frac{d\mathbf{i}_s}{dt} = -R_s \mathbf{i}_s + \mathbf{v}_g - L_m i_r \begin{bmatrix} -\sin\theta \\ \cos\theta \end{bmatrix} \omega$$



$$C_{dc} \frac{dv_{dc}}{dt} = -G_{dc} v_{dc} + i_{dc} + \mathbf{m}^\top \mathbf{i}_f$$

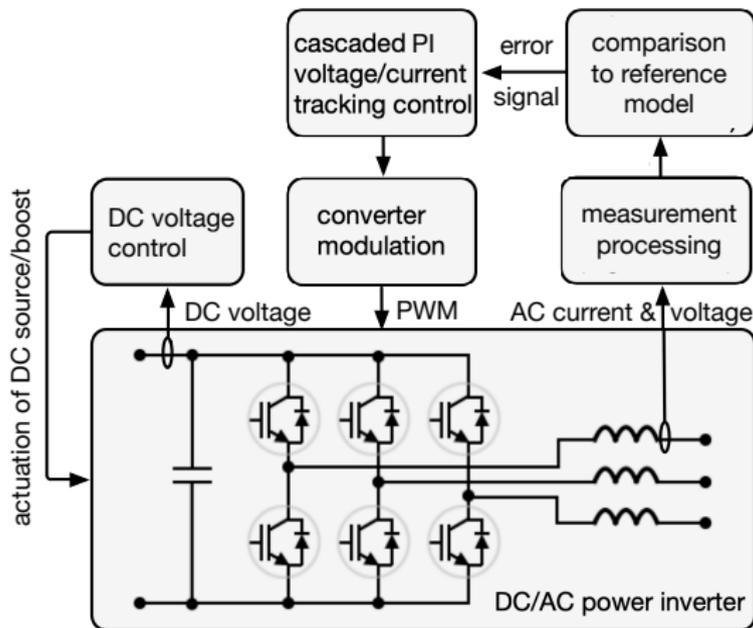
$$L_f \frac{d\mathbf{i}_f}{dt} = -R_f \mathbf{i}_f + \mathbf{v}_g - \mathbf{m} v_{dc}$$



physical & robust  
vs.  
controlled & agile  
**energy conversion**  
& (kinetic) **storage**

anti-podal characteristics  $\implies$  **do not use a converter to emulate a machine**

# Cartoon of power electronics control

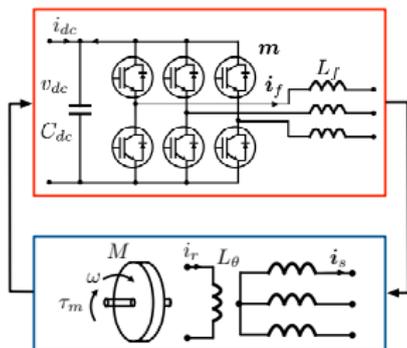


1. acquiring & processing of **AC measurements**
2. synthesis of **references** (voltage/current/power)  
*“how would a synchronous generator respond now ?”*
3. cascaded PI controllers to **track** reference error  
**assumption:** no state constraints encountered
4. **actuation** via modulation
5. **energy balancing** via DC-side supply (P-control on DC voltage)  
**assumption:** unlimited power & instantaneous

6. plus **implementation tricks:** saturation via virtual impedance, low-pass filter for dissipation, limiters, dead zones, logic, ...

# Conventional reference behaviors

## virtual synchronous machine



- **reference** = machine (order 3,...,12)

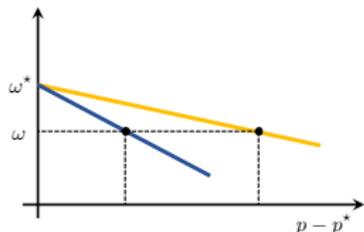
→ most commonly **accepted solution in industry** (backward compatibility?)

→ **poor fit**: converter  $\neq$  flywheel

- good small-signal but **poor post-fault performance** (reference not realizable)
- **over-parametrized** & ignores limits

→ **emulate only “useful” dynamics**

## droop / power-synchronization



- **direct control** of frequency & voltage via  $(p, \omega)$  &  $(q, \|v\|)$  droop

$$\omega - \omega^* \propto p - p^*$$

$$\frac{d}{dt} \|v\| = -c_1(\|v\| - v^*) - c_2(q - q^*)$$

→ **decoupling  $\neq$  true** in transients

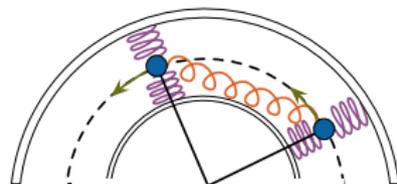
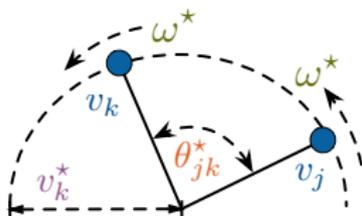
- **good small-signal but poor large signal** (narrow region of attraction)
- main reason: **two linear SISO loops for MIMO nonlinear system**

→ **need “nonlinear & MIMO” droop**

# Modern reference behaviors: VOC family

reference model: **virtual oscillator control (VOC)**

[Aracil, Torres, Johnson, Dhople, Krein, Colombino, Groß, & Dörfler]



- VOC dynamics realizable via **fully decentralized control & set-points**

$$\underbrace{\frac{d}{dt} v_k = \begin{bmatrix} 0 & -\omega^* \\ \omega^* & 0 \end{bmatrix} v_k}_{\text{oscillation at } \omega^*} + \underbrace{c_1 \cdot (v_k^{*2} - \|v_k\|^2) v_k}_{\text{local amplitude regulation}} + \underbrace{c_2 \cdot \left( \frac{1}{v_k^{*2}} \begin{bmatrix} q_k^* & p_k^* \\ -p_k^* & q_k^* \end{bmatrix} v_k - i_{f,k} \right)}_{\text{synchronization through grid current}}$$

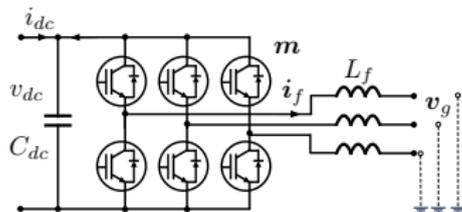
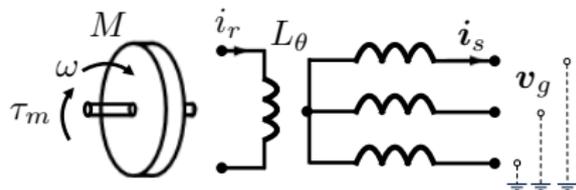
- polar coordinates reveal **nonlinear & multivariable droop control**

$$\frac{d}{dt} \theta_k = \omega^* + c_2 \left( \frac{p_k^*}{v_k^{*2}} - \frac{p_k}{\|v_k\|^2} \right) \Big|_{\|v_k\| \approx 1} \approx \omega^* + c_2 (p_k^* - p_k) \quad (p - \omega \text{ droop})$$

$$\frac{d}{dt} \|v_k\| \Big|_{\|v_k\| \approx 1} \approx c_1 (v_k^* - \|v_k\|) + c_2 (q_k^* - q_k) \quad (q - \|v\| \text{ droop})$$

- strong certificates** (interconnected stability) & **excellent ac performance**

# Duality & matching of synchronous machine conversion



$$\frac{d\theta}{dt} = \omega$$

$$M \frac{d\omega}{dt} = -D\omega + \tau_m + L_m i_r \begin{bmatrix} -\sin \theta \\ \cos \theta \end{bmatrix}^\top \mathbf{i}_s$$

$$L_s \frac{d\mathbf{i}_s}{dt} = -R_s \mathbf{i}_s + \mathbf{v}_g - L_m i_r \begin{bmatrix} -\sin \theta \\ \cos \theta \end{bmatrix} \omega$$

$$\frac{d\delta}{dt} = \eta \cdot v_{dc}$$

$$C_{dc} \frac{dv_{dc}}{dt} = -G_{dc} v_{dc} + i_{dc} + m_{\text{ampl}} \begin{bmatrix} -\sin \delta \\ \cos \delta \end{bmatrix}^\top \mathbf{i}_f$$

$$L_f \frac{d\mathbf{i}_f}{dt} = -R_f \mathbf{i}_f + \mathbf{v}_g - m_{\text{ampl}} \begin{bmatrix} -\sin \delta \\ \cos \delta \end{bmatrix} v_{dc}$$

1. modulation in polar coordinates:

$$\mathbf{m} = m_{\text{ampl}} \begin{bmatrix} -\sin \delta \\ \cos \delta \end{bmatrix} \quad \& \quad \dot{\delta} = m_{\text{freq}}$$

→ **duality**:  $C_{dc} \sim M$  is equivalent inertia

2. **matching**:  $m_{\text{freq}} = \eta v_{dc}$  with  $\eta = \frac{\omega^*}{v_{dc}^*}$

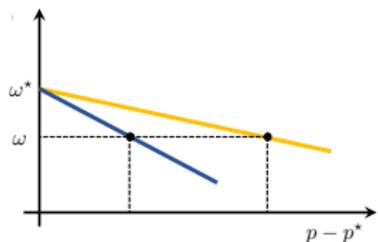
▶ **dc frequency**/imbalance signal  $\omega \equiv v_{dc}$

▶ **dc inertia**  $M \equiv C_{dc} \equiv$  fast dc source

▶ **structural** (not quantitative) **similarities**

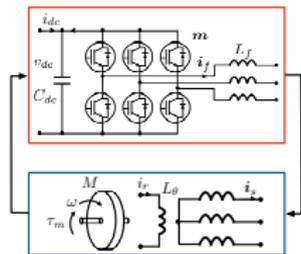
▶ **simple & robust** but **slow ac behavior**

# High-level comparison of grid-forming control



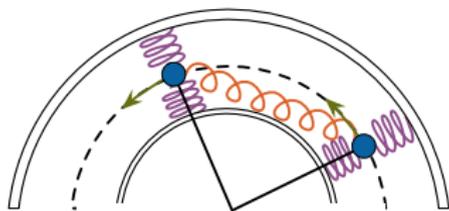
droop control

- + good performance near steady state
- relies on decoupling & small attraction basin



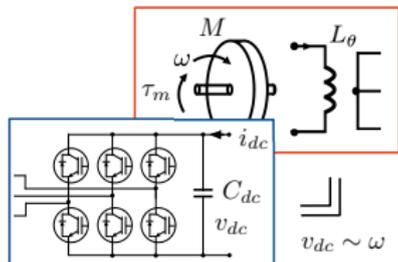
virtual synchronous machine

- + backward compatible in nominal case
- not resilient under large disturbances



virtual oscillator control

- + excellent large-signal behavior + local droop
- voc, droop, & vsm need strong dc source



matching control & duality

- + simple & robust
- slow ac performance

# Detailed comparison(s) (stopped collecting references at mid 2020)

## Comparison of Virtual Oscillator and Droop Controlled Isolated Three-Phase Microgrids

Zhan Shi<sup>1</sup>, Member, IEEE, Jiacheng Li<sup>1</sup>, Student Member, IEEE, Hendra I. Nurdin<sup>1</sup>, Senior Member, IEEE, and John E. Fletcher<sup>2</sup>, Senior Member, IEEE

## Comparison of Virtual Oscillator and Droop Control

Brian Johnson, Miguel Rodriguez  
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Email: brian.johnson@nrel.gov, mig.rodriguez@gmail.com

Mohit Sinha, Saikat Dhoipik  
Department of Electrical & Computer Engineering  
University of Minnesota  
Minneapolis, MN 55455  
Email: {sinha92, sdhoipik}@umn.edu

## Similarities between Virtual Oscillator Controlled and Droop Controlled Three-Phase Inverters

Zhan Shi, Hendra I. Nurdin, John E. Fletcher, Jiacheng Li  
School of Electrical Engineering and Telecommunications, UNSW Sydney, NSW, 2052, Australia  
Email: zhan.shi@unsw.edu.au, h.nurdin@unsw.edu.au, john.fletcher@unsw.edu.au, jiacheng.li@unsw.edu.au

## Comparative Transient Stability Assessment of Droop and Dispatchable Virtual Oscillator Controlled Grid-Connected Inverters

Hai Yu, Student Member, IEEE, M A Awwal, Student Member, IEEE, Hao Tu, Student Member, IEEE, Iqbal Husain, Fellow, IEEE and Sedjan Lukic, Senior Member, IEEE.

## Frequency Stability of Synchronous Machines and Grid-Forming Power Converters

Ali Tayyebi, Dominik Groß, Member, IEEE, Adolfo Ana, Friedrich Kupzog and Florian Dörfler, Member, IEEE

## GRID-FORMING CONVERTERS - INEVITABILITY, CONTROL STRATEGIES AND CHALLENGES IN FUTURE GRIDS APPLICATION

Ali TAYYEBI  
AIT and ETH Zurich - Austria

Florian DÖRFLER  
ETH Zurich - Switzerland

Friedrich KUPZOG  
Austrian Institute of Technology - Austria

## Comparison of Droop Control and Virtual Oscillator Control Realized by Andronov-Hopf Dynamics

Minghui Lu<sup>1</sup>, Victor Pufoa<sup>1</sup>, Saikat Dhoipik<sup>1</sup>, Brian Johnson<sup>2</sup>

## Transient response comparison of virtual oscillator controlled and droop controlled three-phase inverters under load changes

Zhan Shi<sup>1</sup>, Jiacheng Li<sup>1</sup>, Hendra I. Nurdin<sup>1</sup>, John E. Fletcher<sup>2</sup>  
School of Electrical Engineering and Telecommunications, UNSW Sydney, UNSW, NSW, 2052, Australia  
E-mail: zhan.shi@unsw.edu.au

## Simulation-based study of novel control strategies for inverters in low-inertia system: grid-forming and grid-following

Author: Alessandro Crivellano

Mathias Melby  
Comparison of virtual oscillator control and droop control in an inverter-based stand-alone microgrid

## Grid-Forming Converters control based on DC voltage feedback

Yuan Guo<sup>1</sup>, Hai-Peng Ren<sup>2</sup>, Jie Li<sup>2</sup>

- ▶ identical steady-state & similar small-signal behavior (after tuning)
- ▶ virtual synchronous machine has poor transients (converter  $\neq$  flywheel)
- ▶ **VOC has best large-signal behavior**: stability, post-fault-response, ...
- ▶ **matching control**  $\omega \sim v_{dc}$  **is most robust** though with slow AC dynamics
- ▶ ... comparison suggests **multivariable control** (e.g., VOC + matching)

# Synopsis & lessons learnt

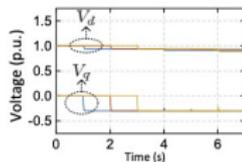
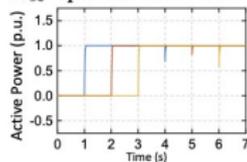
- ① **converter**  $\neq$  **flywheel**: very different actuation & energy storage
- ② take **dc voltage into account**: robust imbalance signal akin to frequency
- ③ **multivariable design** instead of decoupling: simple but results in huge gains

$$\begin{bmatrix} u_1 \\ \vdots \\ u_m \end{bmatrix} = \mathbb{K}(s) \begin{bmatrix} y_1 \\ \vdots \\ y_p \end{bmatrix}$$

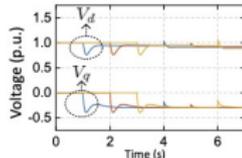
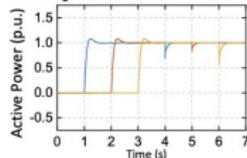
- inputs: modulation, dc-power supply, & inner references
- outputs: (nonlinear) state tracking errors

- blending of VOC + matching controls
- optimal & automated  $\mathcal{H}_2 / \mathcal{H}_\infty$  design

$\mathcal{H}_\infty$ -optimal controller



Drop controller



- ④ wide open: meet **current constraints** & remain stable post-fault
- ⑤ synchronization is only the beginning: what to do once sync'd? **services!**

# Outline

Introduction

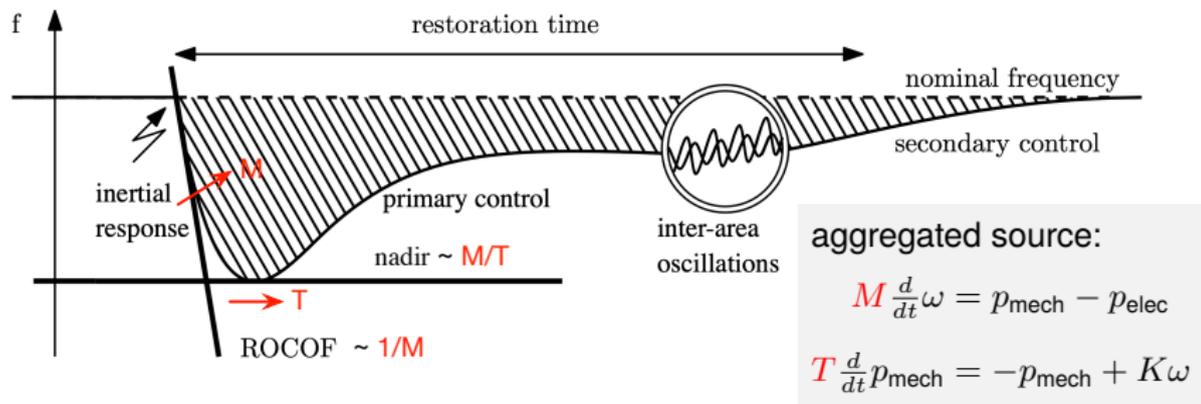
Device-Level: Grid-Forming Converter Control

**System-Level: Ancillary Services in Low-Inertia Grids**

- System-Level Metrics
- Ancillary Services: Where & How?
- Synopsis & Lessons Learnt

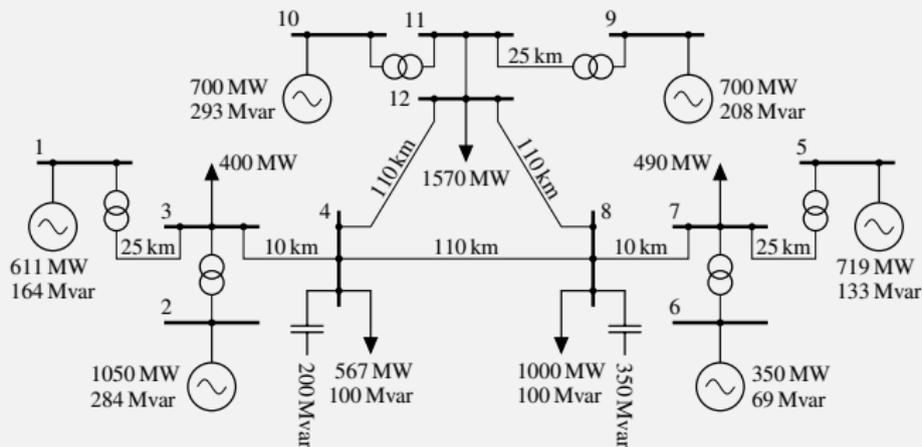
Conclusions

# Naive insight: we are loosing inertia



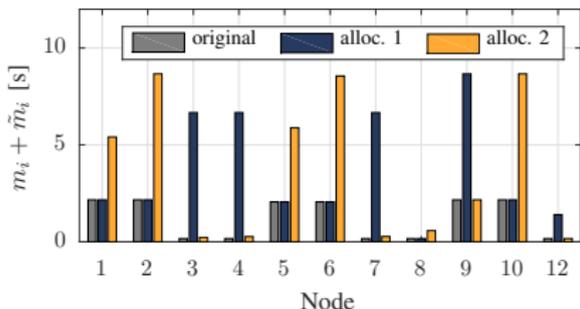
- **first-order observation:** less inertia  $M \implies$  steeper RoCoF & lower nadir
  - **second-order observation:** can trade off inertia  $M$  with faster actuation  $T$
  - **more profound observations:** the above classic hook curves reflect the physical behavior of a system dominated by synchronous machines
- $\rightarrow$  new physical phenomena  $\rightarrow$  **new metrics & new ancillary services** needed

# Illustrative case study: modified Kundur system

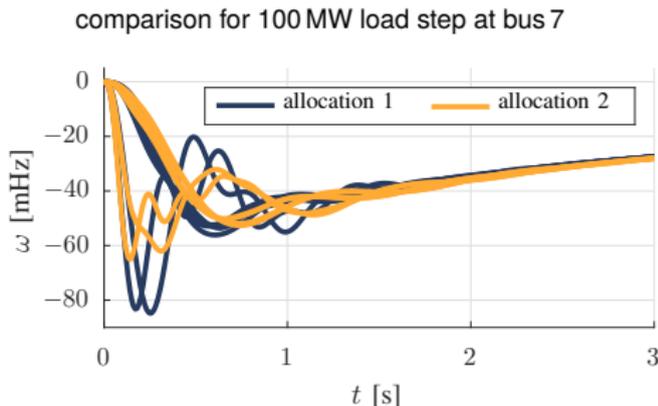
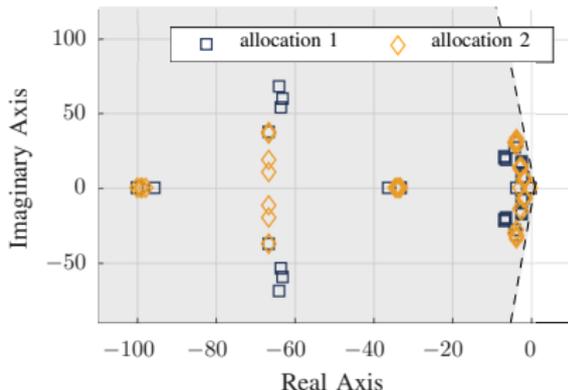


- added 3rd area to standard test case & grid-following virtual inertia at all buses
- original inertia 40s: removed 28s of rotational which can be re-allocated as virtual inertia

# Futile traditional metrics: RoCoF, spectrum, & inertia



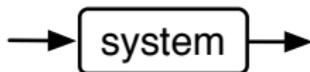
metrics	allocation 1	allocation 2
total inertia	40.85 s	40.85 s
damping ratio	0.1190	0.1206
RoCoF	0.8149 Hz/s	0.8135 Hz/s
$\omega$ nadir	-84.8 mHz	-65.1 mHz
peak injection	118.38 MW	7.0446 MW
control effort	15.581	2.699



# More useful metrics: system norms

- from step responses in a conventional power system to more modern (1980) **system norms** quantifying the effect of shocks on variables of interest

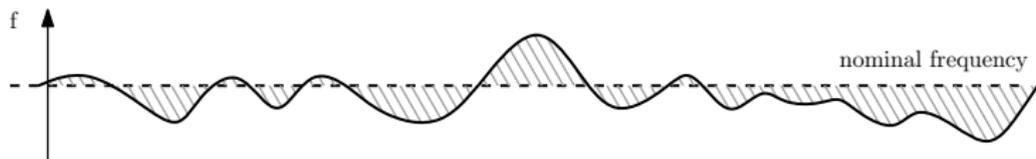
**disturbances:** impulse (fault), step (loss of generation), stochastic signal (renewables)



**performance outputs:** signal energy or peak in time / frequency domain of output

- versatile setup:** stochastic or deterministic (worst-case) settings
- practical:** efficiently computable & useful for both analysis & design
- example:** as a result of fault choose best fast frequency response to minimize

$$\int_0^{\infty} \{\text{frequency deviation}\}^2 + \{\text{coherency: deviation from COI}\}^2 + \{\text{control effort}\}^2 dt$$



# Case-study: South-East Australian Grid with B. Poola & D. Groß

The Sydney Morning Herald

NATIONAL

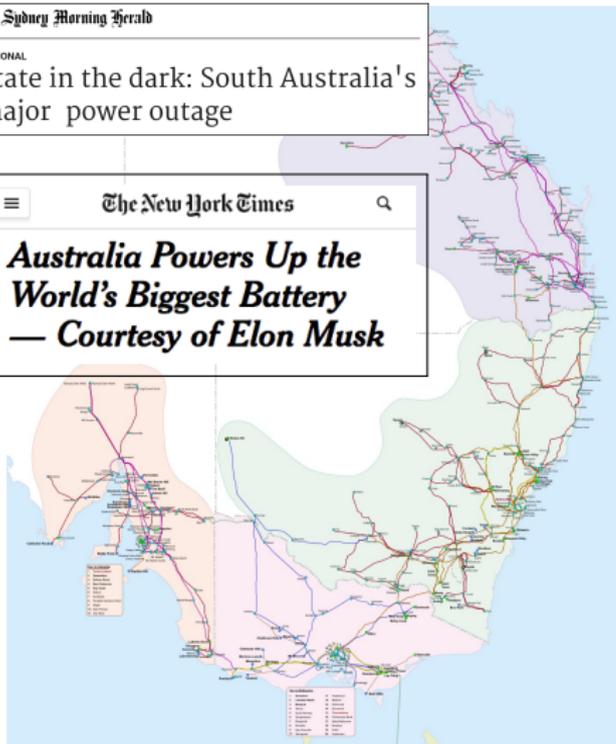
State in the dark: South Australia's major power outage



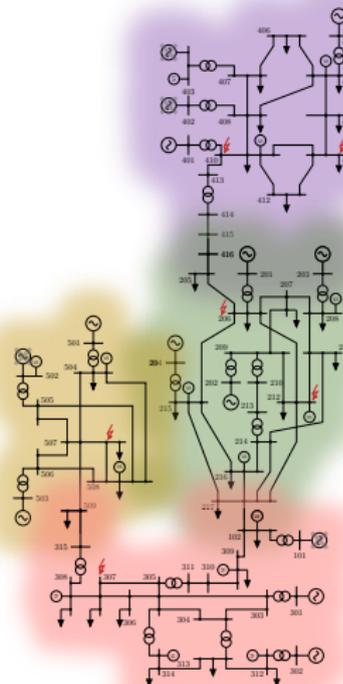
The New York Times



**Australia Powers Up the World's Biggest Battery — Courtesy of Elon Musk**

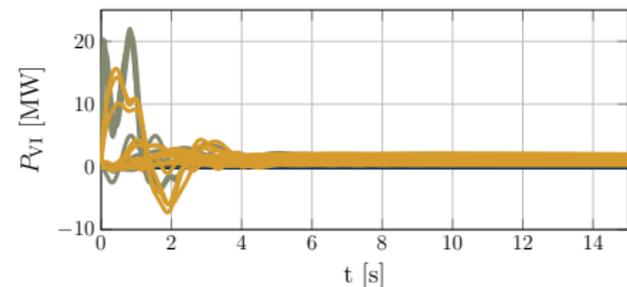
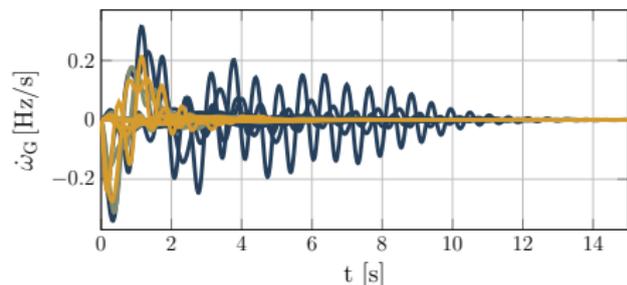
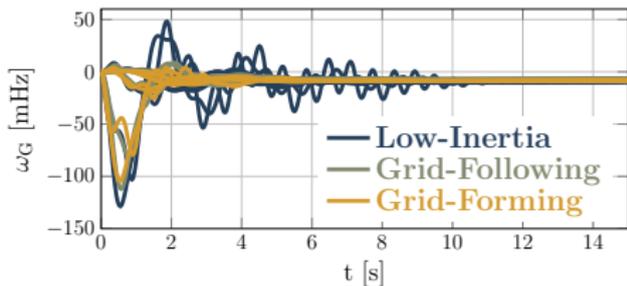


grid topology



simulation model

# Closed-loop with optimal fast frequency response



## *model & fast frequency response*

- replaced some machines with **converters** & (forming or following) fast frequency response: **virtual inertia + damping**

$$\text{power} = \frac{M s + D}{T s + 1} \text{ frequency}$$

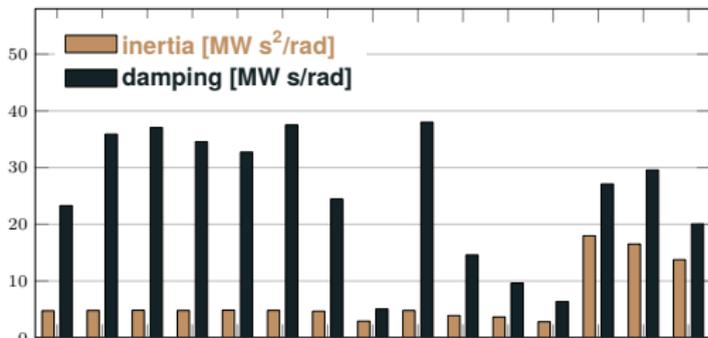
- choose performance inputs / outputs & **optimize response** on linearized model
- nonlinear closed-loop simulations: 200 MW disturbance at node 508

## *observations*

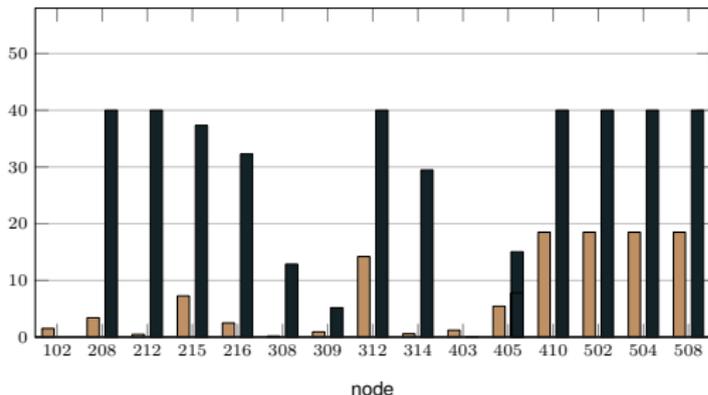
- system-level optimization **makes a difference** (even at same inertia)
- **forming beats following** in nadir, RoCoF, & peak power

# Optimal allocation of virtual inertia + damping

(a) Grid-Forming



(b) Grid-Following



## observations

- both control modes allocate virtual inertia in (blackout & battery) **area 5**
- **grid-following**: more reliance on damping (due to PLL-delay in  $\dot{\omega}$ )
- **grid-forming**: results in a more uniform (thus robust) allocations

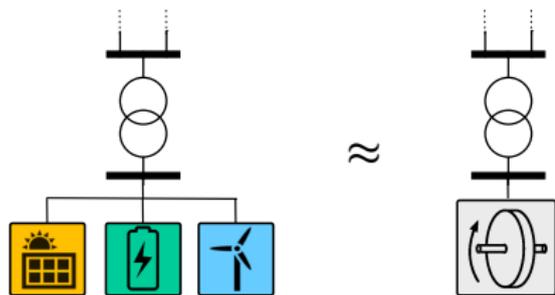
## conclusions

- **total inertia/damping** not crucial
- in comparison **spatial allocation** & **tuning** make a big difference
- implications for pricing & markets

# Services from Dynamic Virtual Power Plant (DVPP)

**DVPP**: coordinate heterogeneous set of DERs to collectively provide dynamic ancillary services

- **heterogenous** collection of devices
  - reliably provide services consistently across all power & energy levels and all time scales
  - none of the devices itself is able to do so
- **dynamic** ancillary services
  - fast response, e.g., inertia for brittle grid, robustly implementable on converter sources
  - specified as desired dynamic I/O response
- **coordination** aspect
  - decentralized control implementation
  - real-time adaptation to variable DVPP generation & ambient grid conditions

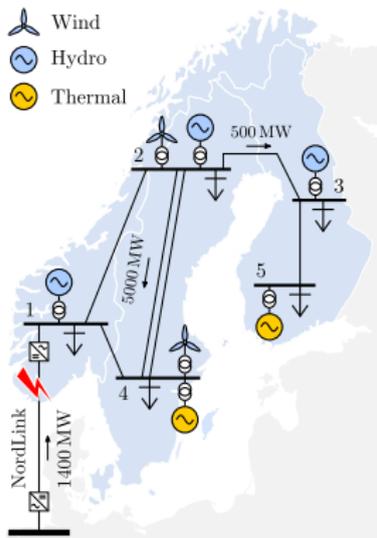


## examples

- ▶ frequency containment with non-minimum phase hydro & batteries (for fast response)
- ▶ wind providing fast frequency response & voltage support augmented with storage
- ▶ hybrid power plants, e.g., PV + battery + supercap

# Nordic case study

with J. Björk (Svenska kraftnät)  
& K.H. Johansson (KTH)



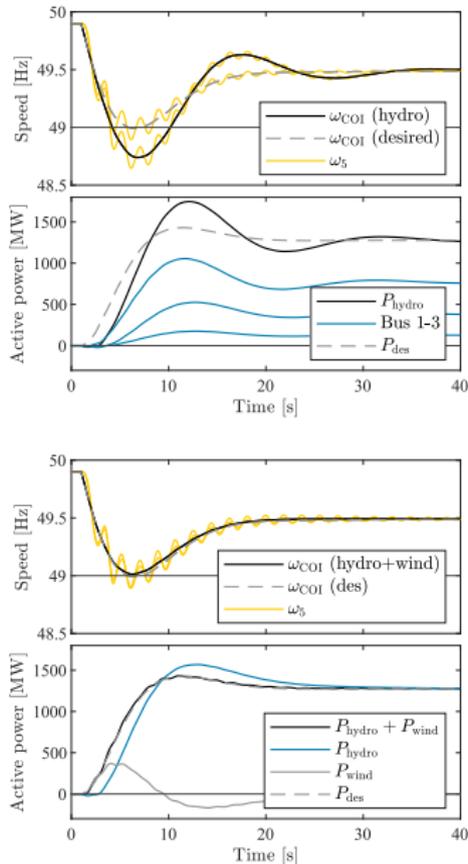
- **well-known issue:**  
 actuation of hydro is non-minimum phase  
 → initial power surge opposes control  
 → unsatisfactory response

- **discussed solution:**  
 augment hydro with on-site batteries for fast response  
 → works but not economic

- **better DVPP solution:**  
 coordinate hydro & wind to cover all time scales

- **FCR-D service**  
 → desired behavior

$$\frac{\text{power}}{\text{frequency}} = \frac{3100 \cdot (6.5s + 1)}{(2s + 1)(17s + 1)}$$



# Synopsis & lessons learnt

- ① initial literature was all about inertia . . . but we **should not extrapolate from the old system**: total inertia & conventional metrics might be misleading
- ② **system norms** are more useful, practical, & sharper metrics for both system analysis & optimal design of fast frequency response
- ③ **spatial allocation & tuning** of fast frequency response & **forming vs. following** behavior matters more than total amount of inertia & damping
- ④ **dynamic virtual power plants** to distribute ancillary services across heterogeneous DERs collectively covering all power levels & time scales
- ⑤ wide open: **specification of future ancillary services**, e.g., desired input/output responses + **% & location of grid-forming** sources

# Conclusions

- **do not think only of “inertia”** when designing converter controls, analyzing power systems, or specifying ancillary services
- rather: **adopt more system-theoretic & computational mind-set:** specify desired responses & use optimization + multivariable control
- grid-forming control is only part of the puzzle: what to once sync'd? **services!** who provides them? where? how to disaggregate the desired behavior?
- last: **free yourself from textbook plots** – tomorrow’s system will be different

