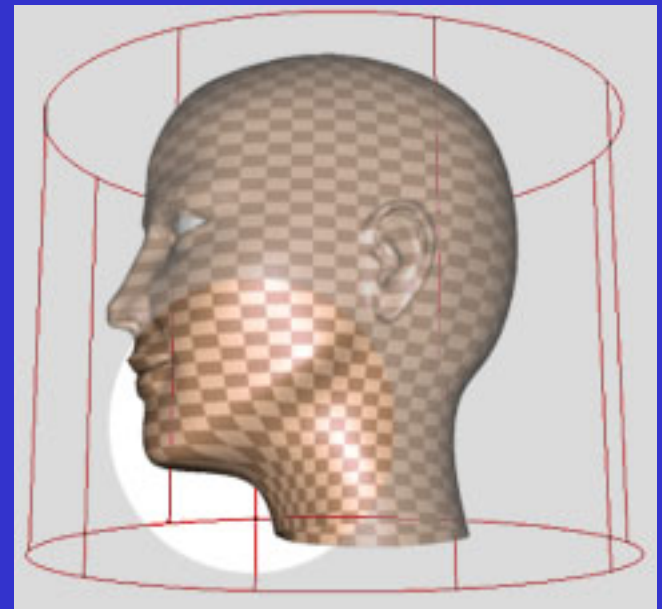


Surface Features: colour and texture



Introduction

colour

- color spaces
- colour constancy
- surface reflectance revisited
- illumination invariant colour features
- the holy grail: BRDFs

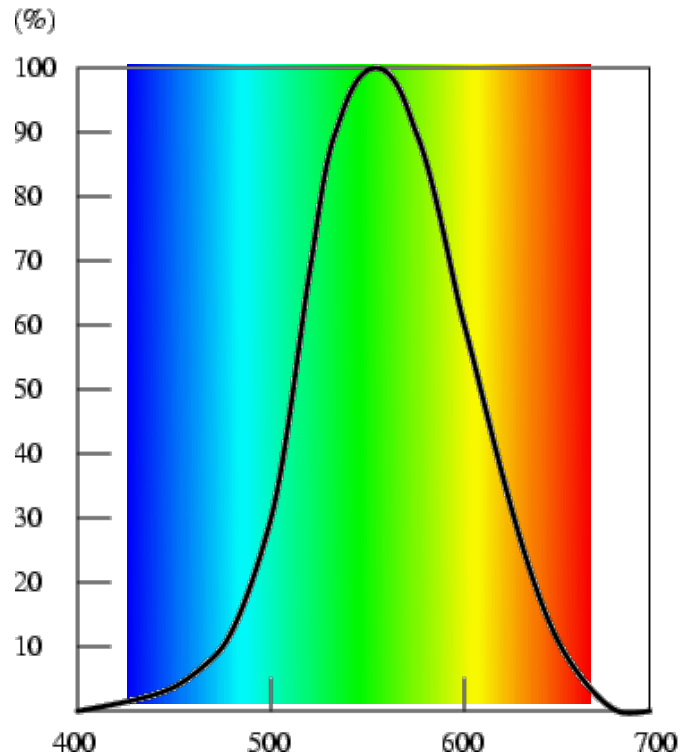
texture

- Fourier features
- cooccurrence matrices
- filter banks (Laws, Gabor, eigenfilters)
- stochastic model

COLOUR

The perception of brightness

- Luminous efficiency function ($v(\lambda)$):
relates radiometry & photometry



- C.I.E. (Commission Internationale de l'Eclairage) → standards



Link radiometry-photometry (Watt to lumen)

Photometry: subjective impressions

Radiometry: objective, physical measurements

at 555 nm : 1lm = 1/683 W = 1.46 mW

for light with spectral composition $c(\lambda)$ (radiant flux)

$$l = k \int_{\lambda=0}^{\infty} c(\lambda)v(\lambda)d\lambda$$

with k is 683 lumens/watt



The study of colour...

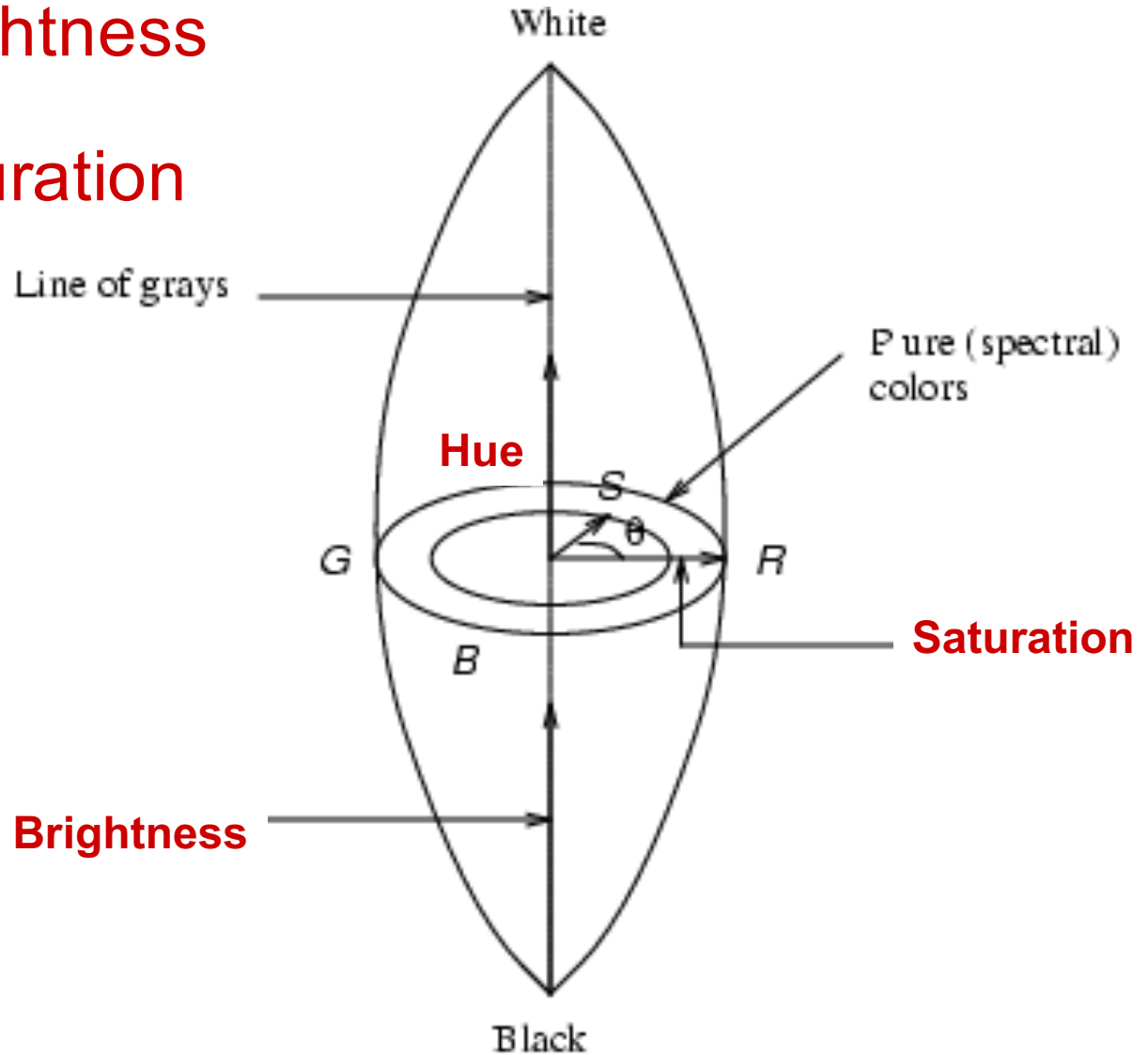
Use :

- pleasing to the eye (visualisation of results)
- characterising colours (features e.g. for recognition)
- generating colours (displays, light for inspection)
- understanding human vision

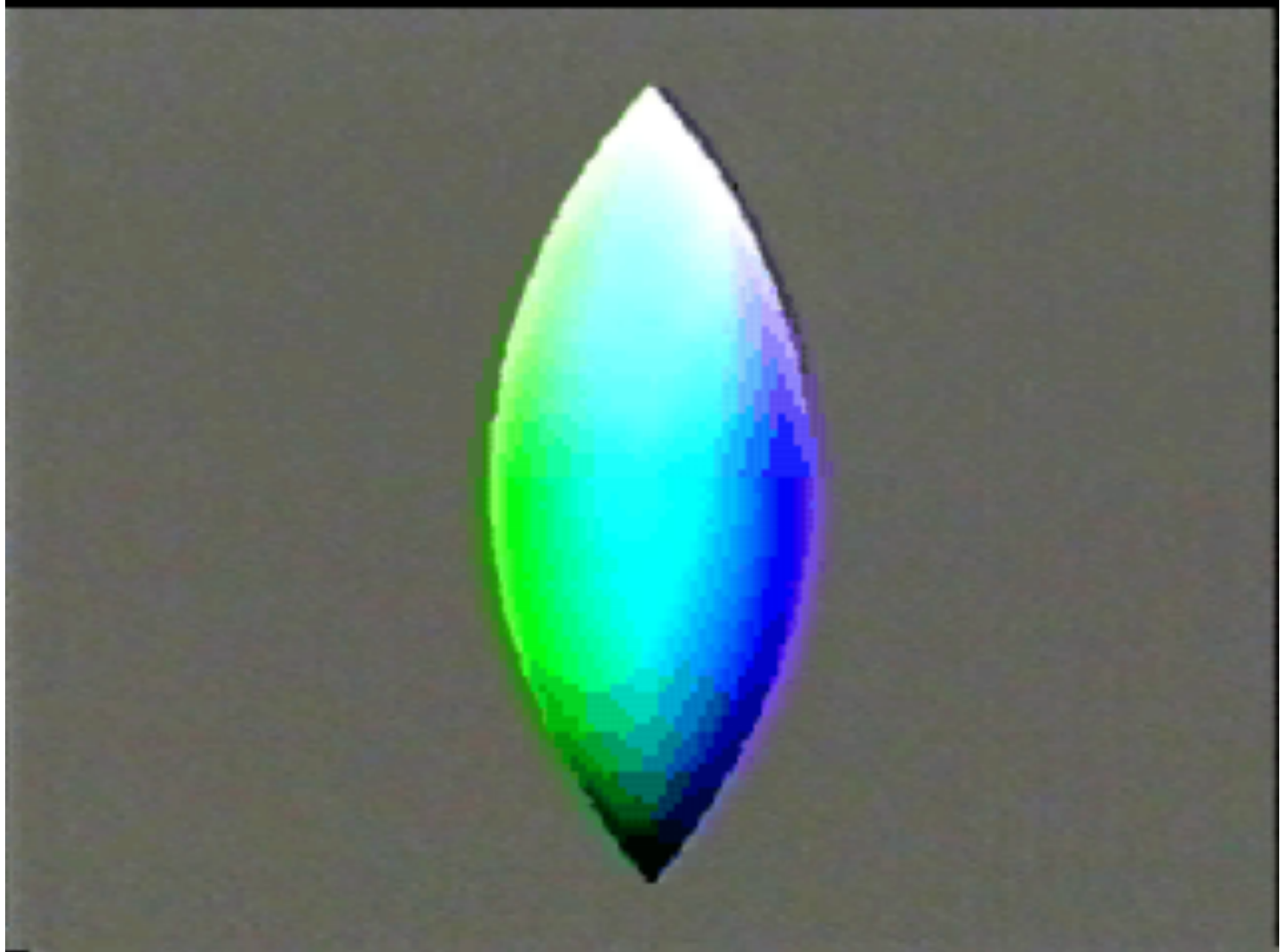


The perceptual attributes of light (humans)

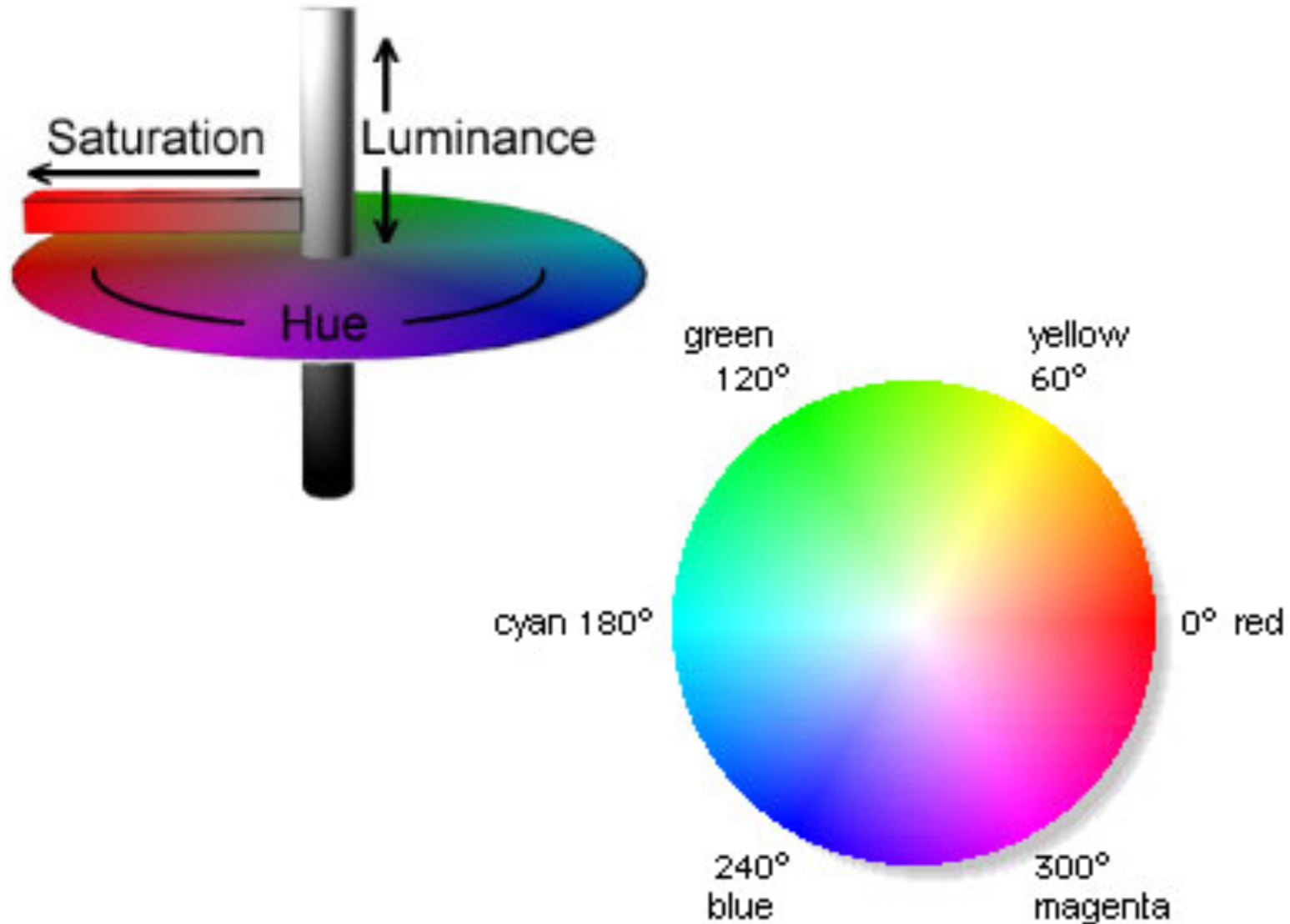
1. brightness
2. hue
3. saturation



The C.I.E. color space



Human perception of light = 3-dimensional



The history of colour

Newton → spectrum



Young → tristimulus model



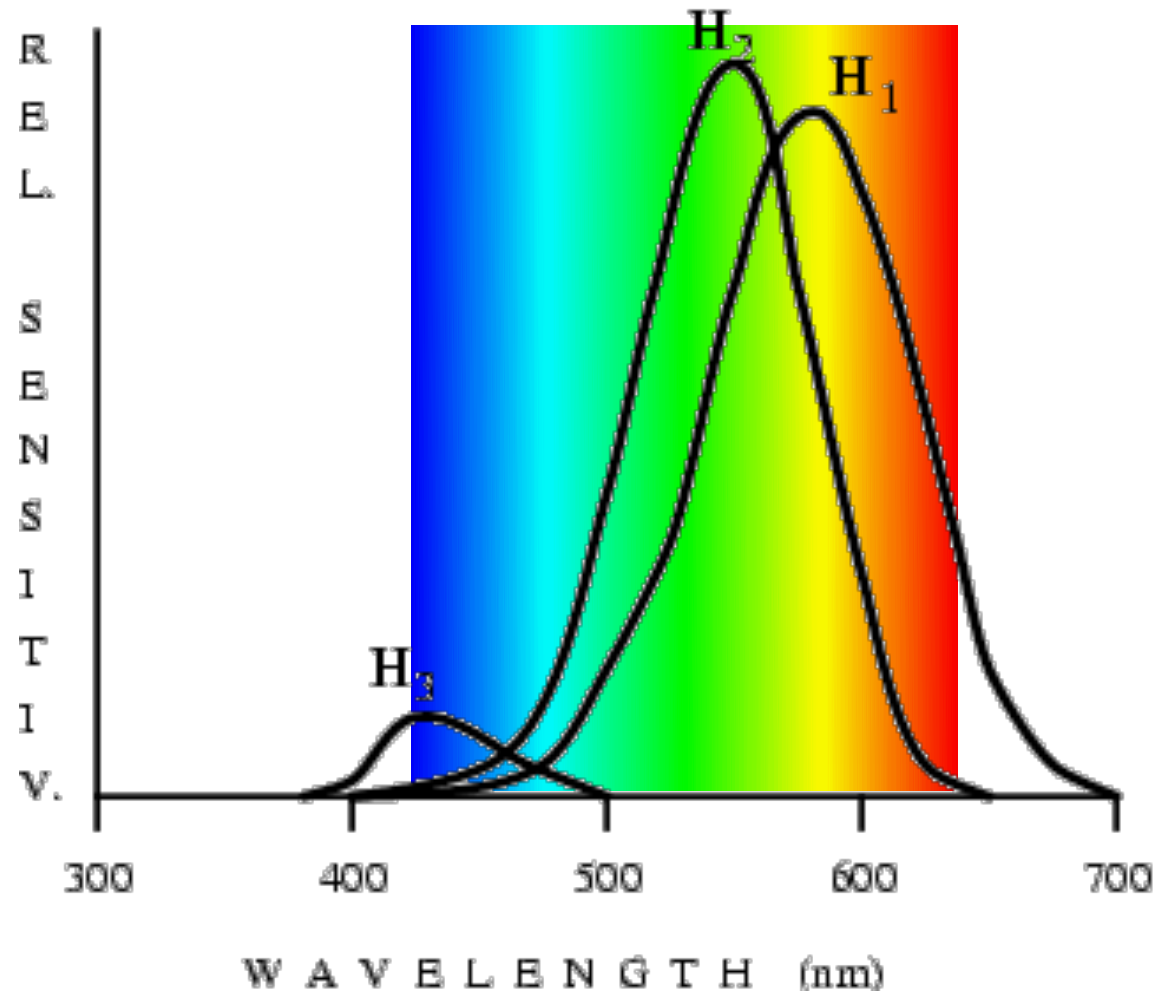
later : physiological
underpinning :

3 cone types



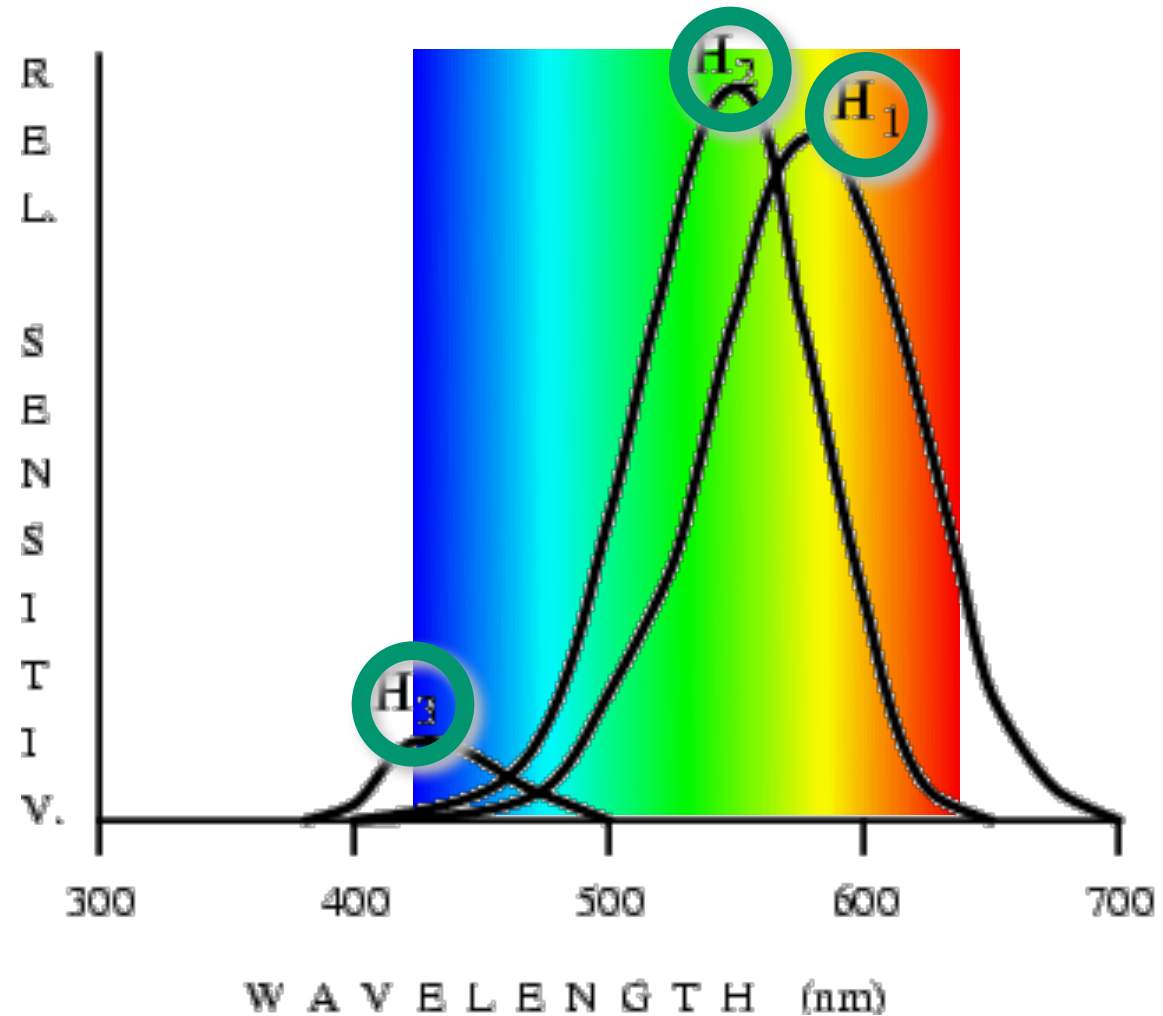
The retinal cones

3 types : blue, green, yellow-green



The retinal cones

3 types : blue, green, yellow-green



Prediction of colour sensation

source with spectral radiant flux $C(\lambda)$
produces responses R_i , with $i = 1, 2, 3$

$$R_i(c) = \int H_i(\lambda)C(\lambda)d\lambda, i = 1, 2, 3$$

Hence, our perception of multi-spectral
sources is quite impoverished:

an entire distribution over λ is projected
onto only 3 numbers R .



Prediction of colour sensation

source with spectral radiant flux $C(\lambda)$
produces responses R_i , with $i = 1, 2, 3$

$$R_i(c) = \int H_i(\lambda) C(\lambda) d\lambda, i = 1, 2, 3$$

- ❑ 2 sources with equal R_i 's \Rightarrow observed as same colour!
- ❑ luminance \perp chrominance
- ❑ 10% of population have abnormal colour vision



- ❑ several birds have 4 cone types (incl. UV)
- ❑ colour constancy



Tristimulus representation of colour

Camera \Rightarrow tristimulus values \Rightarrow display

3 primaries $P_j(\lambda)$, $j = 1, 2, 3$

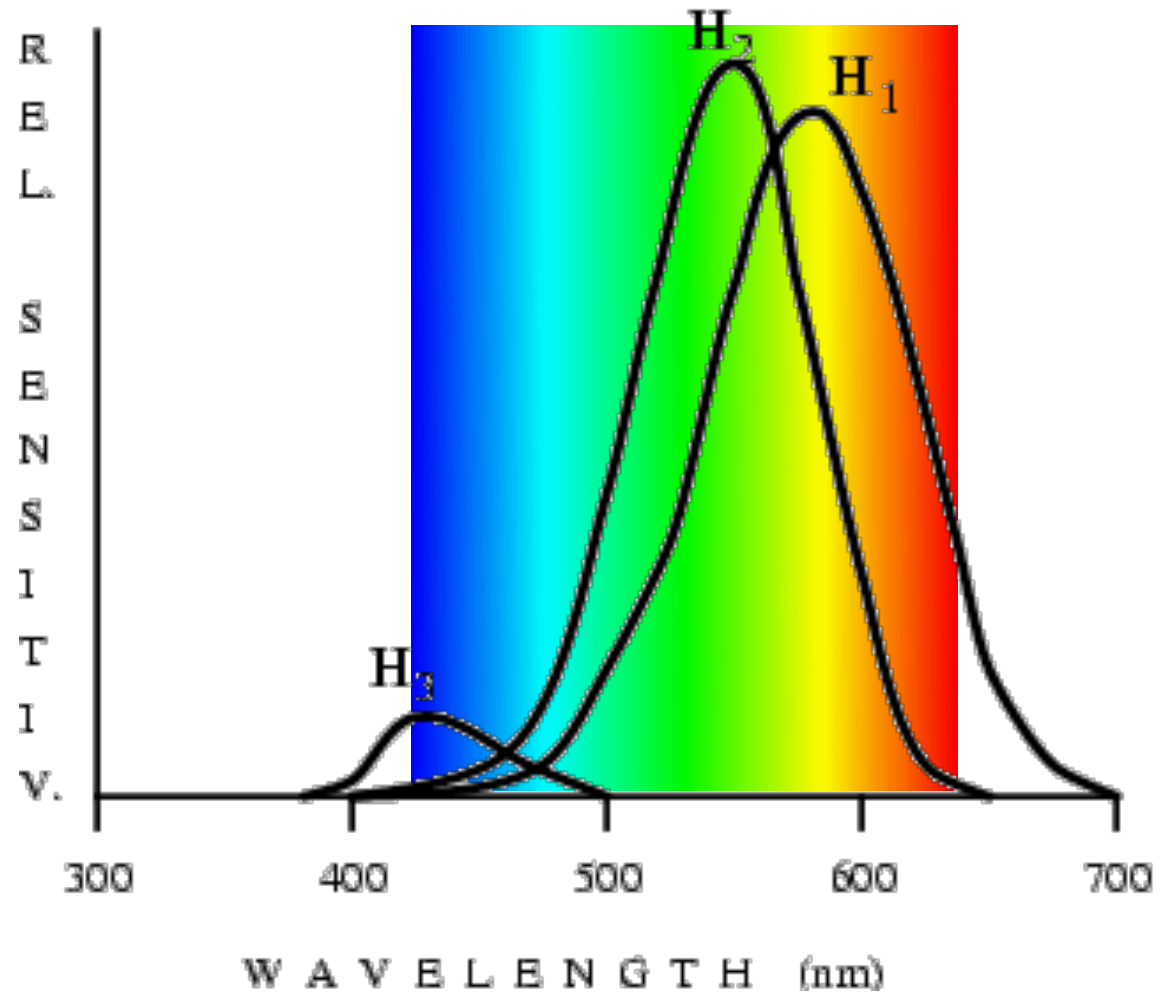
CIE primaries : $\lambda_1 = 700$
 $\lambda_2 = 546.1$
 $\lambda_3 = 435.8$

applications : practical primaries
e.g. TV : EBU and NTSC



Reminder: 3 retinal cone types

3 types : blue, green, yellow-green



The matching of colour

source $C(\lambda)$ matched by primaries

$$\sum_{j=1}^3 m_j P_j(\lambda)$$

$$R_i(C) = \int C(\lambda) H_i(\lambda) d\lambda$$



The matching of colour

source $C(\lambda)$ matched by primaries

$$\sum_{j=1}^3 m_j P_j(\lambda)$$

$$R_i(C) = \int \sum_{j=1}^3 m_j P_j(\lambda) H_i(\lambda) d\lambda$$



The matching of colour

source $C(\lambda)$ matched by primaries

$$\sum_{j=1}^3 m_j P_j(\lambda)$$

$$\begin{aligned} R_i(C) &= \int \sum_{j=1}^3 m_j P_j(\lambda) H_i(\lambda) d\lambda \\ &= \sum_{j=1}^3 m_j \int H_i(\lambda) P_j(\lambda) d\lambda \end{aligned}$$



The matching of colour

source $C(\lambda)$ matched by primaries

$$\sum_{j=1}^3 m_j P_j(\lambda)$$

$$R_i(C) = \int \sum_{j=1}^3 m_j P_j(\lambda) H_i(\lambda) d\lambda$$

$$= \sum_{j=1}^3 m_j \underbrace{\int H_i(\lambda) P_j(\lambda) d\lambda}_{l_{i,j}}$$

can be determined “off-line”



The math

extremely simple : linear equations

$$\sum_{j=1}^3 m_j l_{i,j} = R_i$$

implies inverting the matrix :
independent primaries!

also linear transform between the m_j 's
for different choices of primaries:

$$L m = R$$

$$L' m' = R$$

gives

$$m' = L'^{(-1)} L m$$



Tristimulus values

“white” considered a reference :
specify relative values w.r.t. m_j s for white : w_j

$$\text{Tristimulus values : } T_j = \frac{m_j}{w_j}$$

The scaling preserves the linearity

CIE tristimulus values : **R**, **G**, **B**

(for CIE white = flat spectrum & $w_1 = w_2 = w_3$)

Note that for white $T_1 = T_2 = T_3 = 1$

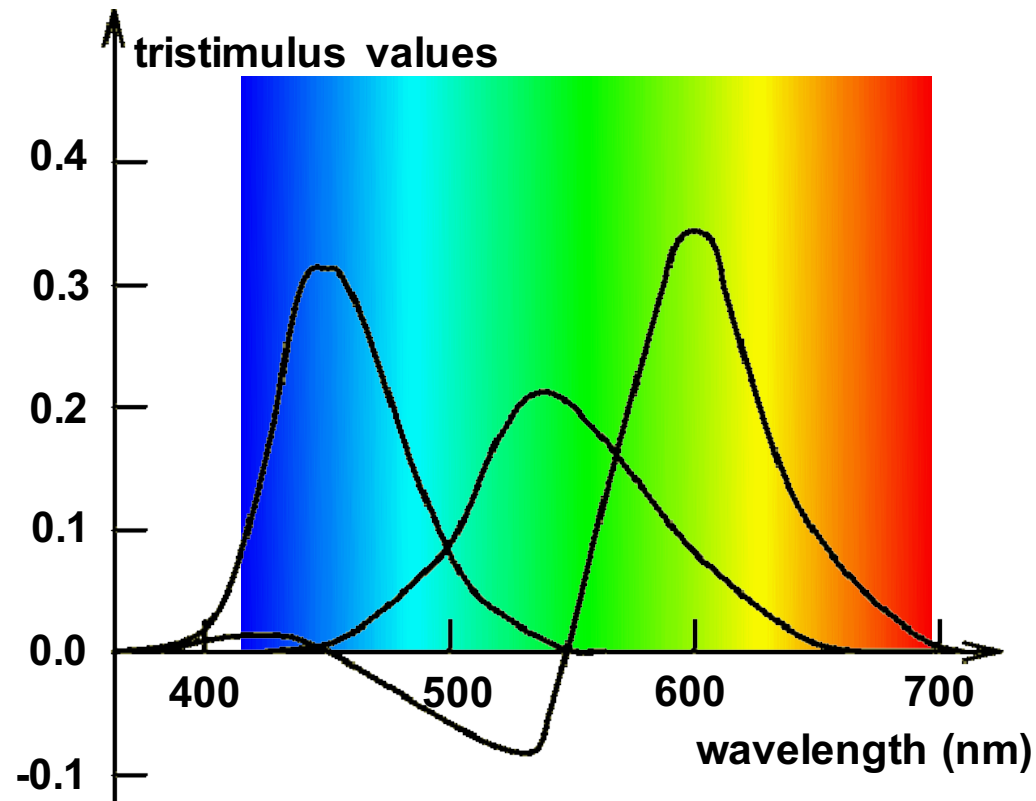


Spectral matching curves

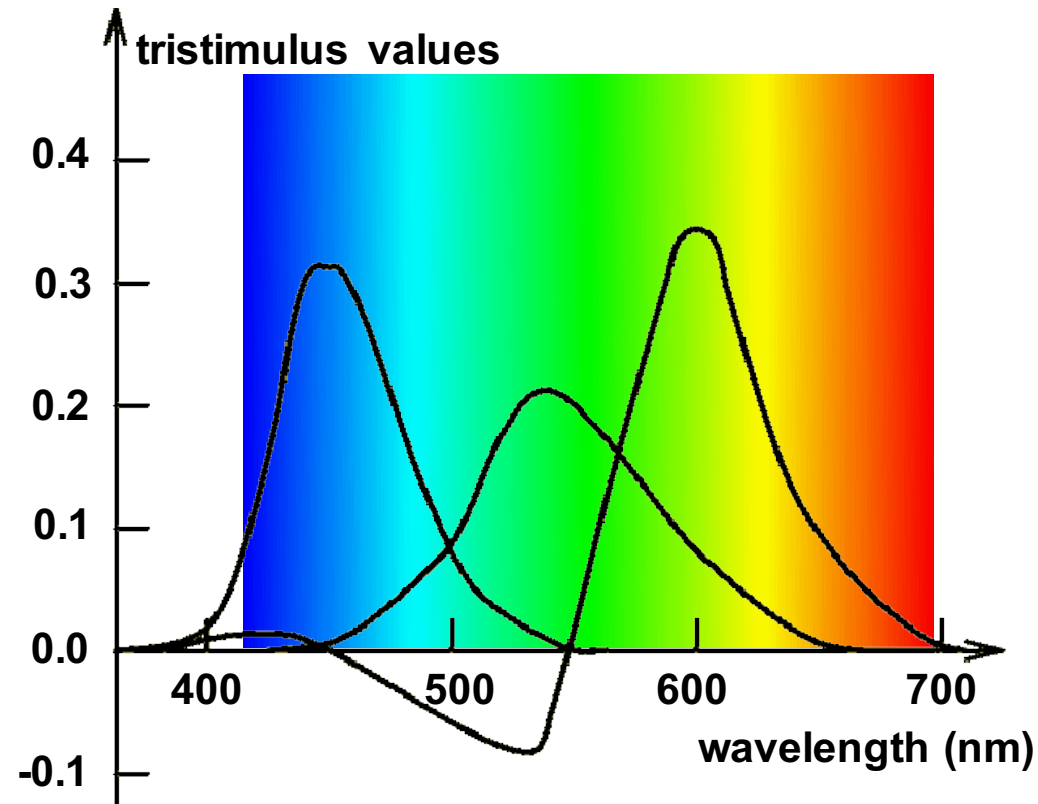
Spectral matching curves $T_j(\lambda)$:
values for monochromatic sources

$$R_i(C_\lambda) = H_i(\lambda) = \sum_{j=1}^3 m_j l_{i,j} = \sum_{j=1}^3 w_j l_{i,j} T_j(\lambda)$$

for the CIE primaries:



Interpretation of these curves



negative values : colours that cannot be produced

In such case:

$\text{mix}(\text{target}, \text{neg. primary}) = \text{mix}(\text{pos. primaries})$

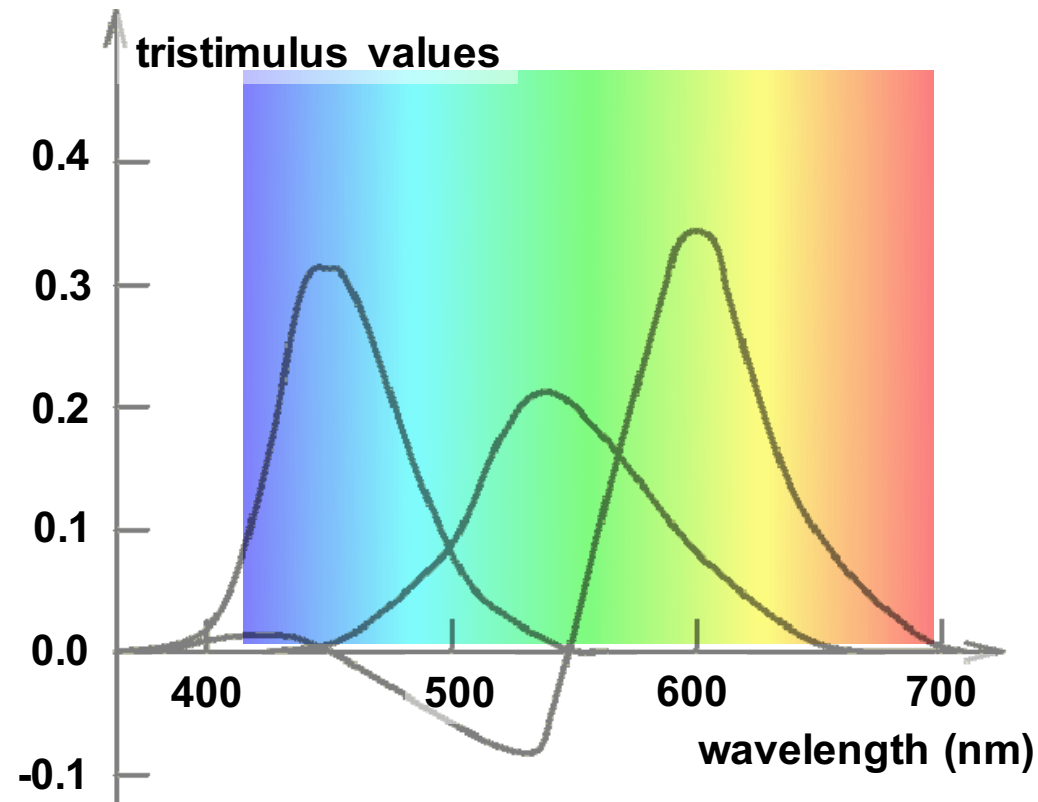
for any primary triple some colours cannot be produced



Interpretation of these curves

for arbitrary source $C(\lambda)$:

$$T_j(C) = \int C(\lambda)T_j(\lambda)d\lambda$$



Chromaticity coordinates

tristimulus values still contain brightness info

chrominance info pure : normalising the
tristimulus values



chromaticity coordinates :

$$t_j = \frac{T_j}{T_1 + T_2 + T_3}$$

$t_1 + t_2 + t_3 = 1$ allows to eliminate one

2 chromaticity coordinates specify saturation
and hue



Chromaticity coordinates

tristimulus values still contain brightness info

chrominance info pure : normalising the
tristimulus values



chromaticity coordinates :

$$t_j = \frac{T_j}{T_1 + T_2 + T_3}$$

Note that for white $t_1 = t_2 = t_3 = 1/3$

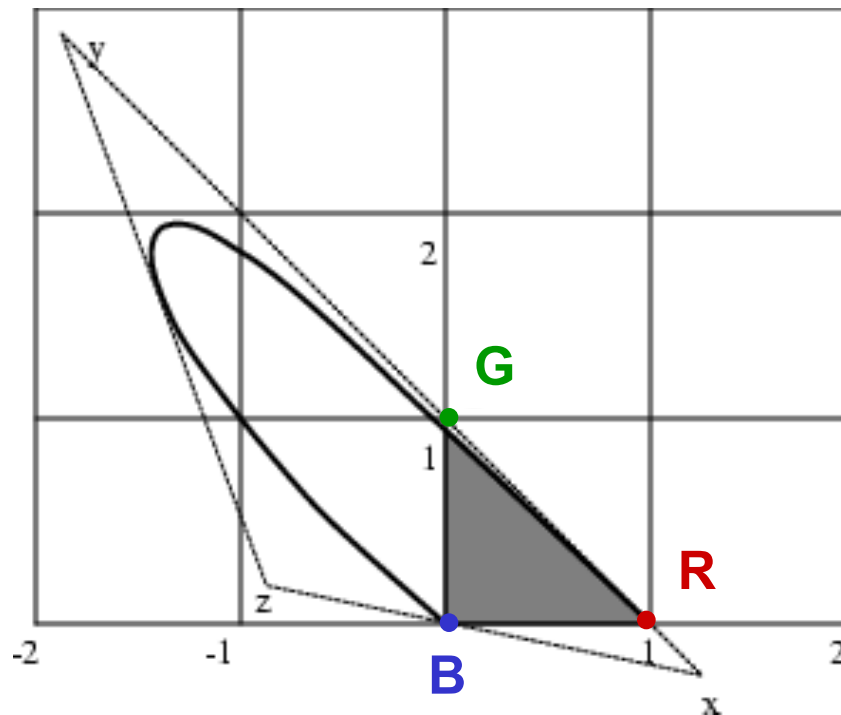


CIE chromaticity diagram

chromaticity coordinates (r, g) for CIE primaries :

$$r = \frac{R}{R + G + B} \quad g = \frac{G}{R + G + B}$$

The corresponding colour space :



CIE x-y coordinates

In order to get rid of the negative values :
virtual tristimulus colour system X,Y,Z
(no such physically realizable primaries exist !)

linear transf. from R,G,B to X,Y,Z coordinates :

$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix} = \begin{pmatrix} 0.490 & 0.310 & 0.200 \\ 0.177 & 0.813 & 0.011 \\ 0.000 & 0.010 & 0.990 \end{pmatrix} \begin{pmatrix} R \\ G \\ B \end{pmatrix}$$

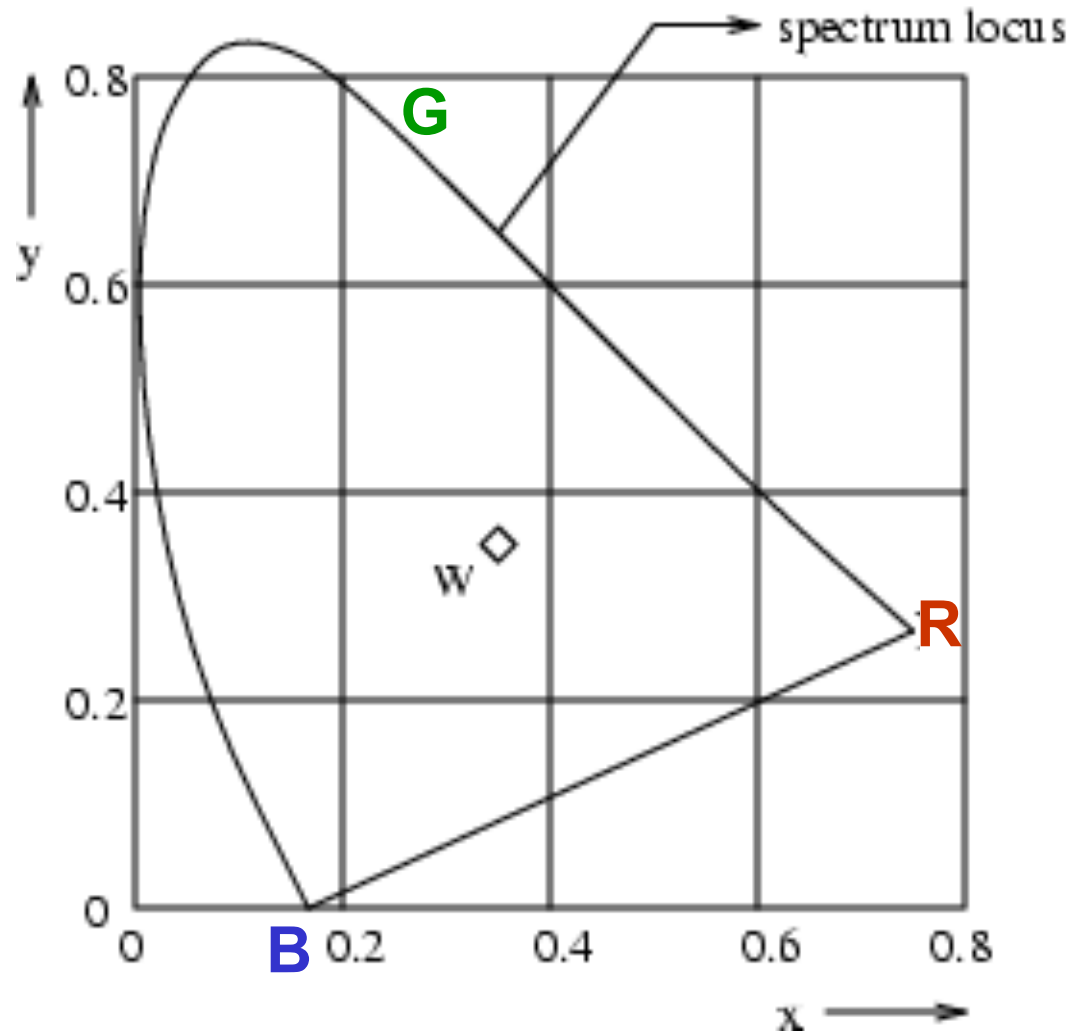
chosen as to make Y represent luminance

white (R=G=B=1) mapped to X=Y=Z=1

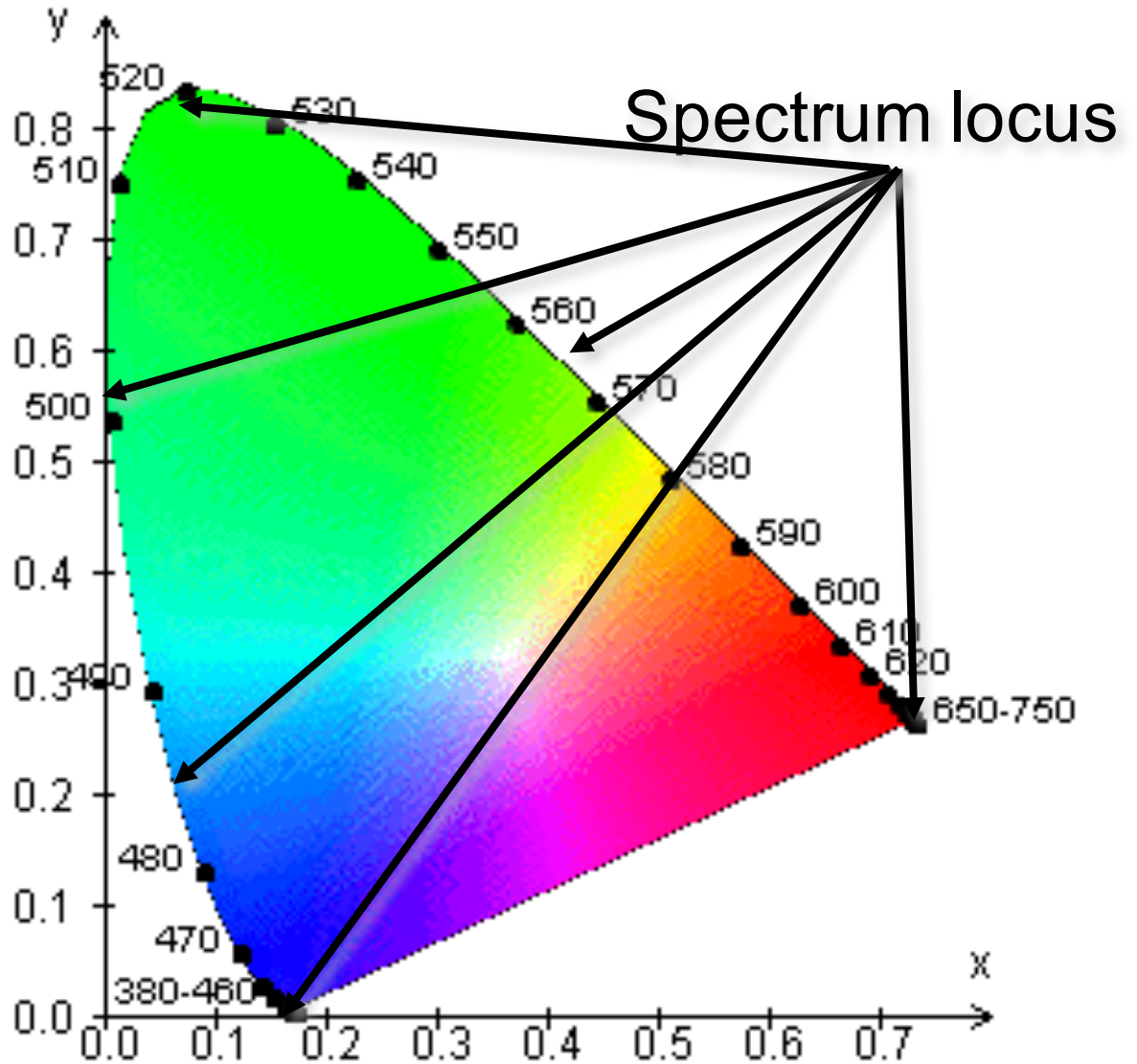
$$x = \frac{X}{X + Y + Z} \qquad y = \frac{Y}{X + Y + Z}$$



CIE x,y colour triangle



CIE x,y colour triangle



TV primaries

the EBU primaries have coordinates

$$R_r : \quad x = 0.64 \quad y = 0.33$$

$$G_r : \quad x = 0.29 \quad y = 0.60$$

$$B_r : \quad x = 0.15 \quad y = 0.06$$

the NTSC primaries have coordinates

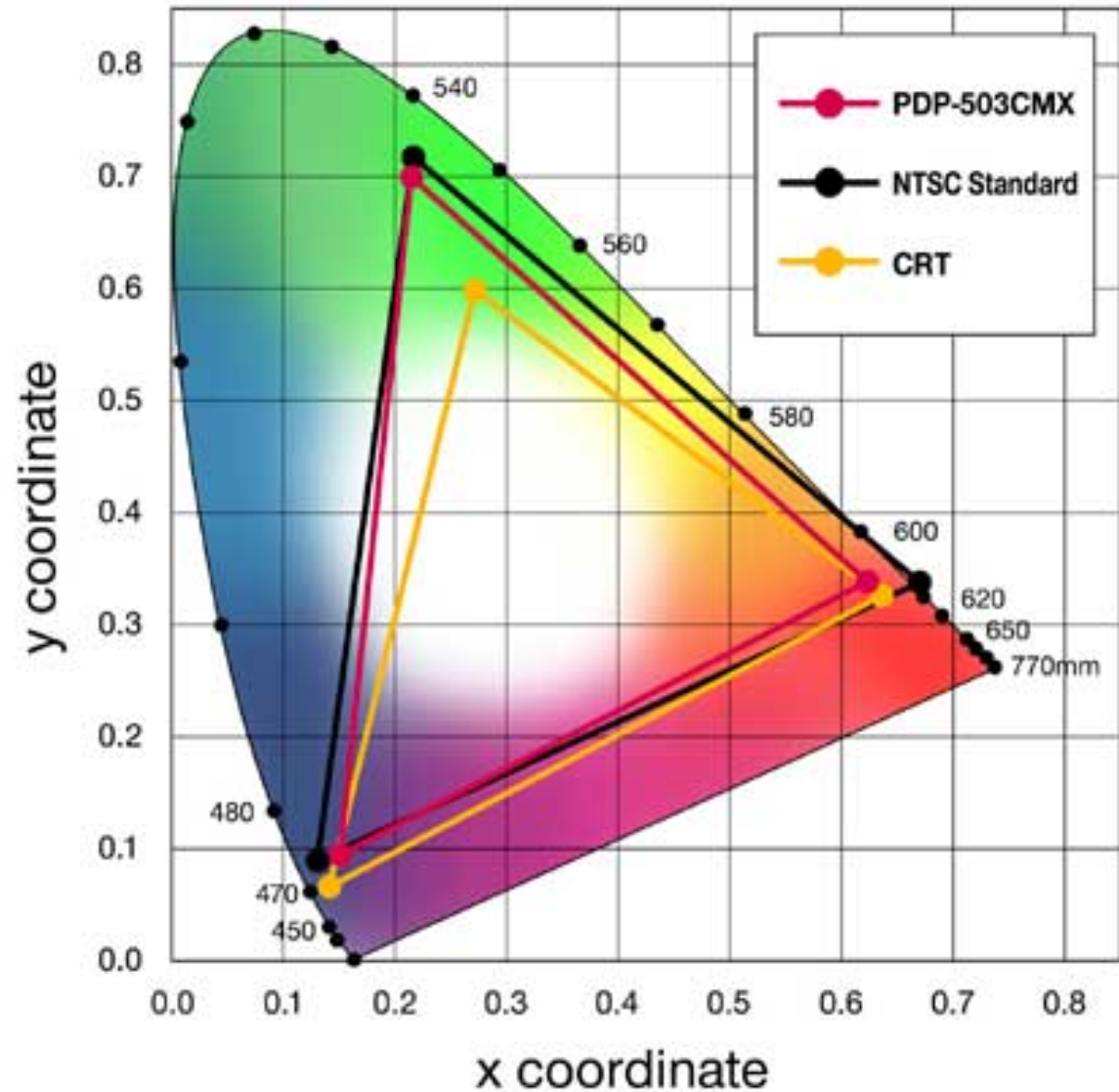
$$R_N : \quad x = 0.67 \quad y = 0.33$$

$$G_N : \quad x = 0.21 \quad y = 0.71$$

$$B_N : \quad x = 0.14 \quad y = 0.08$$



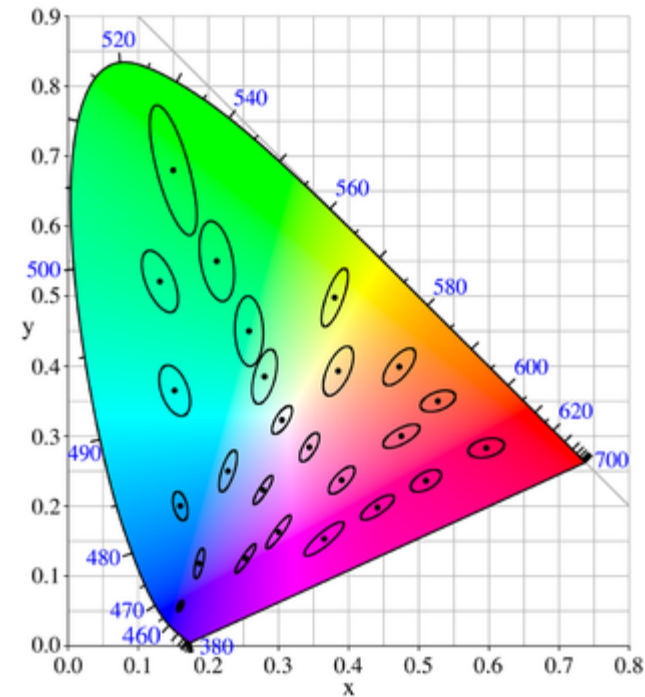
CIE Chromaticity Coordinates



Notes

Minimize colours outside the triangle!

Area dubious criterion :
projective transf. between chromaticity coordinates
distance in triangle no faithful indication of
perceptual difference



pure spectrum colours (on the spectrum locus) are rare
in nature



Chromaticity coordinate transitions

So, colour coordinates need for their definition
3 primaries + white : 4 points

4 points define a projective frame :

primaries $\implies (0,0), (1,0), (0,1)$

white $\implies (0.33, 0.33)$

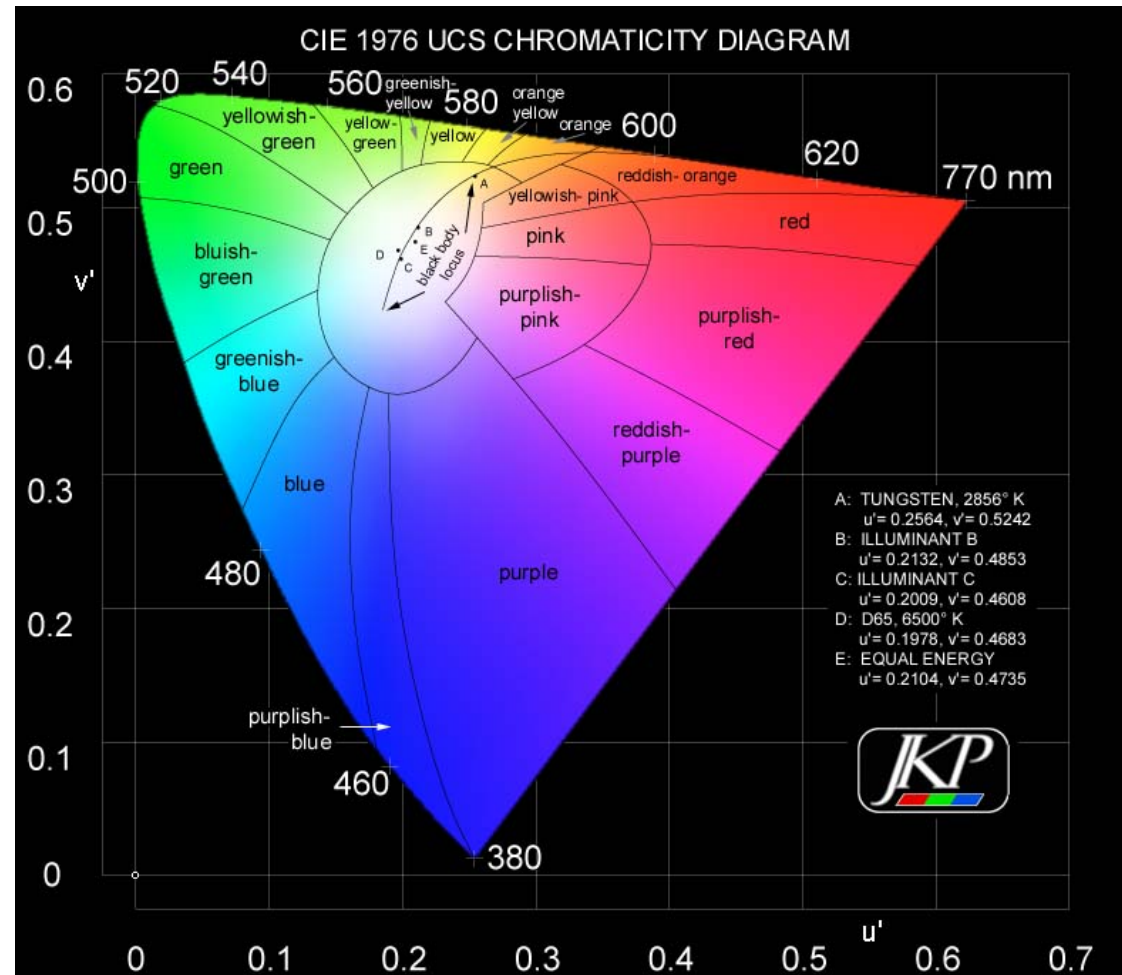
a chromaticity coordinate transformation can be shown to be projective, i.e. non-linear



CIE u-v color coordinates

$u - v$ diagram +/- faithfully represents perceptual distance :

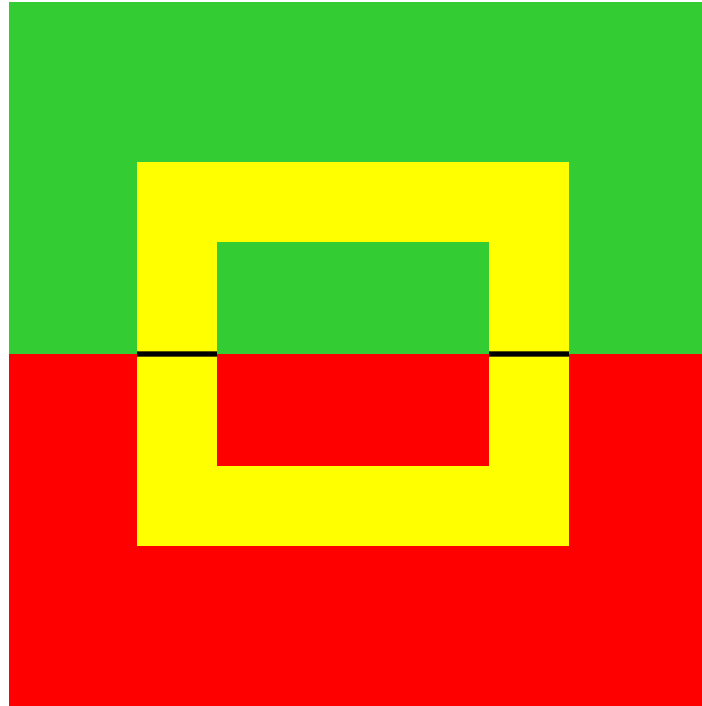
$$u = \frac{4x}{-2x + 12y + 3} \quad v = \frac{6y}{-2x + 12y + 3}$$



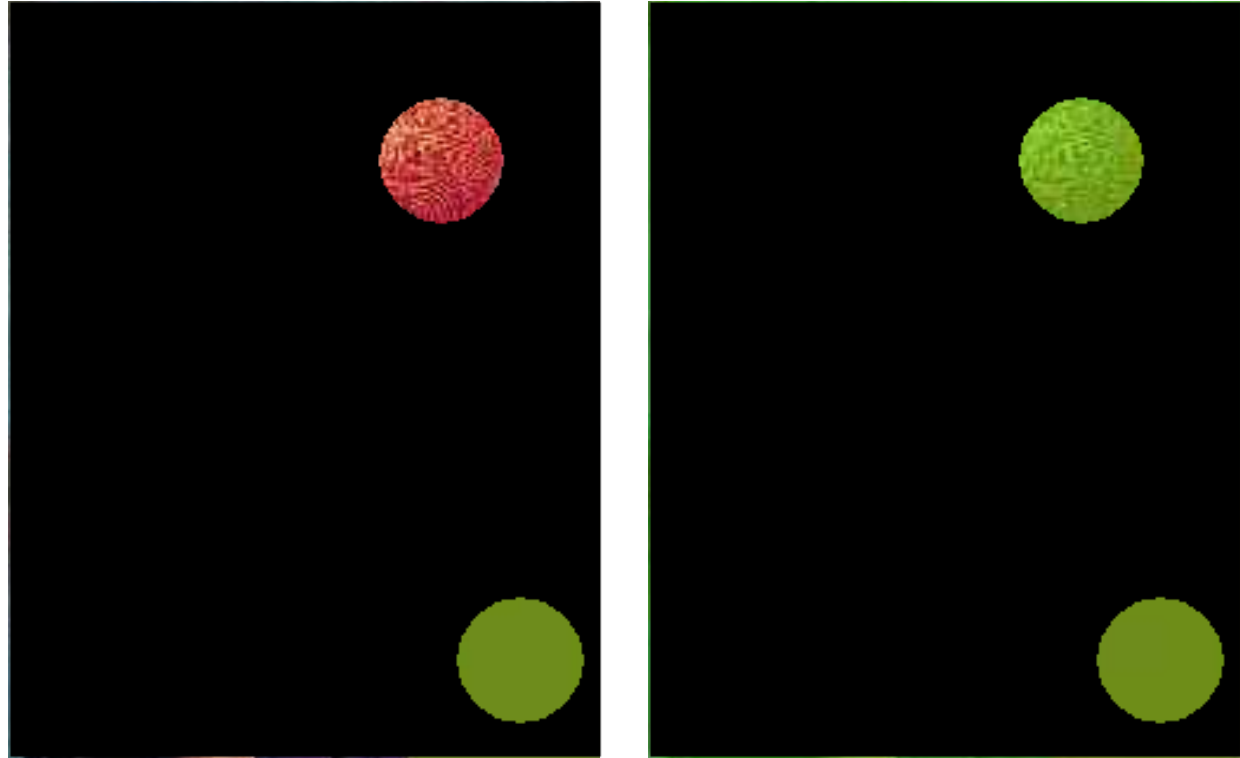
Using colour as a feature:

- colour constancy
- illumination invariant colour features

Koffka ring with colours



Colour constancy



Colour constancy

Patches keep their colour appearance even if they reflect differently (e.g. the hat)

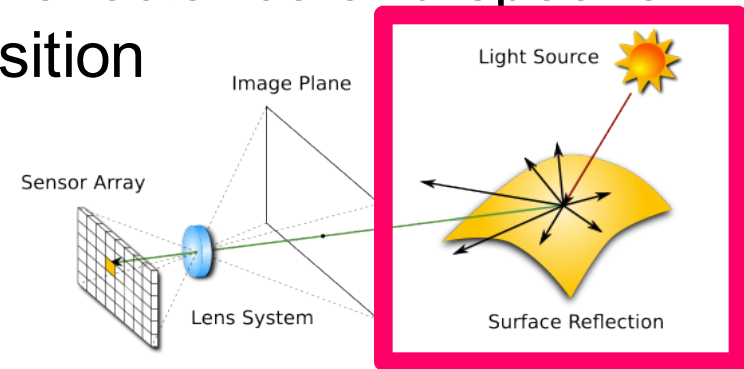
Patches change their colour appearance if they reflect identically but surrounding patches reflect differently (e.g. the background)

There is more to colour perception than 3 cone responses

Edwin Land performed in-depth experiments (psychophysics)

Colour constancy - notes

The colour of a surface is the result of the product of spectral reflectance and spectral light source composition



Our visual system can from a single product determine the two factors, it seems

The colour of the light source can be guessed via that of specular reflections, but the visual system does not critically depend on this trick

On the menu:

- colour constancy
- illumination invariant colour features

Illumination invariant colour features

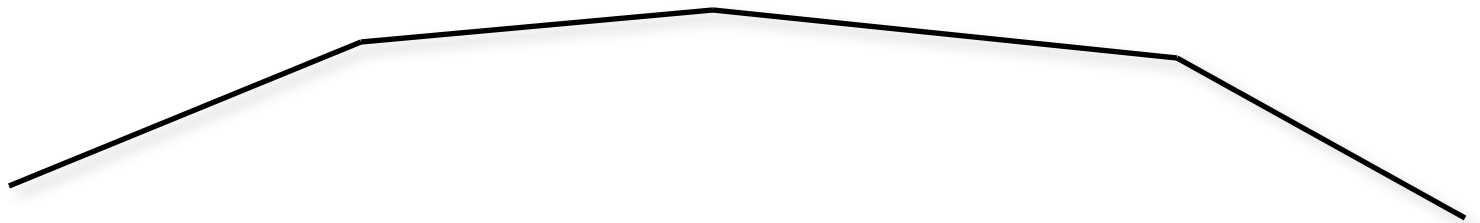
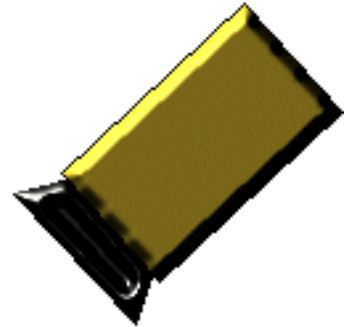
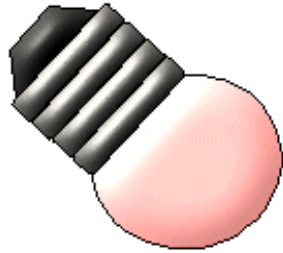
Extracting the true surface colour under varying illumination - as the HVS can - is very difficult

A less ambitious goal is to extract colour features that do not change with illumination

- 1) Spectral or 'internal' changes
- 2) Geometric or 'external' changes
- 3) Spectral + geometric changes

Illumination invariant colour features

1) Spectral changes



Illumination invariant colour features

1) Spectral changes

Let I_R, I_G, I_B represent the irradiances at the camera for red, green, blue

A simple model: the irradiances change by

$$\alpha, \beta, \gamma : (I'_R, I'_G, I'_B) = (\alpha I_R, \beta I_G, \gamma I_B)$$

Consider irradiances at 2 points:

$$I_{R1}, I_{G1}, I_{B1} \text{ and } I_{R2}, I_{G2}, I_{B2}$$

$$I'_{R1} / I'_{R2} = (\alpha I_{R1}) / (\alpha I_{R2}) = I_{R1} / I_{R2}$$

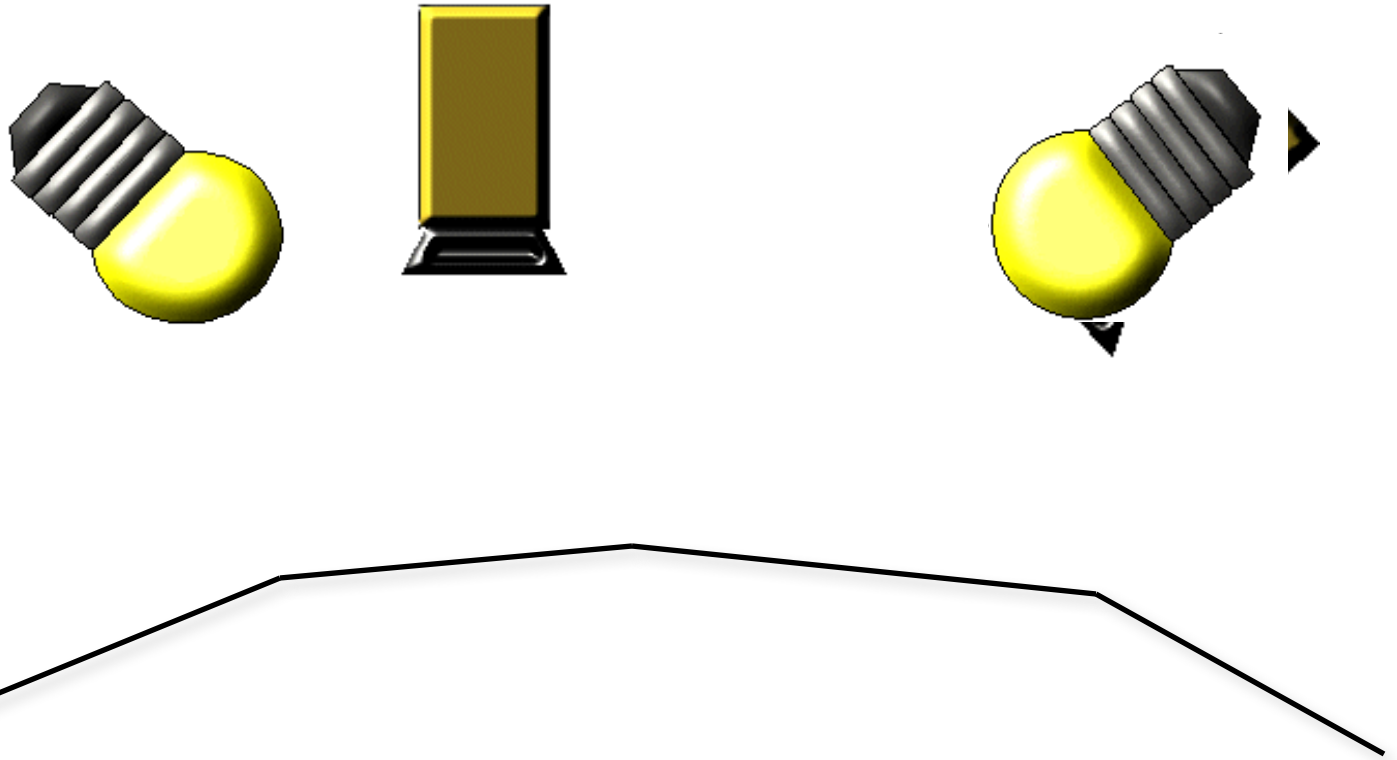
Illumination invariant colour features

For a camera with a non-linear response:

$$(\alpha I_{R1})^\gamma / (\alpha I_{R2})^\gamma = (I_{R1})^\gamma / (I_{R2})^\gamma$$

Illumination invariant colour features

2) Geometric changes



Illumination invariant colour features

1) Geometric changes

$$(I'_R, I'_G, I'_B) = (s(x, y)I_R, s(x, y)I_G, s(x, y)I_B)$$

$$I'_R / I'_G = I_R / I_G$$

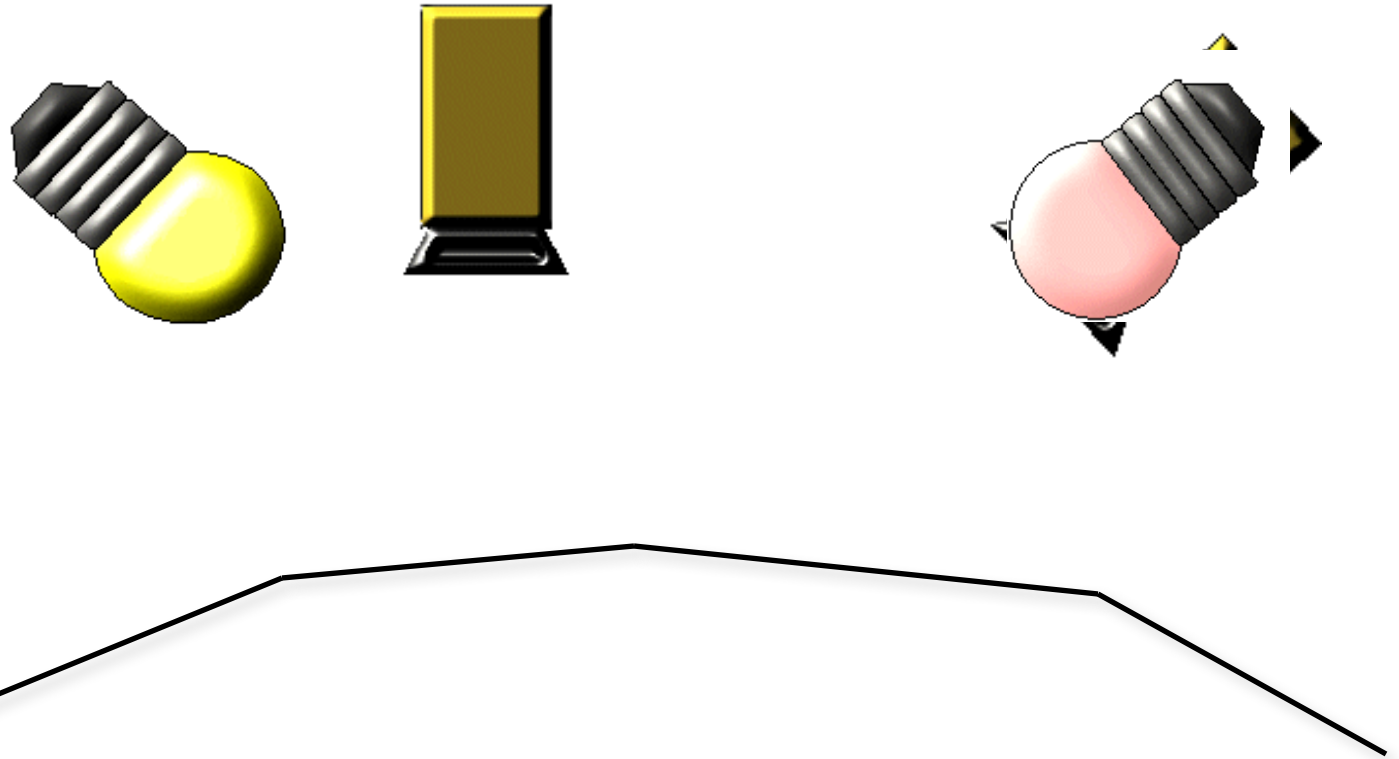
and

$$I'_R / I'_B = I_R / I_B$$

are invariant

Illumination invariant colour features

3) Spectral + geometric changes



Illumination invariant colour features

3) Geometric + spectral changes

$$\frac{I'_{R1} I'_{G2}}{I'_{R2} I'_{G1}} = \frac{\alpha s(x_1, y_1) I_{R1} \beta s(x_2, y_2) I_{G2}}{\alpha s(x_2, y_2) I_{R2} \beta s(x_1, y_1) I_{G1}} = \frac{I_{R1} I_{G2}}{I_{R2} I_{G1}}$$

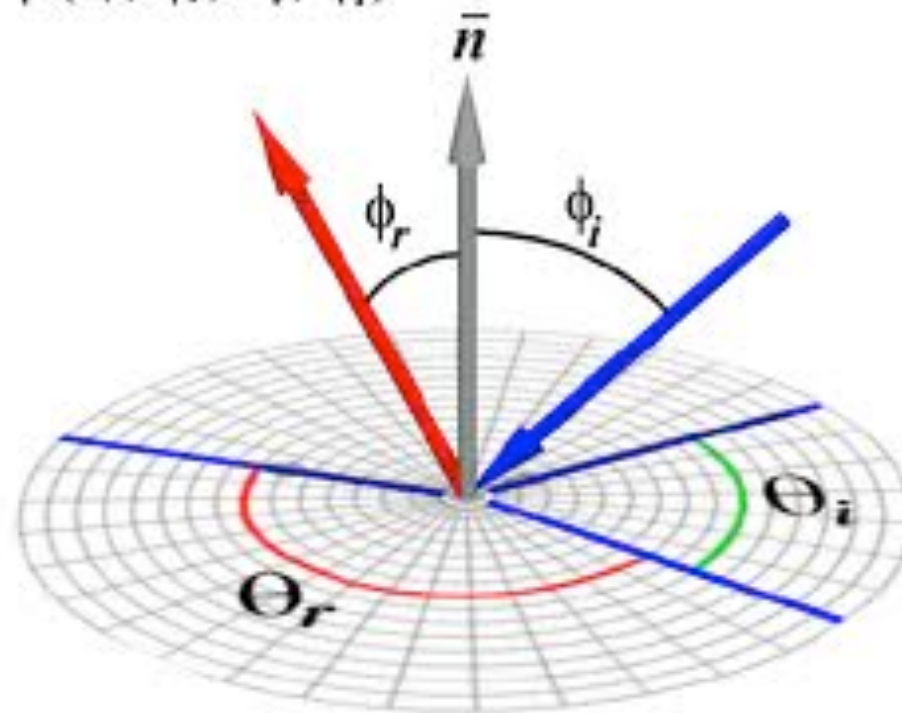
for points on both sides of a colour edge

$s(x_1, y_2) \cong s(x_2, y_2)$ and hence I_{R1} / I_{R2}
is invariant

The elusive BRDF

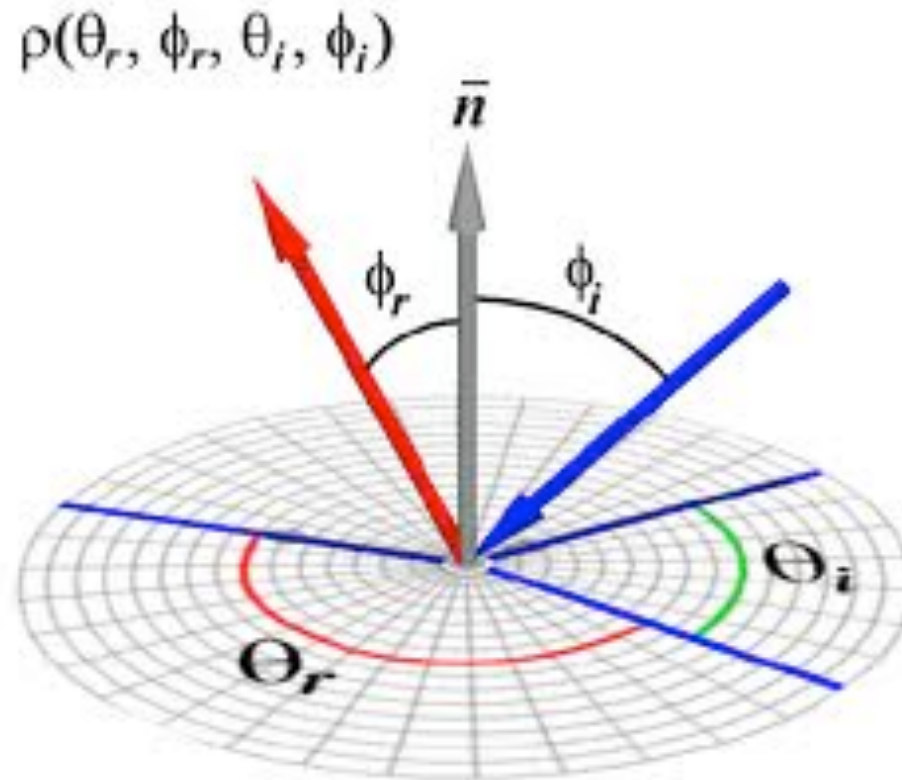
Bidirectional Reflection Distribution Function
.... for different wavelengths

$$\rho(\theta_r, \phi_r, \theta_i, \phi_i)$$



The elusive BRDF

A 4D function, specifying the radiance for an outgoing direction given an irradiance for an incoming direction, relative to the normal and ideally for 1 wavelength at a time



Mini-dome to study reflectance

KATHOLIEKE UNIVERSITEIT
LEUVEN

Mini-dome to study reflectance



Mini-dome to study reflectance



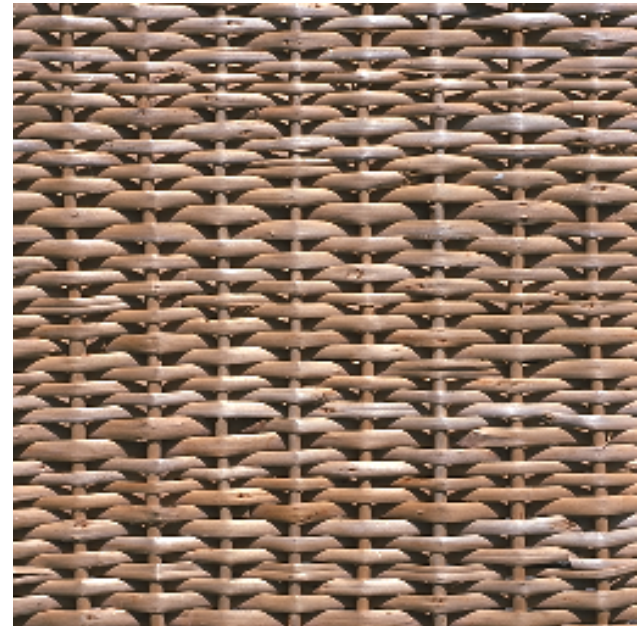
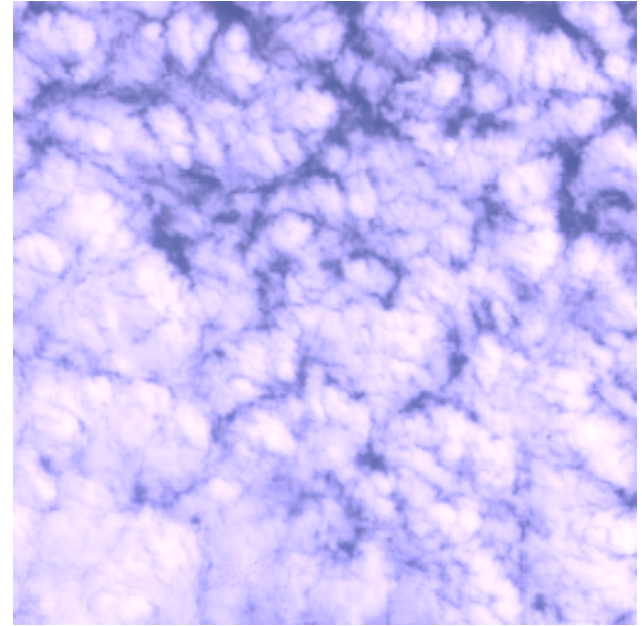
REAL

SIMULATED

TEXTURE

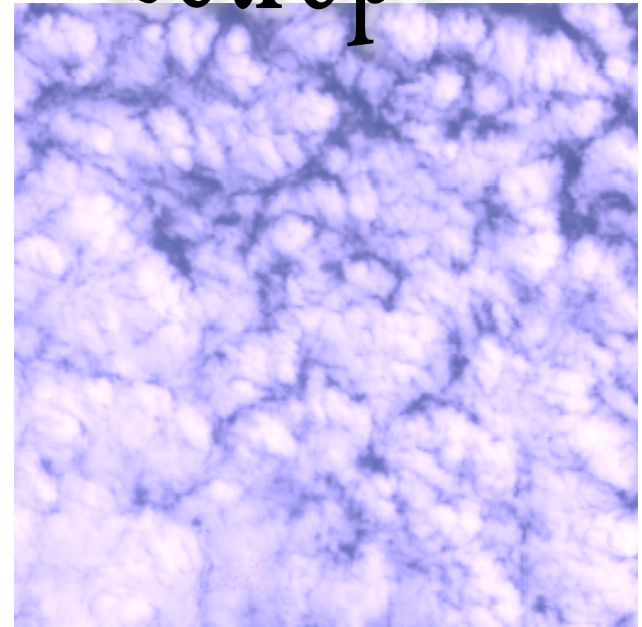
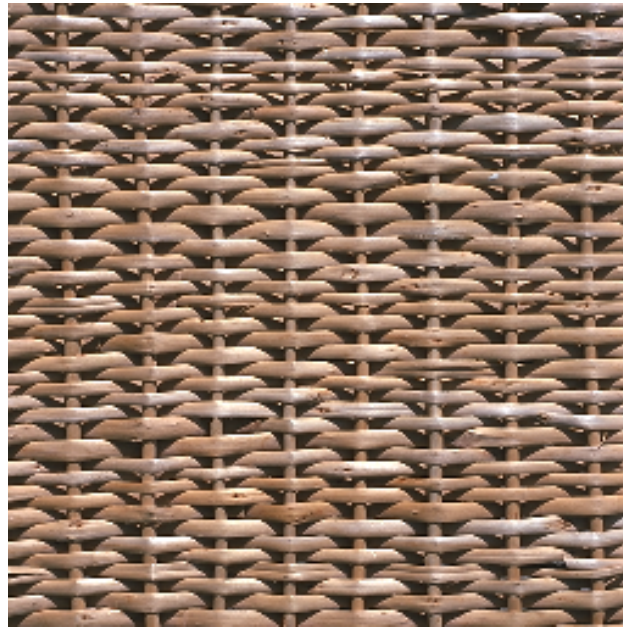
The word "TEXTURE" is rendered in a 3D, blocky font. Each letter is filled with a brown, crumpled paper texture. The letters have a dark green top surface and a dark green bottom surface, creating a strong sense of depth and shadow. The text is positioned on a white background, with a blue vertical bar on the left side of the image.

Example textures



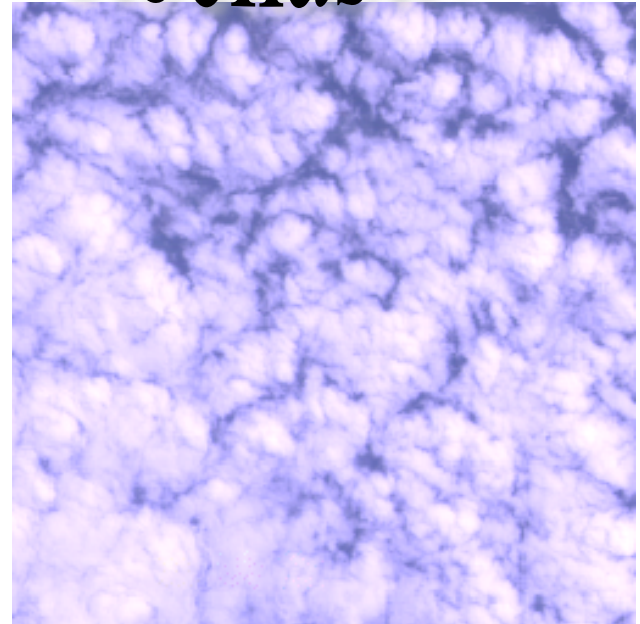
Texture characteristics

oriented vs. isotropic



Texture characteristics

regular vs. stochastic



Texture characteristics

coarse vs. fine



On the menu:

- Fourier features
- cooccurrence matrices
- filter banks (Laws, Gabor, eigenfilters)
- stochastic models)

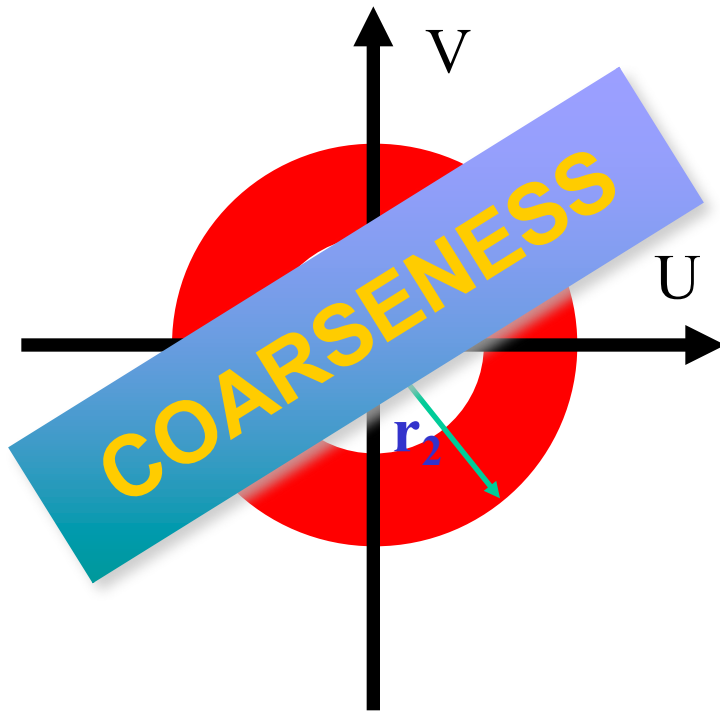
Fourier features

Based on the integration of regions of the Fourier power spectrum $\int_A \int |F(u, v)|^2 dudv$

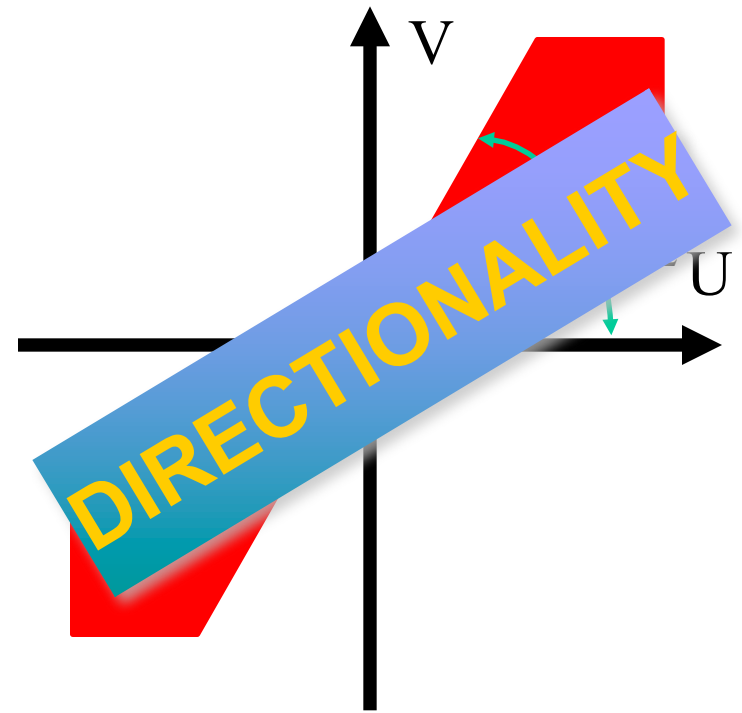
Intuitively appealing

- peaks if periodic
- mostly low/high freq. if coarse resp. fine
- the sine patterns each have an orientation

Fourier features



$$r_1^2 \leq u^2 + v^2 < r_2^2$$



$$\theta_1 \leq \arctan\left(\frac{u}{v}\right) < \theta_2$$

Fourier features

THE FOURIER TRANSFORM COLLECTS
INFORMATION GLOBALLY OVER THE
ENTIRE IMAGE

NOT GOOD FOR SEGMENTATION OR
INSPECTION

On the menu:

- Fourier features
- cooccurrence matrices
- filter banks (Laws, Gabor, eigenfilters)
- stochastic models

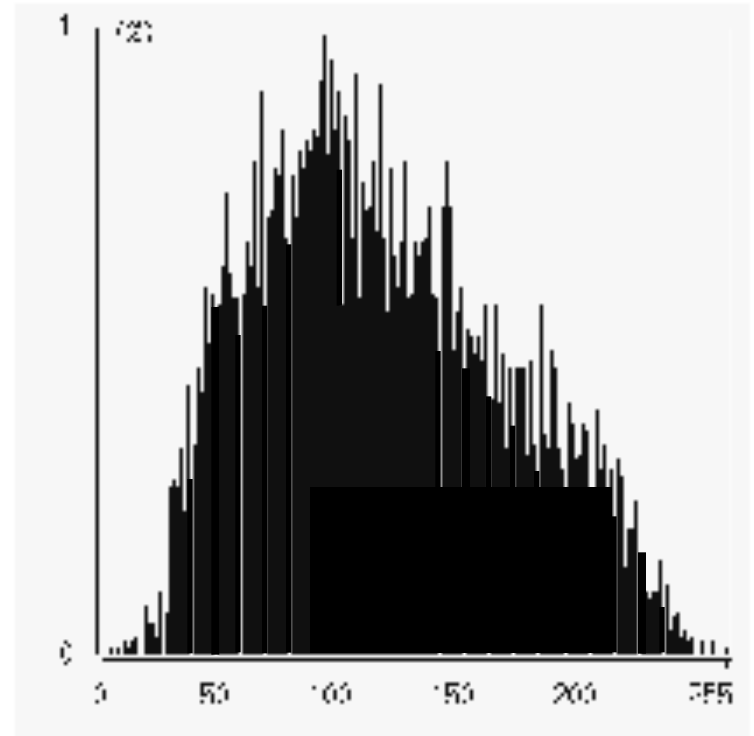
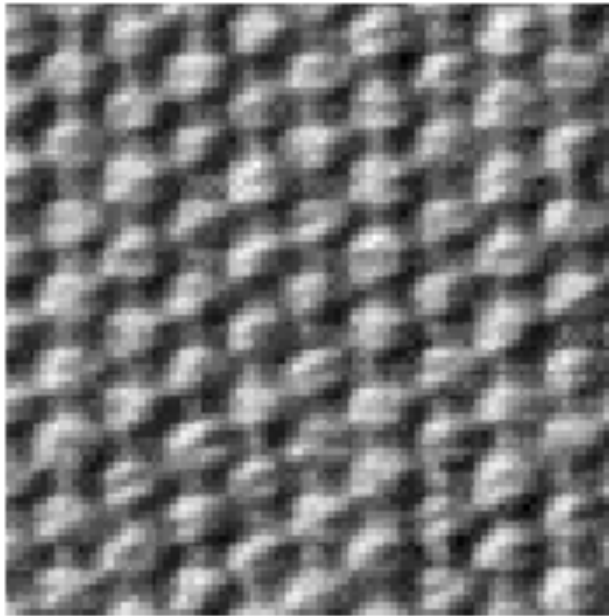
Histograms: principle

Intensity probability distribution

Captures global brightness information in a compact, but incomplete way

Doesn't capture spatial relationships

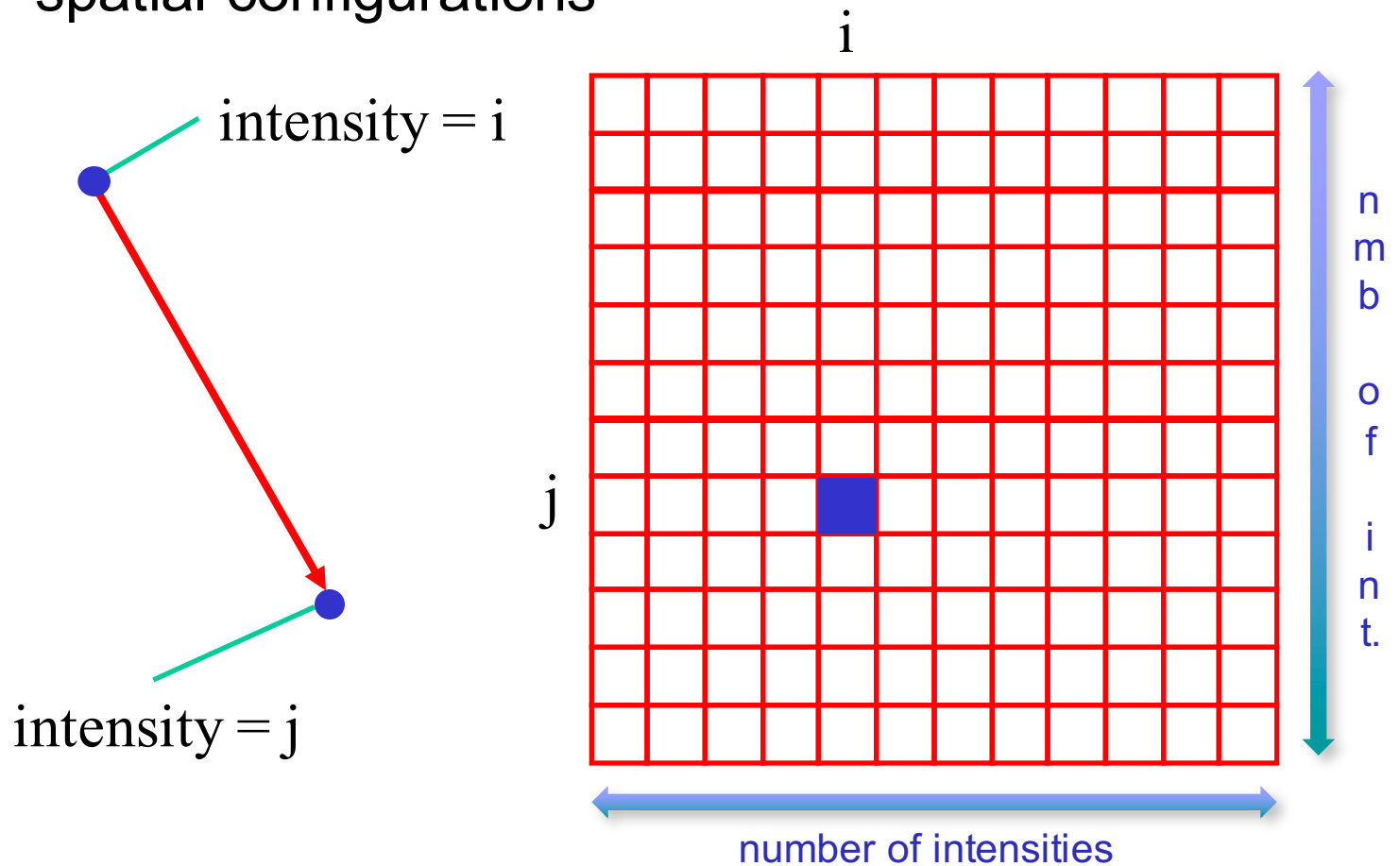
Histograms : example



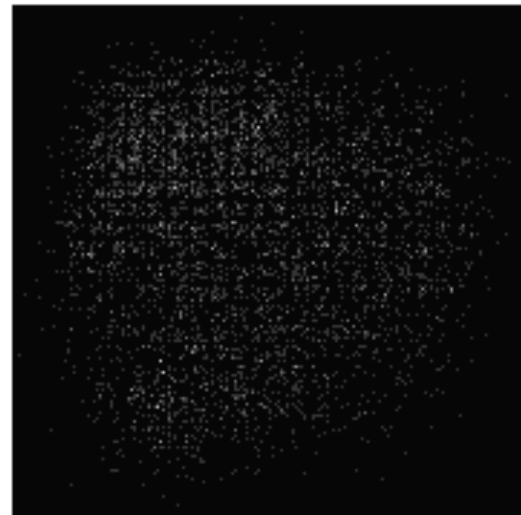
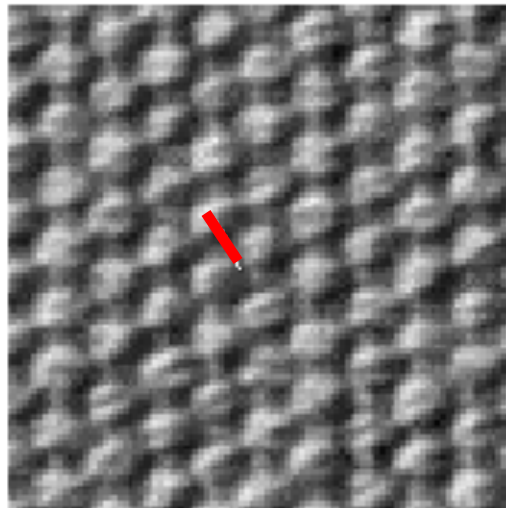
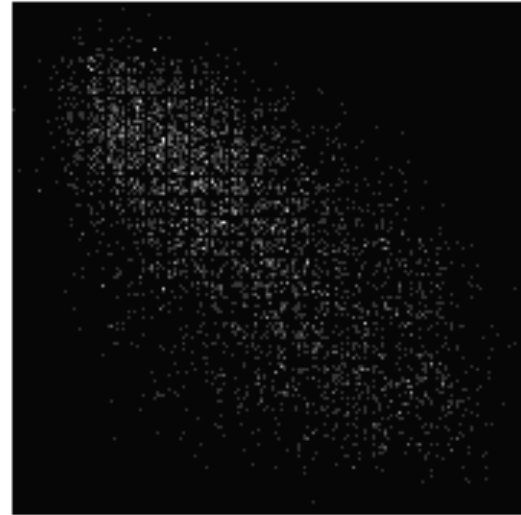
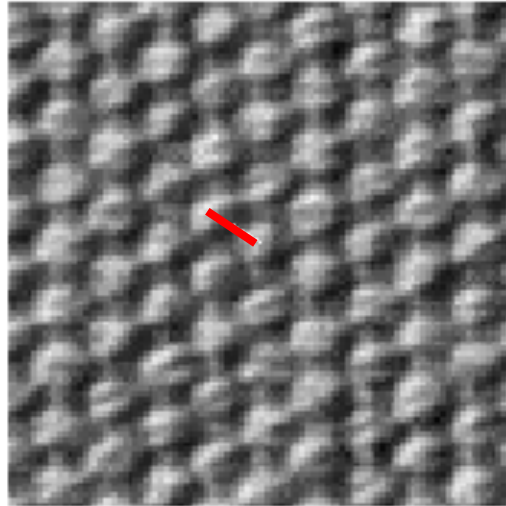
Cooccurrence matrix

probability distributions for intensity pairs

Contains information on some aspects of the spatial configurations



Cooccurrence matrix



Cooccurrence matrix

Features calculated from the matrix:

feature	expression
energy	$\sum_i \sum_j C^2(i, j)$
entropy	$-\sum_i \sum_j C(i, j) \log C(i, j)$
contrast	$\sum_i \sum_j (i - j)^2 C(i, j)$
homogeneity	$\sum_i \sum_j C(i, j) / (1 + i - j)$
max. probability	$\max_{i, j} C(i, j)$

On the menu:

- Fourier features
- cooccurrence matrices
- filter banks (Laws, Gabor, eigenfilters)
- stochastic models)

Feature	1D filter
L3	$[1 \ 2 \ 1]$
E3	$[-1 \ 0 \ 1]$
S3	$[-1 \ 2 \ -1]$
L5	$[1 \ 4 \ 6 \ 4 \ 1]$
E5	$[-1 \ -2 \ 0 \ 2 \ 1]$
S5	$[-1 \ 0 \ 2 \ 0 \ -1]$
W5	$[-1 \ 2 \ 0 \ -2 \ 1]$
R5	$[1 \ -4 \ 6 \ -4 \ 1]$
L7	$[1 \ 6 \ 15 \ 20 \ 15 \ 6 \ 1]$
E7	$[-1 \ -4 \ -5 \ 0 \ 5 \ 4 \ 1]$
S7	$[-1 \ -2 \ 1 \ 4 \ 1 \ -2 \ -1]$
W7	$[-1 \ 0 \ 3 \ 0 \ -3 \ 0 \ 1]$
R7	$[1 \ -2 \ -1 \ 4 \ -1 \ -2 \ 1]$
O7	$[-1 \ 6 \ -15 \ 20 \ -15 \ 6 \ -1]$

L
a
w
S
f
i
l
t
e
r
s

Laws filters

This fixed filter set yields simple convolutions but has proven very effective in some cases

Gabor filters

Gaussian envelope multiplied by cosine

$$g(x, y) = e^{-\frac{x^2 + y^2}{4\Delta_{x,y}^2}} \cos(2\pi u^* x + \varphi)$$

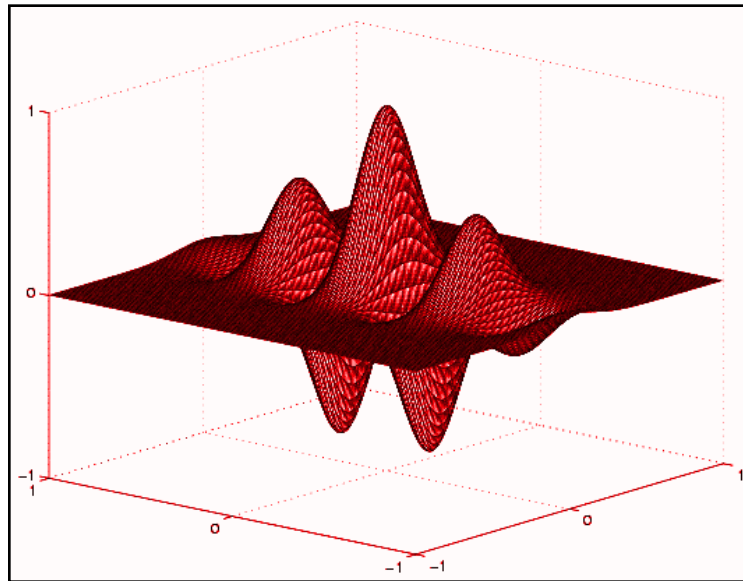
The filter's Fourier power spectrum

$$G(u, v) =$$

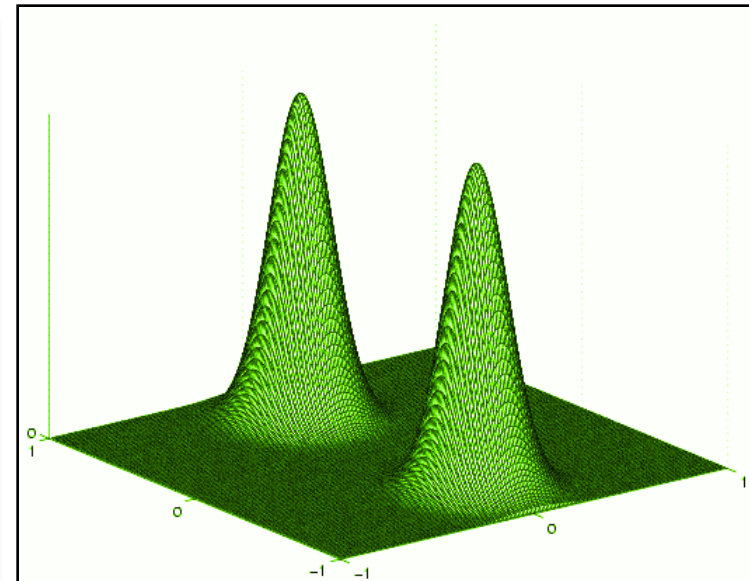
$$\frac{1}{4\pi\Delta_{u,v}^2} \left(e^{-((u-u^*)^2 + v^2)/(4\Delta_{u,v}^2)} + e^{-((u+u^*)^2 + v^2)/(4\Delta_{u,v}^2)} \right)$$

Gabor filters

Spatial domain



Frequency domain



Good localisation in both domains

Gabor filters

$$f = f(x, y)$$

$$F = F(u, v)$$

$$x_{av} = \frac{\int_{-\infty}^{\infty} x f \bar{f} dx}{\int_{-\infty}^{\infty} f \bar{f} dx}$$

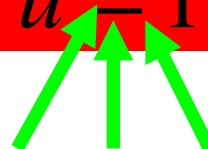
$$u_{av} = \frac{\int_{-\infty}^{\infty} u F \bar{F} du}{\int_{-\infty}^{\infty} F \bar{F} du}$$

$$(\Delta x)^2 = \frac{\int_{-\infty}^{\infty} (x - x_{av})^2 f \bar{f} dx}{\int_{-\infty}^{\infty} f \bar{f} dx}$$

$$(\Delta u)^2 = \frac{\int_{-\infty}^{\infty} (u - u_{av})^2 F \bar{F} du}{\int_{-\infty}^{\infty} F \bar{F} du}$$

the Heisenberg uncertainty principle

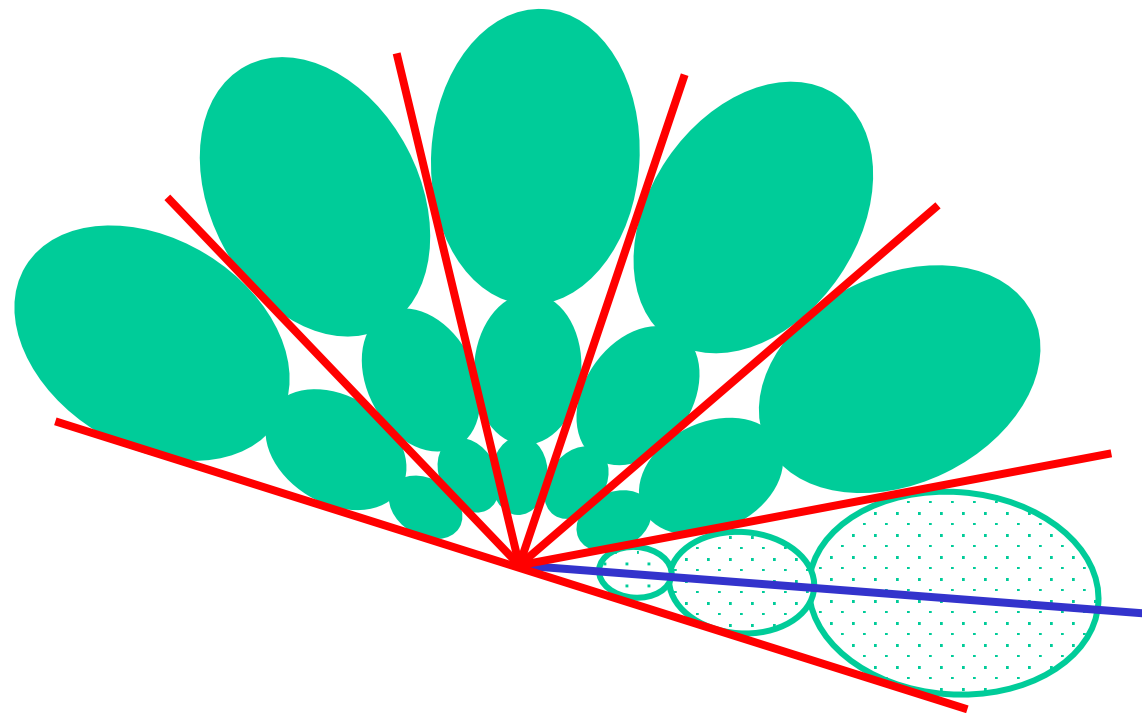
$$\Delta x \Delta u = 1 / 4\pi$$



Gabor filters

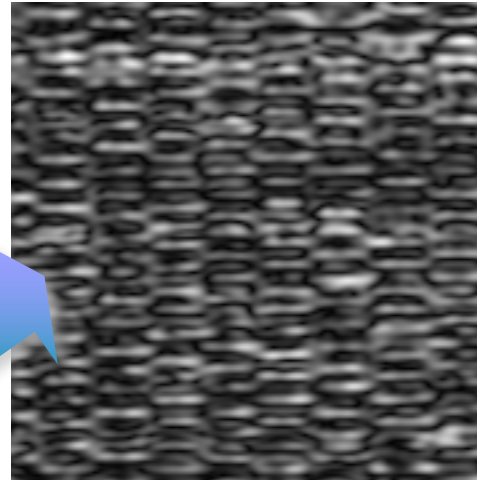
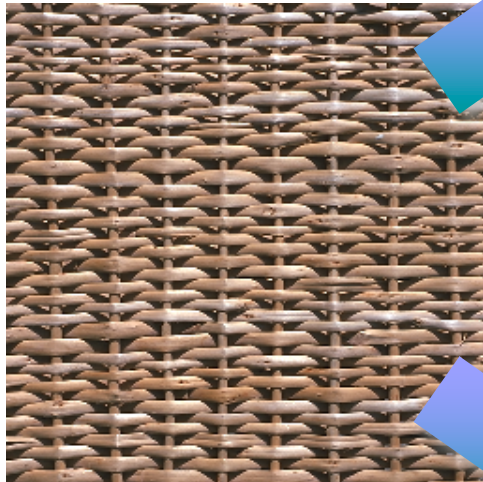
Covering the Fourier domain with responses

- to probe for directionality
- to look at different scales

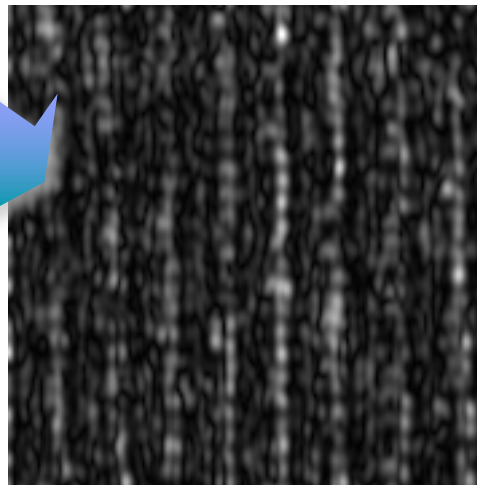


Gabor filters

Input texture



Output for filter
responsive to
horizontal
structures



Output for filter
responsive to
vertical
structures

Eigenfilters (Ade, ETH)

Filters adapted to the texture

- 1) shift mask over training image
- 2) collect intensity statistics
- 3) PCA -> eigenvectors -> 'eigenfilters'
- 4) energies of eigenfilter outputs

Eigenfilters

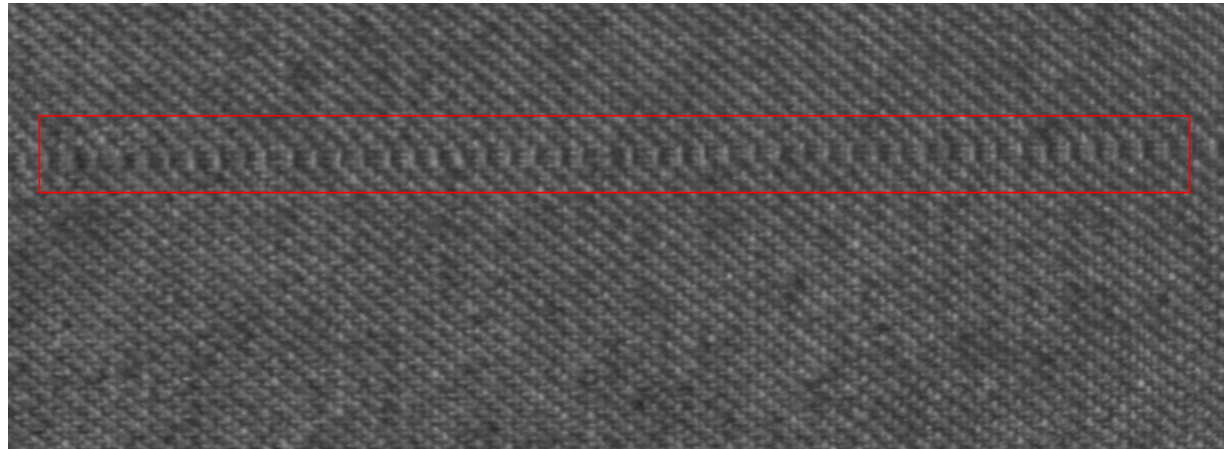
Filters adapted to the texture

but small filters may reduce efficacy

hence large, but sparse filters

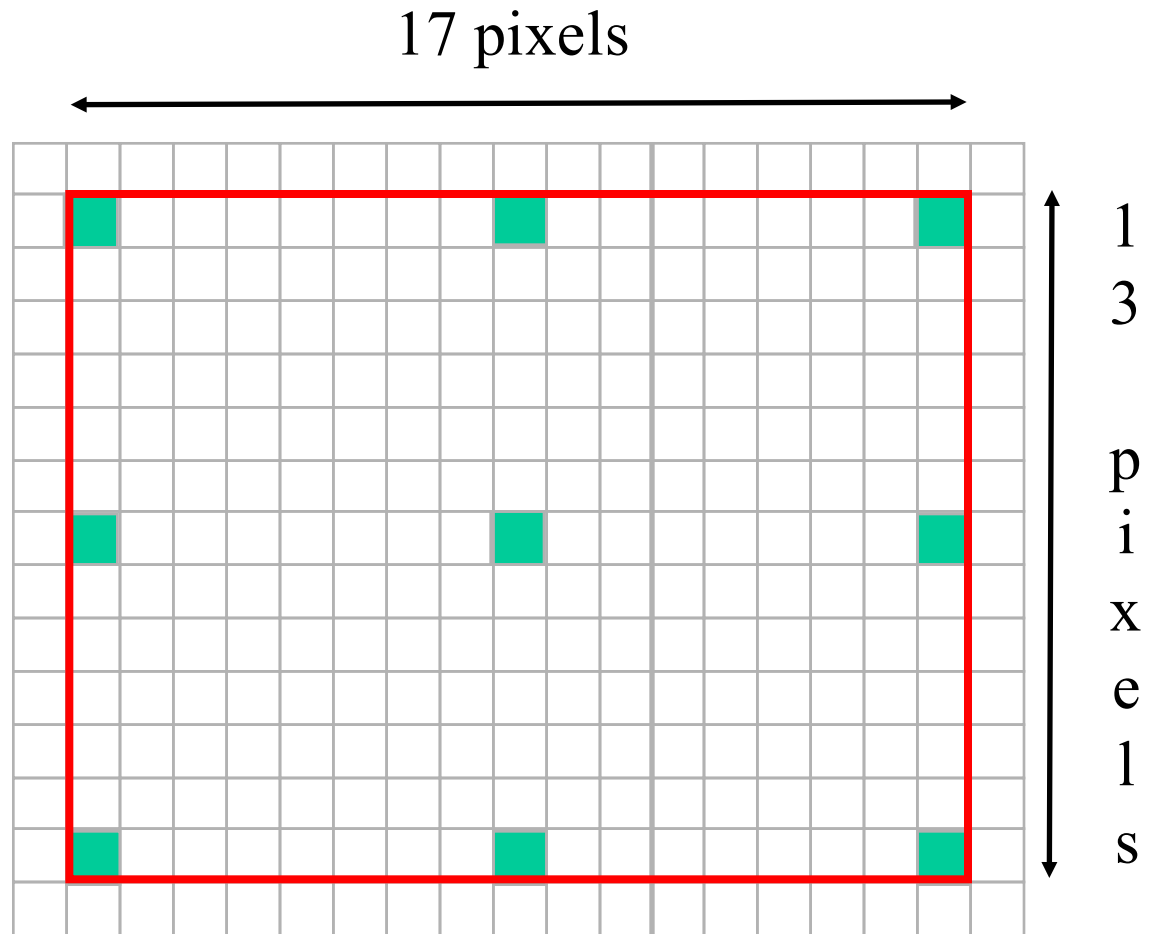
Eigenfilters

Example applications: textile inspection



Filters with size of one period
(period found as peak in autocorrelation)

Eigenfilters



Eigenfilters

Covariance matrix needed for PCA

$$\begin{pmatrix} 174.1 & -77.6 & 101.6 & -60.8 & 72.7 & -71.5 & 116.5 & -77.9 & 91.4 \\ -77.6 & 173.9 & -78.2 & 71.5 & -61.7 & 73.1 & -76.4 & 116.4 & -78.4 \\ 101.6 & -78.2 & 173.5 & -70.4 & 71.7 & -62.1 & 95.3 & -77.0 & 116.3 \\ -60.8 & 71.5 & -70.4 & 173.9 & -76.5 & 101.0 & -59.4 & 71.8 & -70.1 \\ 72.7 & -61.7 & 71.7 & -76.5 & 173.7 & -77.1 & 70.6 & -60.3 & 72.1 \\ -71.5 & 73.1 & -62.1 & 101.0 & -77.1 & 173.4 & -69.3 & 70.9 & -60.7 \\ 116.5 & -76.4 & 95.3 & -59.4 & 70.6 & -69.3 & 173.4 & -75.3 & 99.8 \\ -77.9 & 116.4 & -77.0 & 71.8 & -60.3 & 70.9 & -75.3 & 173.2 & -75.9 \\ 91.4 & -78.4 & 116.3 & -70.1 & 72.1 & -60.7 & 99.8 & -75.9 & 172.8 \end{pmatrix}$$

Eigenfilters

$$\begin{pmatrix} 0.35 \\ -0.33 \\ 0.35 \\ -0.30 \\ 0.30 \\ -0.30 \\ 0.35 \\ -0.33 \\ 0.35 \end{pmatrix}$$

$$\begin{pmatrix} 0.31 \\ 0.12 \\ 0.31 \\ 0.51 \\ -0.20 \\ 0.49 \\ 0.34 \\ 0.12 \\ 0.31 \end{pmatrix}$$

$$\begin{pmatrix} 0.10 \\ 0.58 \\ 0.10 \\ -0.19 \\ 0.41 \\ -0.19 \\ 0.11 \\ 0.59 \\ 0.09 \end{pmatrix}$$

$$\begin{pmatrix} 0.46 \\ -0.00 \\ -0.43 \\ 0.30 \\ 0.03 \\ -0.28 \\ 0.41 \\ -0.02 \\ -0.49 \end{pmatrix}$$

$$\begin{pmatrix} -0.10 \\ -0.15 \\ -0.09 \\ 0.33 \\ 0.83 \\ 0.33 \\ -0.13 \\ -0.14 \\ -0.06 \end{pmatrix}$$

$$\begin{pmatrix} 0.27 \\ 0.11 \\ -0.11 \\ -0.62 \\ 0.00 \\ 0.63 \\ 0.11 \\ -0.12 \\ -0.27 \end{pmatrix}$$

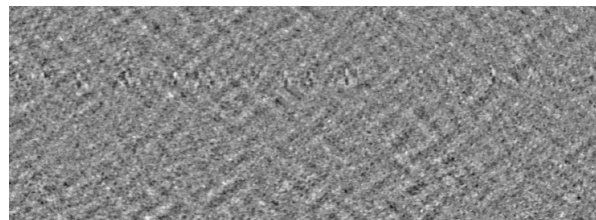
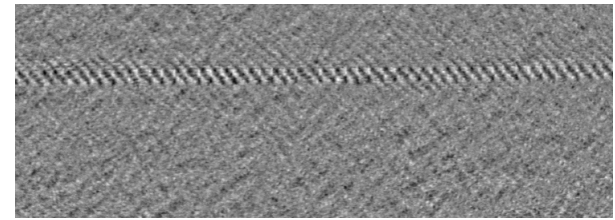
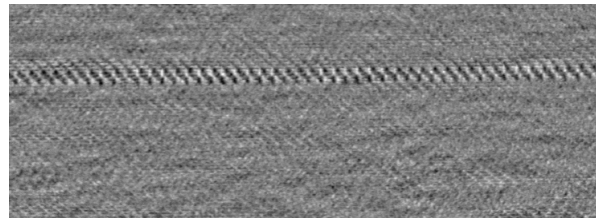
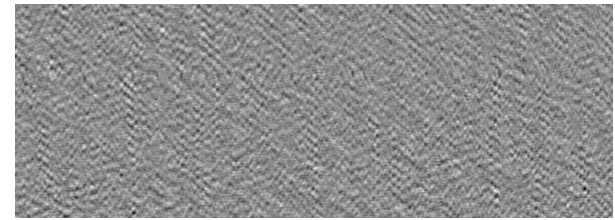
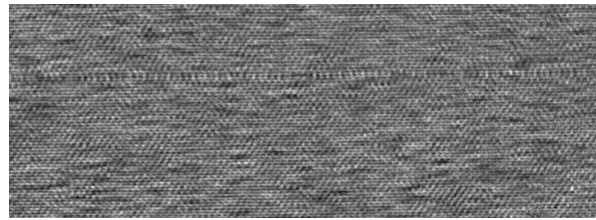
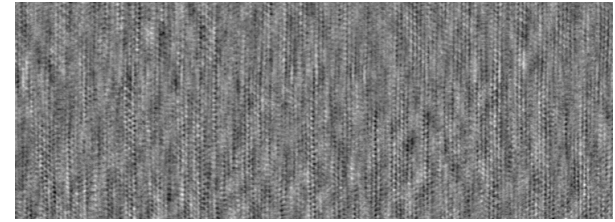
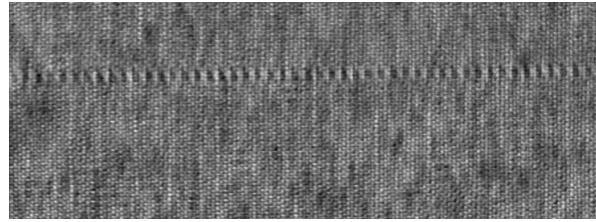
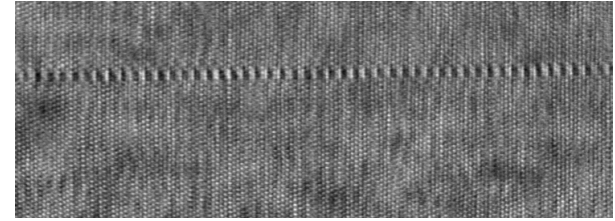
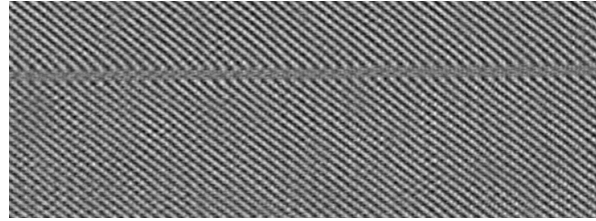
$$\begin{pmatrix} -0.43 \\ -0.06 \\ -0.54 \\ -0.10 \\ 0.00 \\ 0.09 \\ 0.55 \\ 0.05 \\ 0.40 \end{pmatrix}$$

$$\begin{pmatrix} 0.08 \\ -0.69 \\ 0.02 \\ -0.09 \\ -0.00 \\ 0.10 \\ -0.02 \\ 0.69 \\ -0.09 \end{pmatrix}$$

$$\begin{pmatrix} -0.50 \\ -0.00 \\ 0.50 \\ 0.00 \\ 0.02 \\ 0.00 \\ 0.47 \\ -0.01 \\ -0.50 \end{pmatrix}$$

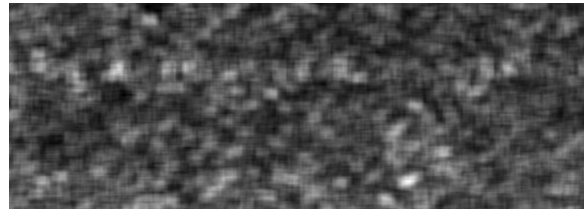
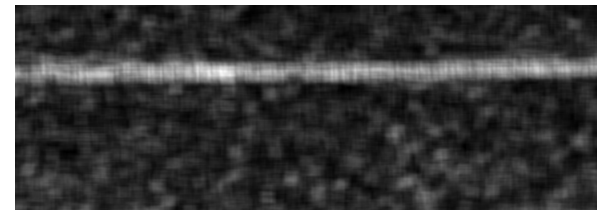
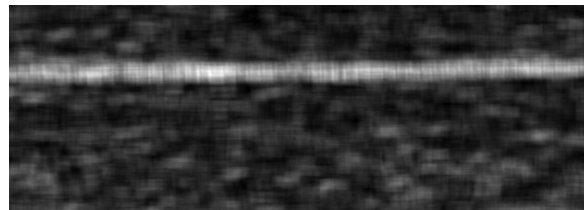
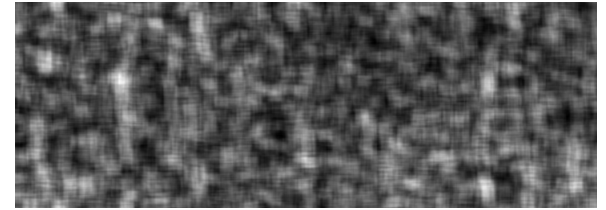
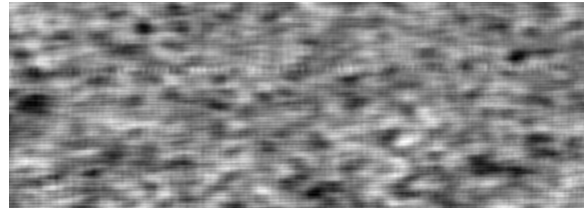
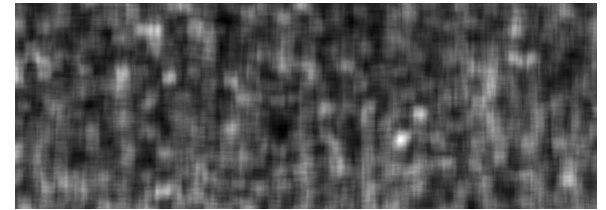
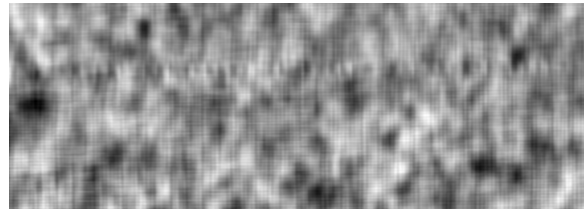
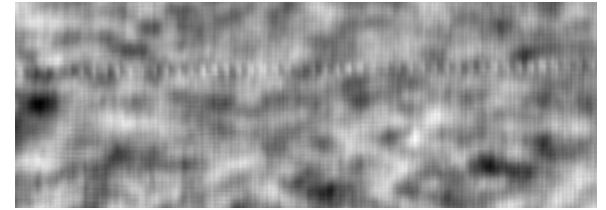
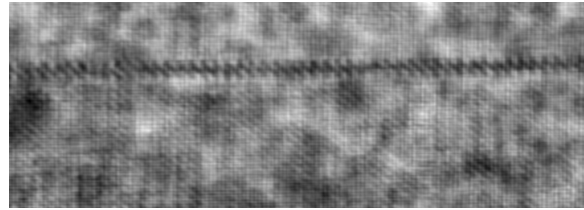
Eigenfilters

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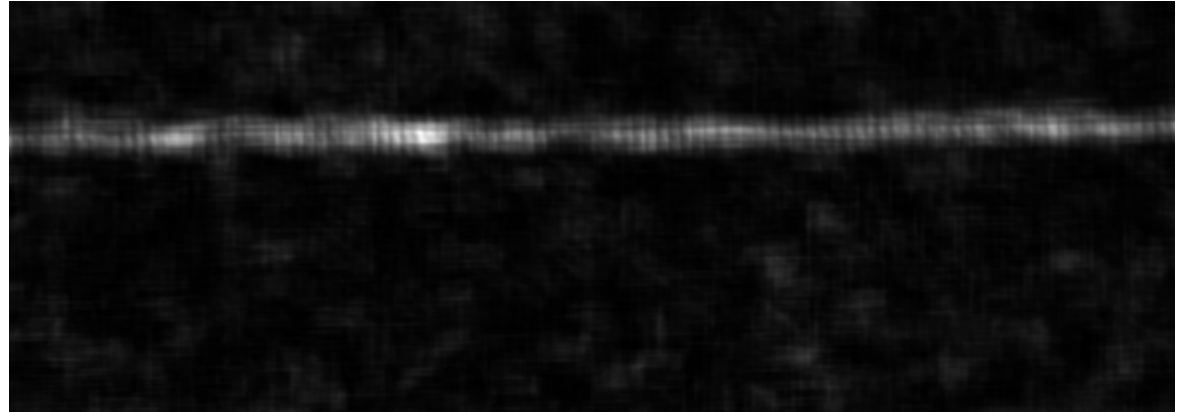
Eigenfilters

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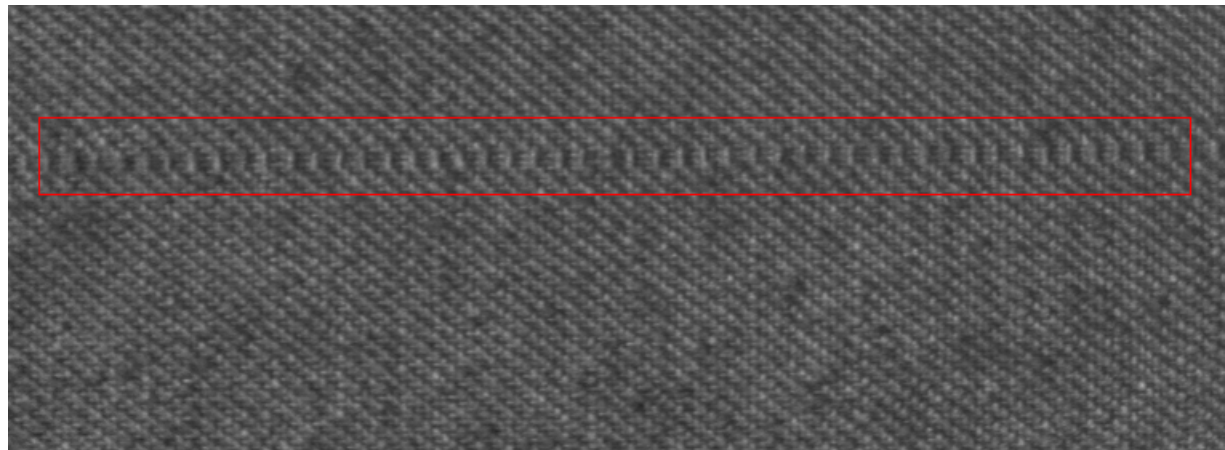


Eigenfilters

Mahalanobis distance of the energies:

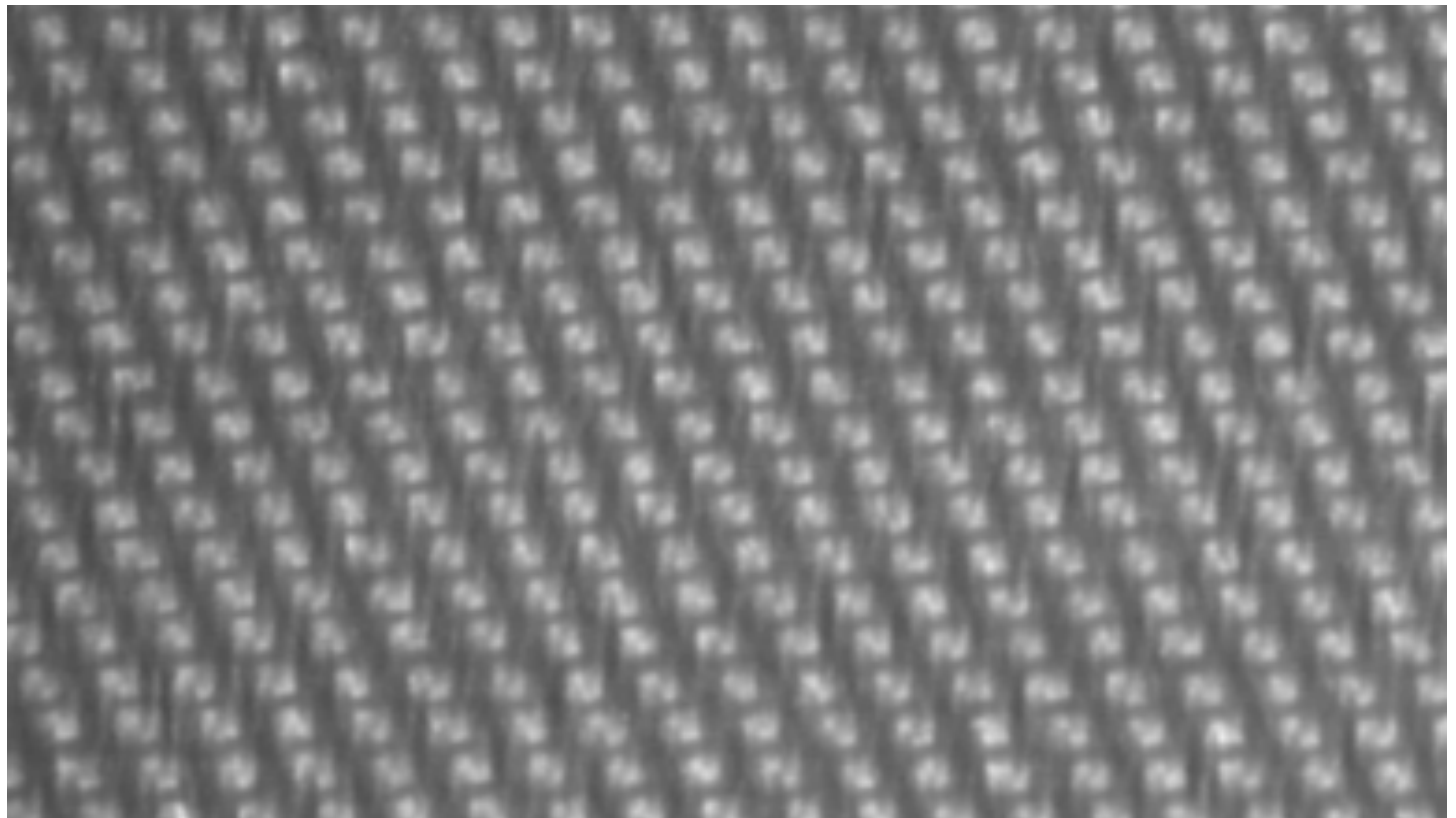


Flaw region found by thresholding:



Eigenfilters

Textile inspection: a second example



The texture is coarser, the filters are larger...

Eigenfilters

Textile inspection: eigenfilter blueprint

1	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
...
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	1
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
...
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	1

47 rows

21 columns

The covariance matrix

Covariance Matrix :

743,89	-331,82	632,59	-316,03	618,47	-298,31	632,41	-302,50	548,84
-331,82	741,71	-345,42	641,76	-330,40	614,36	-334,25	629,22	-316,68
632,59	-345,42	738,28	-338,50	638,50	-343,03	618,37	-347,55	624,75
-316,03	641,76	-338,50	746,54	-328,93	634,29	-314,59	619,83	-297,11
618,47	-330,40	638,50	-328,93	743,82	-343,16	643,10	-329,00	615,32
-298,31	614,36	-343,03	634,29	-343,16	739,56	-337,44	639,40	-342,03
632,41	-334,25	618,37	-314,59	643,10	-337,44	748,53	-328,18	636,26
-302,50	629,22	-347,55	619,83	-329,00	639,40	-328,18	745,57	-342,19
548,84	-316,68	624,75	-297,11	615,32	-342,03	636,26	-342,19	741,04

Eigenfilters

Eigenvectors / eigenvalues

Eigenvalues :

4428,70	1432,36	215,64	126,57	126,19	113,86	98,41	85,21	62,01
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Eigenvectors :

0,337	0,292	-0,621	-0,121	0,119	-0,319	-0,229	0,040	-0,480
-0,317	0,382	0,225	0,273	-0,369	-0,465	-0,302	-0,429	-0,025
0,353	0,271	-0,055	-0,434	-0,536	0,069	-0,179	0,155	0,513
-0,314	0,400	0,240	-0,294	0,259	-0,399	0,266	0,548	0,034
0,350	0,285	-0,005	0,404	-0,292	-0,005	0,734	-0,004	-0,096
-0,318	0,381	-0,234	-0,410	0,161	0,353	0,295	-0,541	0,033
0,350	0,294	0,056	0,312	0,610	-0,056	-0,144	-0,163	0,518
-0,317	0,386	-0,219	0,421	-0,081	0,530	-0,261	0,412	-0,025
0,340	0,274	0,630	-0,173	0,079	0,330	-0,198	-0,046	-0,475

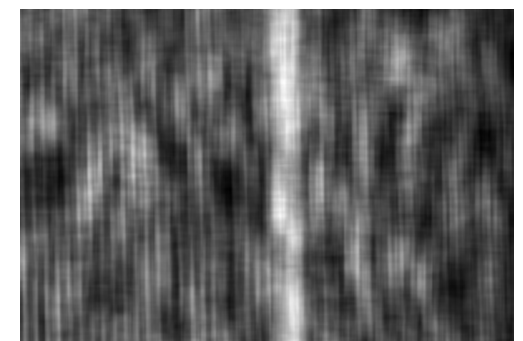
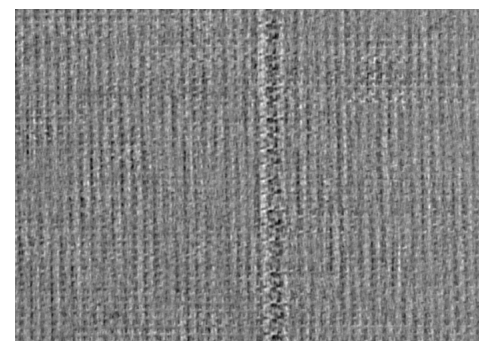
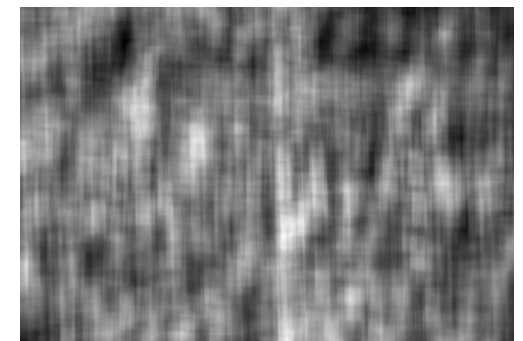
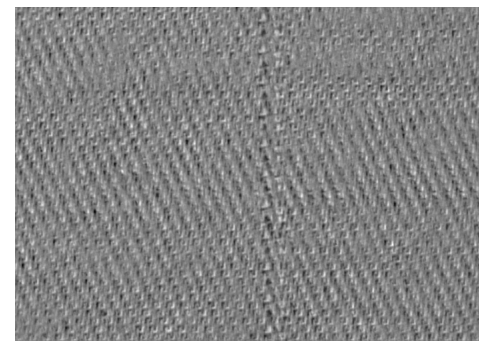
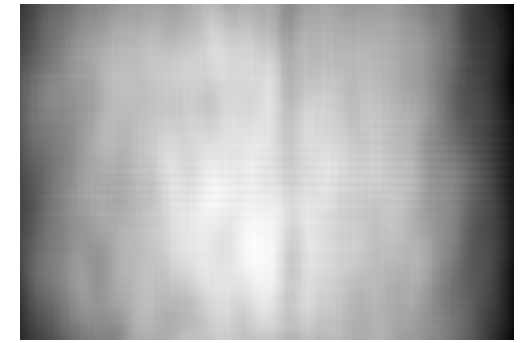
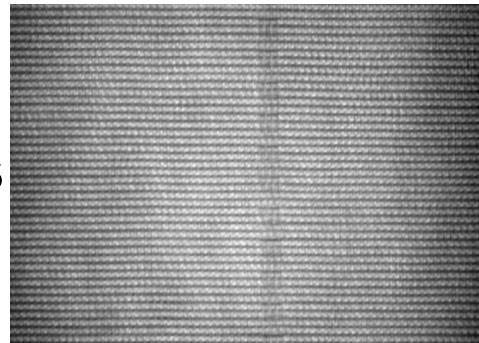
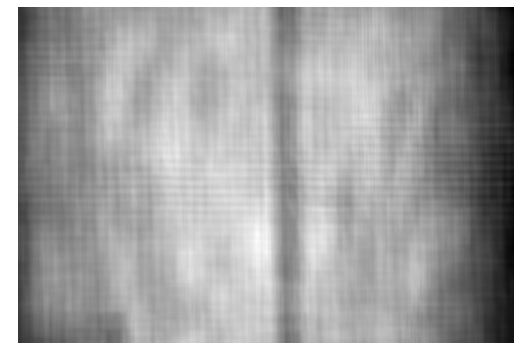
Eigenfilters

example of defect



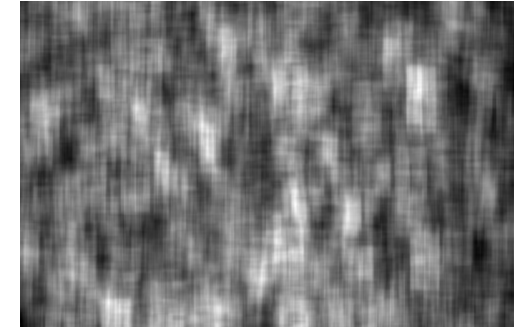
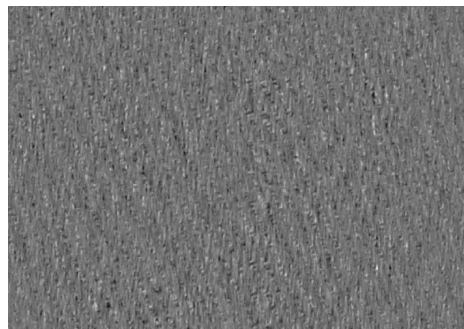
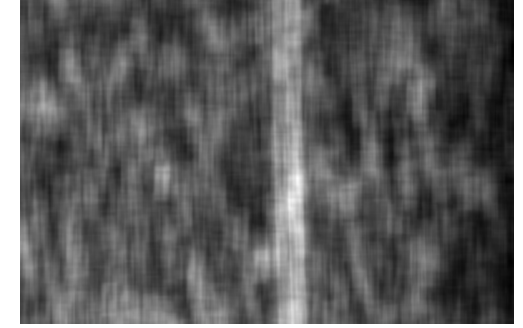
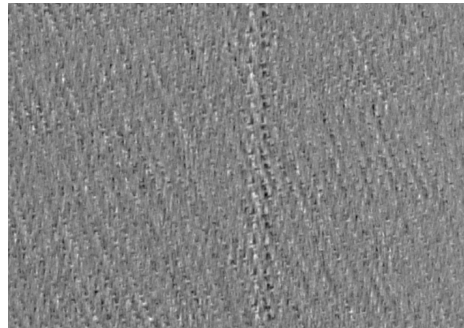
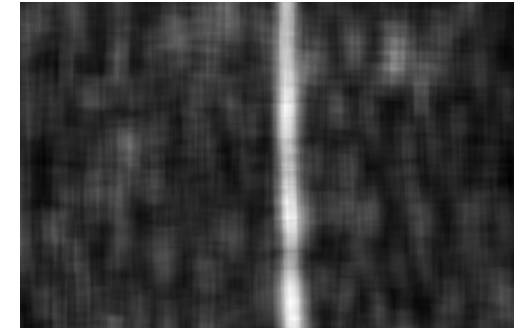
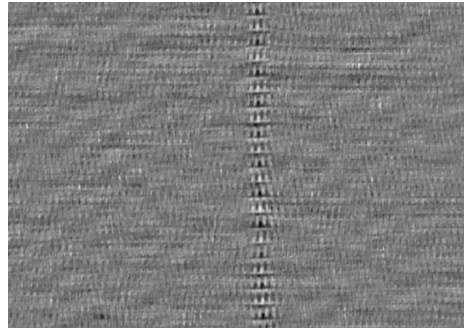
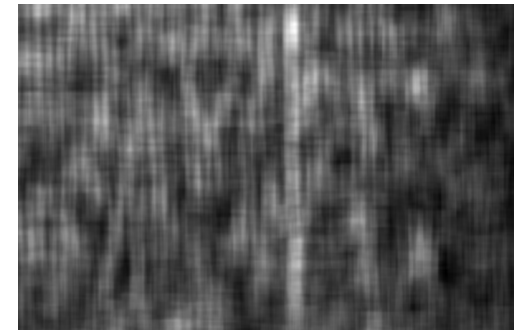
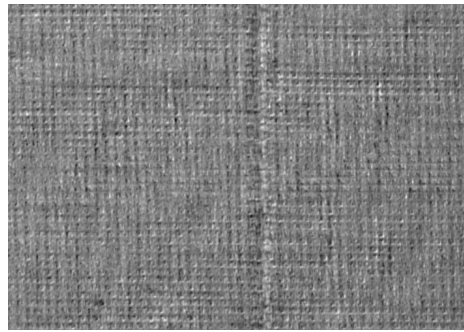
Eigenfilters

Outputs/energies
for the
4 largest
eigenvalues



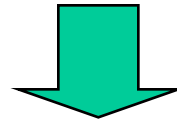
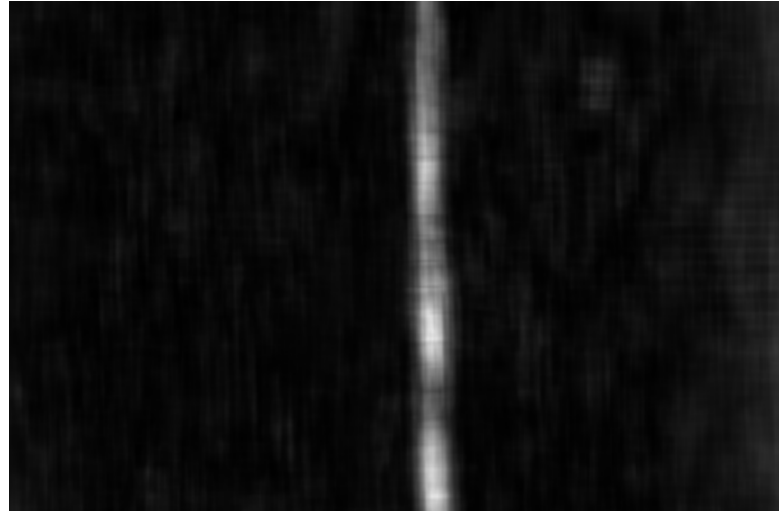
Eigenfilters

4 smallest
eigenvalues



Eigenfilters

Mahalanobis
distance



Threshold



On the menu:

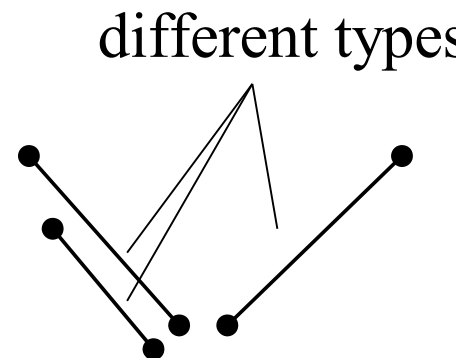
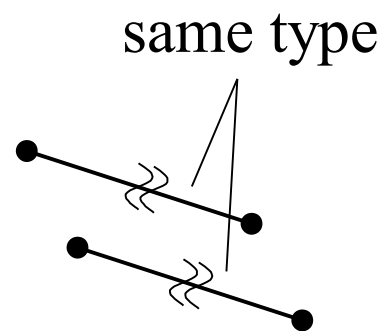
- Fourier features
- cooccurrence matrices
- filter banks (Laws, Gabor, eigenfilters)
- stochastic models

A 2-component texture model

1. Neighbourhood system

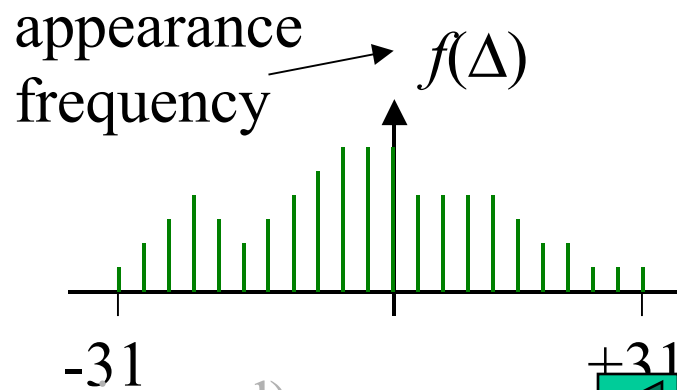
Pairs of pixels (Cliques)

Clique types:

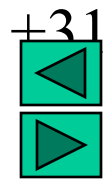


2. Statistical parameter set

Intensity difference
histograms:



(additionally histogram of singletons is used)



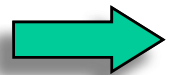
Histogram distance:

Δ - signal difference

$f(\Delta)$ - appearance frequency

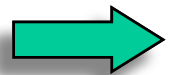
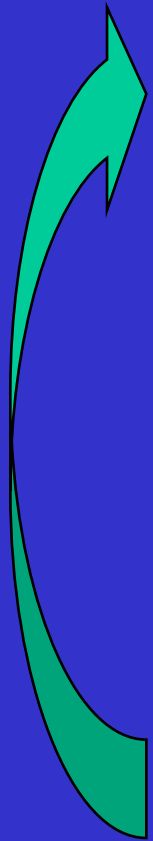
$$\forall \text{type } t: d_t = \sqrt{\sum_{\Delta} (f_t(\Delta) - f_t^0(\Delta))^2}$$

reference texture



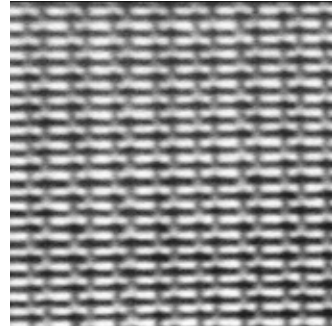
Analysis (clique type selection algorithm)

0. Collect reference histograms for all clique types (restriction on maximal clique length)
1. Collect histograms for the current synthesized texture (initially random noise)
2. Select the clique type with a maximal distance
3. If maximal distance $<$ threshold \Rightarrow **STOP**
4. Add clique type to the texture model
5. Synthesize texture based on new model
6. Go to 1

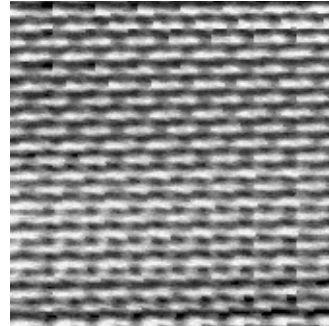


Clique type selection

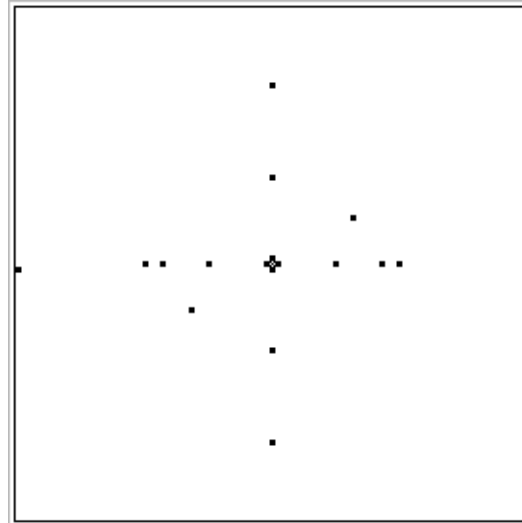
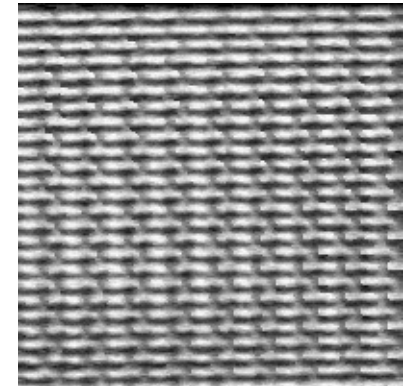
reference
texture



analysis
steps



final
synthesis

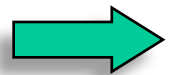
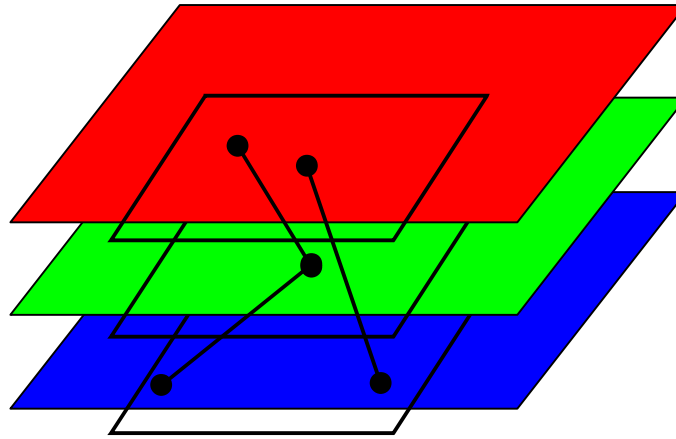


Successive
neighborhood system
update

9 clique types



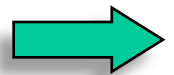
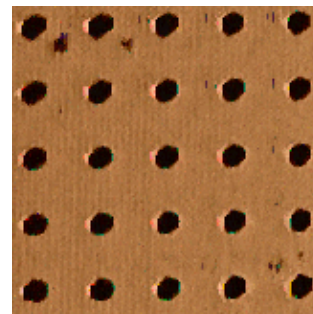
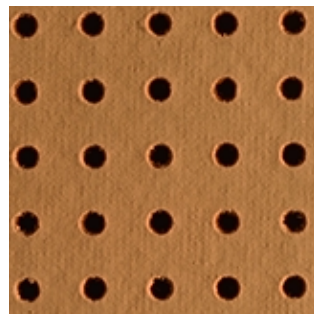
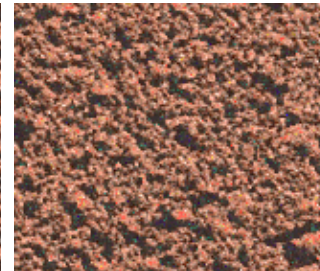
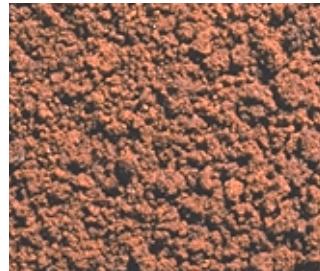
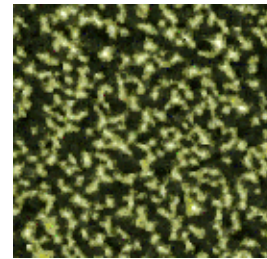
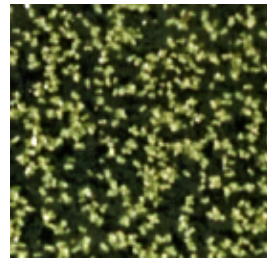
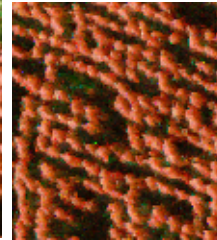
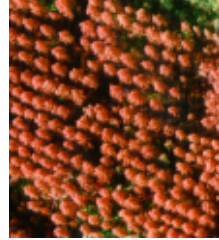
Interaction structure for color textures



Synthesized textures

Original

Synthesis



Ex2: cedars on Sagalassos' mountain



ready →



Ex.: cedars on Sagalassos' mountain



ready →



Ex.: cedars on Sagalassos' mountain



Note that texture synthesis was also used to remove the crane and van













Filling in of vegetation maps



ready →



Sagalassos landscape, synthetic



AUTOMATIC

ready →



Sagalassos landscape, with interactions



AUTOMATIC

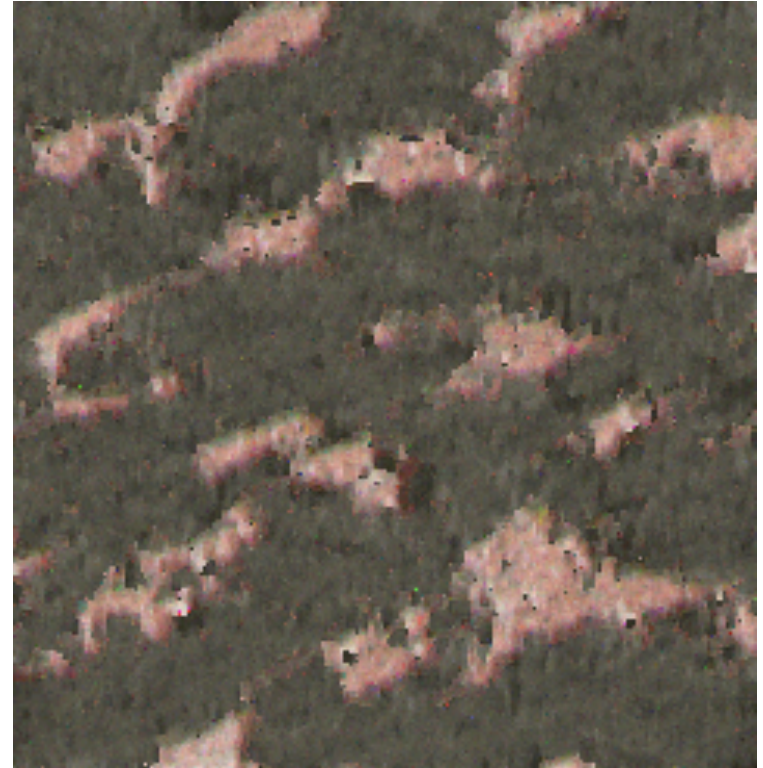
ready →



Sagalassos landscape with interactions



Example image



Synthetic image



Viewpoint / lighting dependent textures

Real orange

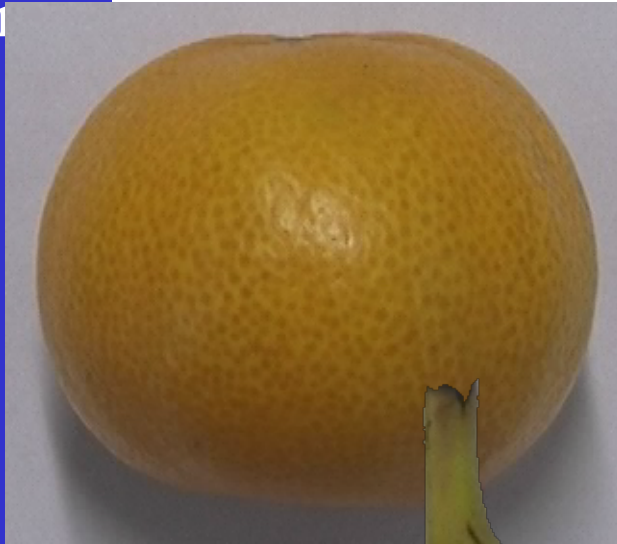


Synthetic orange

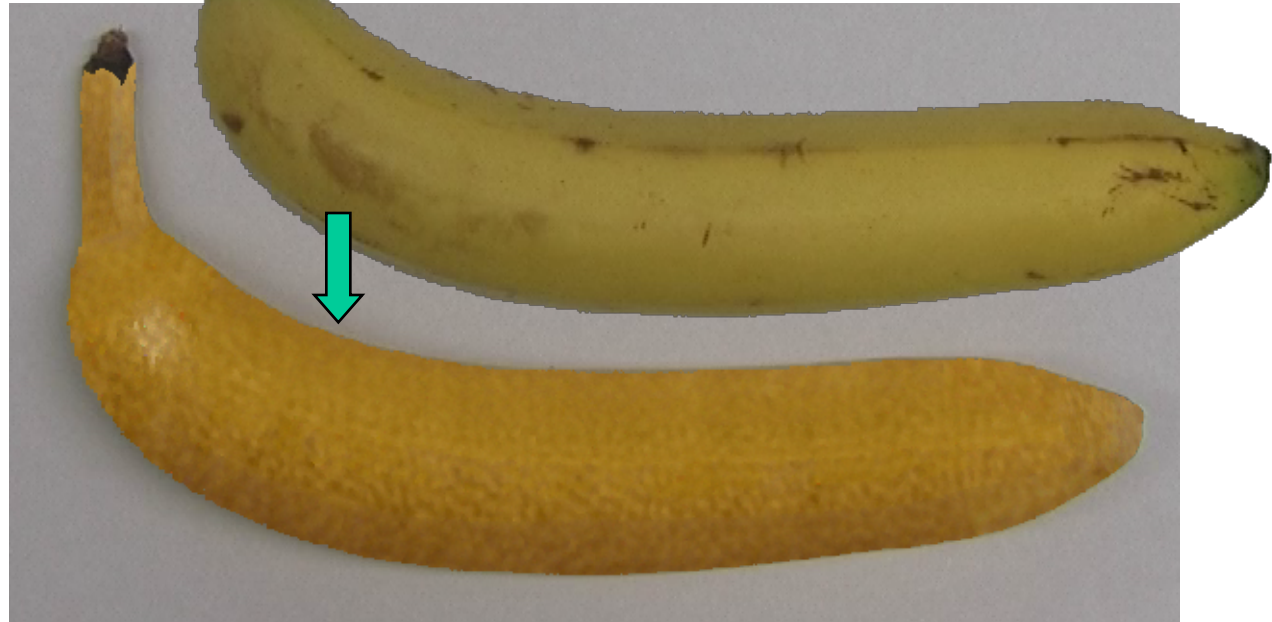


“Banarine”

Real tangerine



Synthetic tangerine



Example of 'smart copying'

Bush campaign digitally altered TV ad

President Bush's campaign acknowledged Thursday that it had digitally altered a photo that appeared in a national cable television commercial. In the photo, a handful of soldiers were multiplied many times.

Modified
Bush
2004
election
campaign
ad

This section shows a sampling of the duplication of soldiers.

